

Laser Source Modeling in WaveTrain

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Outline

- Short overview of WaveTrain
- Laser Resonator Modeling
 - Introduction & Theoretical Foundations
 - ResonatorSource Component
 - SimpleSaturableGain Component
- Examples
 - Stable Resonator without Gain
 - Stable Resonator with Gain
 - Unstable Laser Resonator

Introduction to WaveTrain

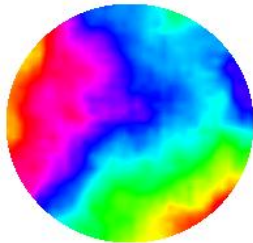
WaveTrain

wave optics made easier

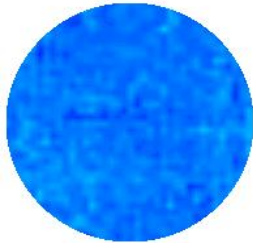
The Challenge of Wave Optics Simulation

Wave optics simulation is a crucial technology for the design and development for advanced optical systems. Until now it has been the sole province of a handful of specialists because the available codes were extraordinarily complicated, difficult to use, and they often required supercomputing resources.

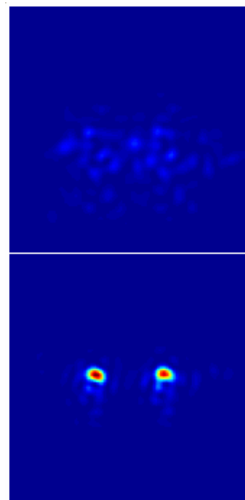
Without Adaptive Optics



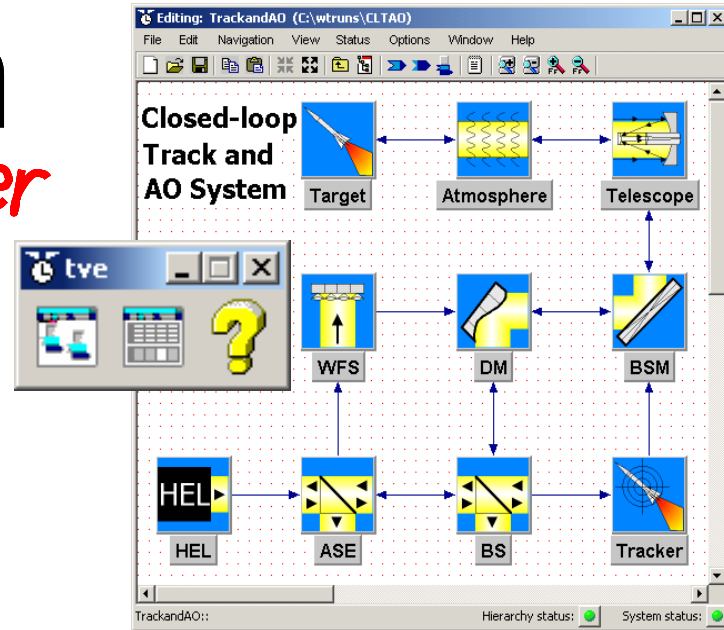
With Adaptive Optics



Phase



Image



The Solution is WaveTrain

WaveTrain puts the power of wave optics simulation on your PC. Through an intuitive connect-the-blocks visual programming environment in which you can assemble beam lines, control loops, and complete system models, including closed-loop adaptive optics (AO) systems.



For more information:
wavetrain@mza.com
www.mza.com
(505) 245-9970



What is WaveTrain?

- WaveTrain is a systems modeling and simulation tool that performs detailed physical simulations of complex closed-loop optical systems.
 - Supports arbitrarily complex sequential optical path modeling.
 - Adaptive optics controls including wavefront sensors and deformable mirrors.
 - Propagation through the atmosphere and other random media (e.g. aero-optics).
 - Continuous and discrete controls systems.
- WaveTrain is designed for ease of use, so that it can be used by a broad technical user community.
 - Plug-n-play block diagram editing and parameter specification.
 - Provides extensive features for a broad spectrum of users, from the occasional model “runner”, to the simple model “builder”, to sophisticated model “builders” and subsystem programmers.
- WaveTrain is designed to be reconfigurable, so that it can be used to model a wide variety of optical systems and experiments.
 - Users build-up models from a library of available components.
 - Programmers add their own components programming in C++, C, Matlab m-file, and Fortran.
 - Not limited to a particular propagation algorithm or phase screen implementation.
- WaveTrain provides wave optics and system simulation techniques in a true modern object-oriented programming (OOP) paradigm.
 - WaveTrain is not a graphical user interface (GUI) layered on top of a legacy wave-optics code.
 - WaveTrain is a bottoms up implementation of the fundamental features of composition-based simulation with emphasis on the modeling of optical systems.





WaveTrain Modeling References

General

find these at www.mza.com

- Extending the Hierarchical Block Diagram Paradigm for Modeling and Development of Large-Scale Systems, Comp. Sim. Conf., 1997
- WaveTrain: A User-Friendly Wave Optics Propagation Code, SPIE, 1999.
- WaveTrain Hands-On Workshop, 1999-present, MZA presentation.
- Introduction to Beam Control, 2003, MZA presentation.
- Choosing Mesh Spacings and Mesh Dimensions for Wave Optics Simulation, 2007, SPIE.
- Determining Wave-Optics Mesh Parameters for Complex Optical Systems, 2007, SPIE.

Short Courses and Tutorials

DEPS 2004 – Modeling and Simulation of Beam Control Systems

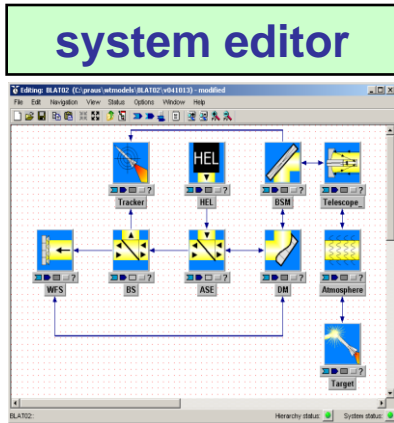
DEPS 2005 – Modeling and Simulation using WaveTrain

DEPS 2006 – Introduction to tempus

DEPS 2007 – Analysis of Optical Systems using Scaling and Wave-Optics Models

WaveTrain Process Flow

- Create test cases
- Devise parametric studies

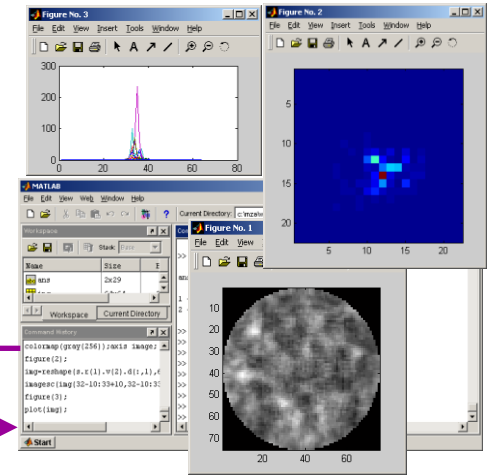


The runset editor window shows two tables: Run Variables and System Parameters.

Type	Name	Value	Description
1	stopTime	0.025	Simulation stop time
2	beam	Beam0	Control loop variable
3	band	0	Aberration randomization loop variable
4	control	0	Control parameterization loop variable
5	target	Beam0	Start angle to target (rad)
6	vectorWidth	Target(0:0:0.0)	Start vector (rad)
7	vectorWidth	Target(0:0:175.0)	Target velocity (rad/s)
8	beam	0.5	Telescope aperture diameter (m)

Type	Name	Value	Description
1	beam	beam0	Range to beamControl (m)
2	beam	beam0_range	Focal distance of telescope (m)
3	AcousticSpec	AcousticSpec0d_wavelengthDistancesStrength	Specification of acoustic AcousticSpec0d_wavelength
4	Acoustic	AcousticEquation_123456789rand	Random seed for phase screen
5	beam	stopTime	Maximum length of beam used to size phase screen
6	vectorWidth	vectorWidth	Platform velocity (m/s)
7	vectorWidth	vectorWidth	Target velocity (m/s)
8	vectorWidth	vectorWidth	Mid velocity assumed uniform throughout (m/s)
9	DMControl	DMControl	Specification of DM geometry
10	beam	beam0	Beam
11	beam	beam0_wavelength	Wavelength of outgoing beam (m)
12	beam	beam0_wavelength	Wavelength of incoming point source (m)
13	beam	beam0_wavelength	Wavelength of auxiliary point source (m)
14	beam	beam0	Location of the beam (m)
15	beam	beam0_x	X location of the beam (m)
16	beam	beam0_y	Y location of the beam (m)
17	beam	beam0_z	Z location of the beam (m)
18	beam	beam0_z	Number of grid points on the propagation grid
19	beam	beam0	Propagation grid spacing (m)
20	beam	beam0	Number of pixels on the targetboard

analysis



- Construct & modify tempus Systems
- Create Atomic System templates

The programming window shows C++ code for a WaveTrain system. The code includes headers for WaveTrain and WaveTrainInspector, and defines a class for the system. The code is as follows:

```

#include "WaveTrain.h"
#include "WaveTrainInspector.h"

using namespace WaveTrain;

int main() {
    WaveTrainInspector inspector;
    WaveTrain system;
    system.Initialize();
    system.Run();
    return 0;
}
    
```


- Visualize and analyze results

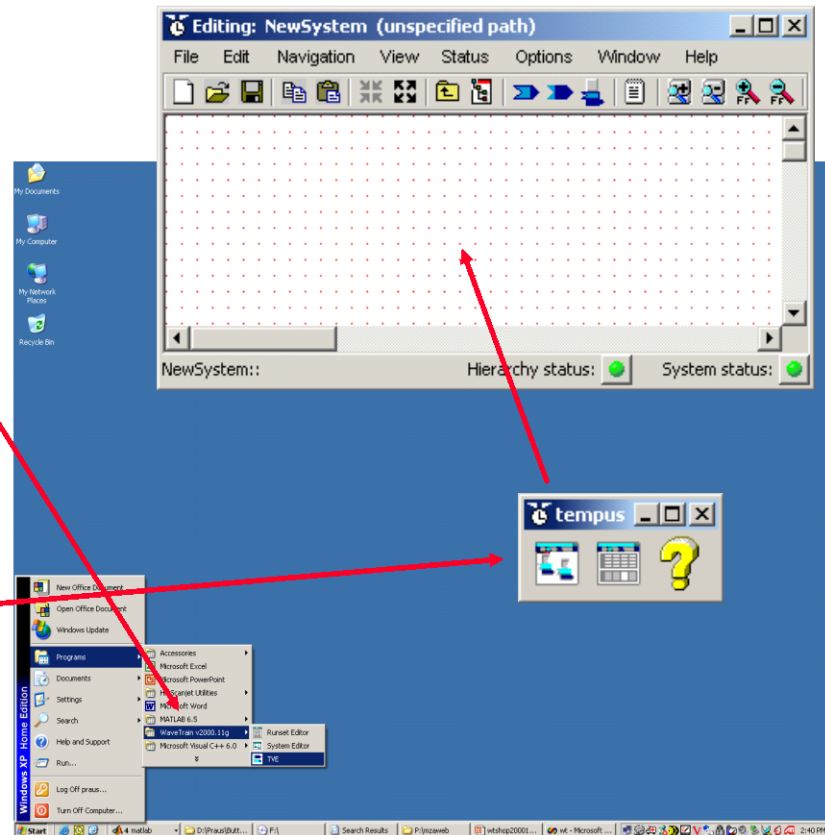
The process supports WaveTrain System development, debugging, and analysis

- Write Atomic Systems
- Debug applications



Starting the WaveTrain GUI (tve)...

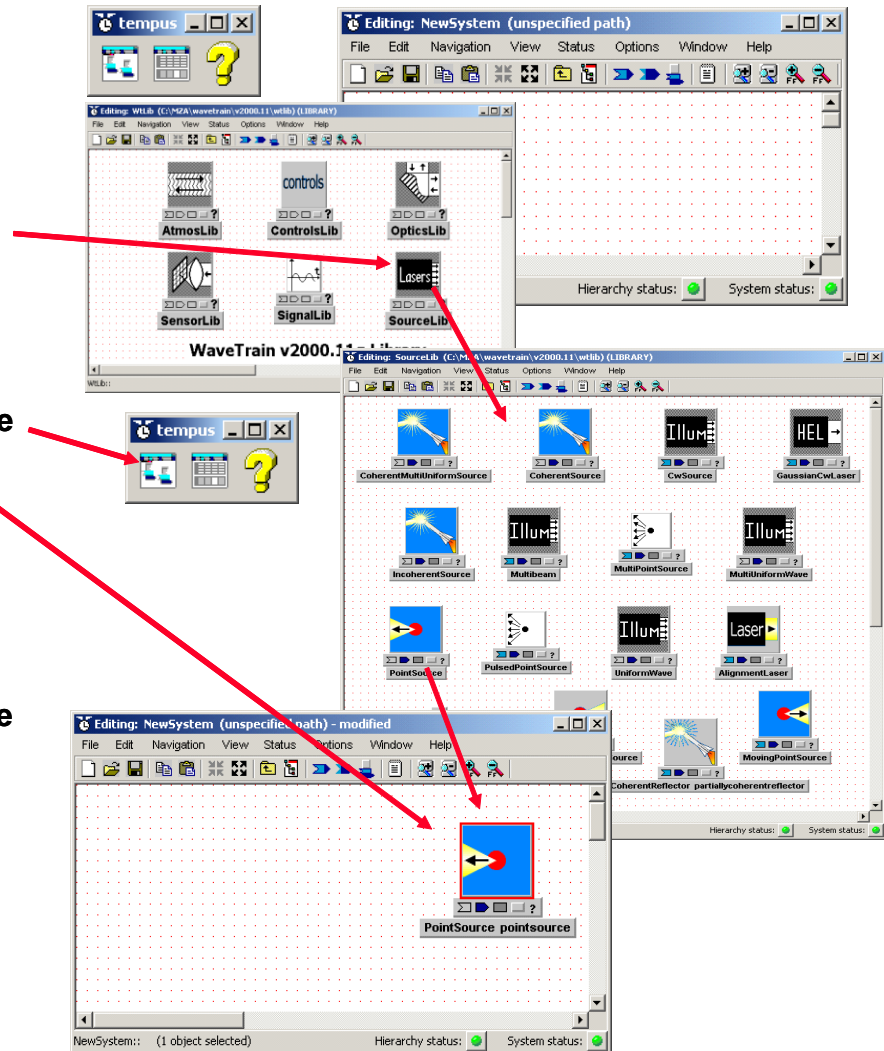
- WaveTrain is built atop tempus, a general-purpose simulation tool. In tempus, a system model is defined in terms of its interface (inputs, outputs, and parameters), its subsystems, and the connections between them. Each system model is mapped into a portable C++ class via automatic source code generation.
- To begin, **start the GUI by selecting WaveTrain v2000.11 TVE under the Windows Start-Programs menu** (possibly nested in a program group). This will bring up the tempus top-level window. Alternatively you can open System Editor or Runset Editor (TRE) by selecting the corresponding item in the WaveTrain program group.
-  **Click on** which will bring up the **System Edit Window** (skip this step if you started System Editor directly). When System Editor window comes up it already has a new system model, called "NewSystem", loaded by default.



WaveTrain includes a graphical user interface which is used to construct models by establishing relationships (connections) between the dynamic "Inputs" and "Outputs" of fundamental building blocks.

Copying from the component library...

- On your screen you should now have the tempus top-level window and two System Edit Windows, one for WtLib, one for NewSystem, as shown in the upper right.
- **Double-click on SourceLib** to “descend” into it. **Click on PointSource** to select it, then use **Ctrl-C** to copy it into the paste buffer.
- **Click on the NewSystem window**, then use **Ctrl-v** to paste a PointSource, which will appear in the upper left. **Move it to the upper right by clicking on it**, holding the button down, moving the mouse to the desired spot, then releasing it.
- **Click on the WtLib window**, then **double-click on white space** to ascend back to the top of the library.



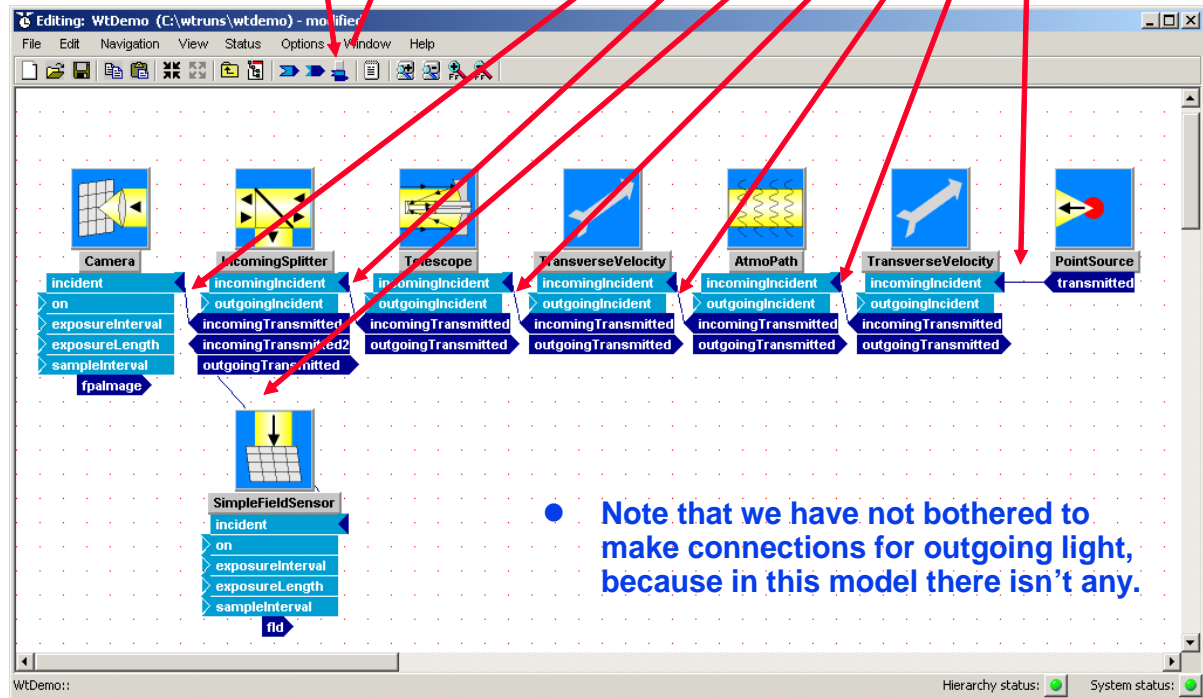
First, you have to copy modules from the WaveTrain component library.

Connecting the components...

- Click the toolbar button with image of the subsystem. A small menu will pop up.
- Select the button with a light blue “receptor” shape, also shown depressed at right. This will display all subsystem inputs. The window should now appear as shown in the upper right.
- Select the button with a dark blue arrowhead, shown depressed at right. This should cause all subsystem outputs (dark blue arrows attached to the bottom of each subsystem) to be displayed. If it does not work, click on white space and try again.



- Connect outputs to inputs as shown, by clicking on the pointed tip of each output, and dragging it to the receptor of the appropriate input.



Then you have to connect the components.

Specifying parameter values...

- **Undisplay** the subsystem inputs and outputs. The window should now look as shown in the upper right.
- **Click on the button with the medium gray rectangle** (lower left corner of the menu), which will display the subsystem parameters, as shown at the lower right



- For each parameter, the parameter name appears to the left, and its “setting expression” appears to the right, if any has been specified.
- Setting expressions are evaluated using the parameters of the containing system, but we have not yet defined any.

The screenshot shows the WTDemo software interface. The main window displays a system diagram with components: camera1, incoming splitter1, telescope1, transverse velocity3, atmospheric path1, transverse velocity1, and point source. Below the diagram, there are two panels showing parameter lists.

Parameter List 1 (Left):

focalLength	1.0
minWavelength	wavelength
maxWavelength	wavelength
nxyPupil	apdiam / propdxy
dxyPupil	propdxy
nxyDetector	64
dxyDetector	wavelength / apdiam
computationalLag	0.0

Parameter List 2 (Right):

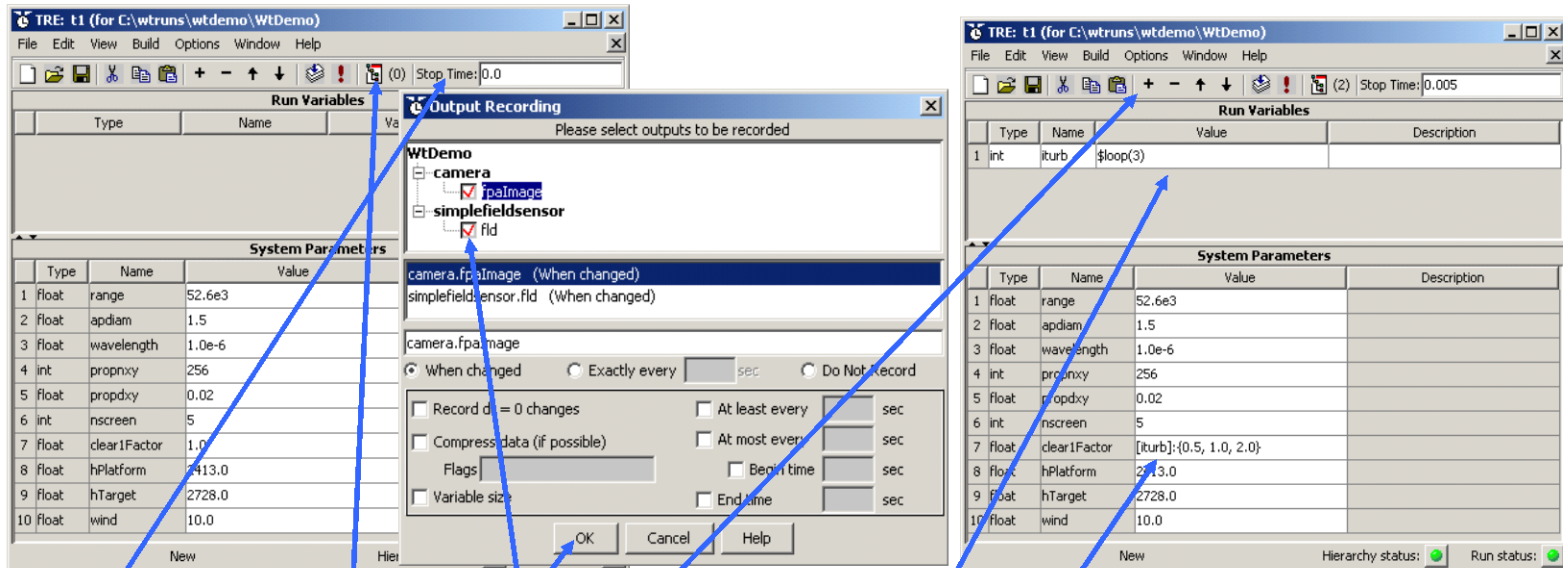
range	range
apertureRadius	apdiam/2.0
annulusRadius	0.0
vx	wind
vy	0.0
x0	0.0
y0	0.0
wavelength	wavelength
power	1.0e6
x	0.0
y	0.0


Parameter List 3 (Bottom):

atmSpec	AcSAtmSpec(wavelength,nscreen,clear1Factor,hPlatform,hTarget,range)
atmoSeed	-123456789
propnx	propnx
propdxy	propdxy
superApDiameter	1.8
edgeSigma	0.05
xp1	-propnx*propdxy / 2.0
xp2	propnx*propdxy / 2.0
yp1	-propnx*propdxy / 2.0
yp2	propnx*propdxy / 2.0
xt1	-propnx*propdxy / 2.0
xt2	propnx*propdxy / 2.0
yt1	-propnx*propdxy / 2.0
yt2	propnx*propdxy / 2.0
screenDxy	propdxy
xReferenceFocus	0.0
yReferenceFocus	0.0
locFlag	0

Followed by specifying values (and relationships) for parameters.

Creating a "runset" ...



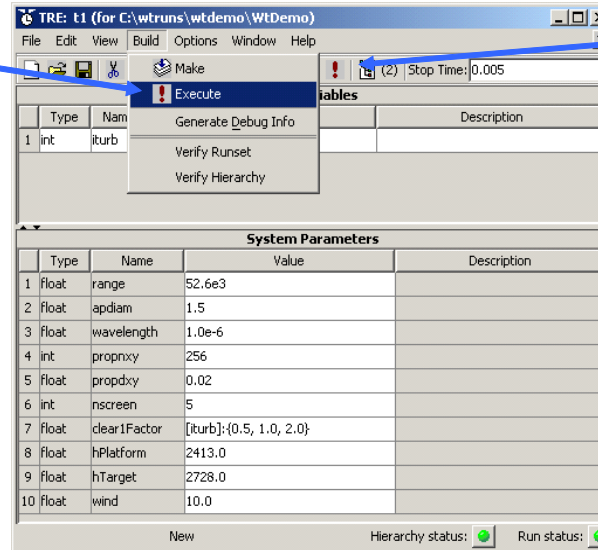
- Initially, the Runset will have all system parameters set to the defaults you specified when you built the system. The stop time for each run will be set to zero, and no outputs recording will be set up.
- Set the stop time to 0.005
- Click the button  (Recorded Outputs) to display a window for specifying output recording. Click on checkboxes next to each of the two outputs. Click "OK".
- Click the button "+" to create space for one run variable, then enter "int" "iturb" "\$loop(3)"; this will create a for-loop, resulting in three separate simulation runs.
- Set clear1Factor to "[iturb]:{0.5,1.0,2.0}"; so its value will change with each loop iteration.

WaveTrain and tempus names are case sensitive!

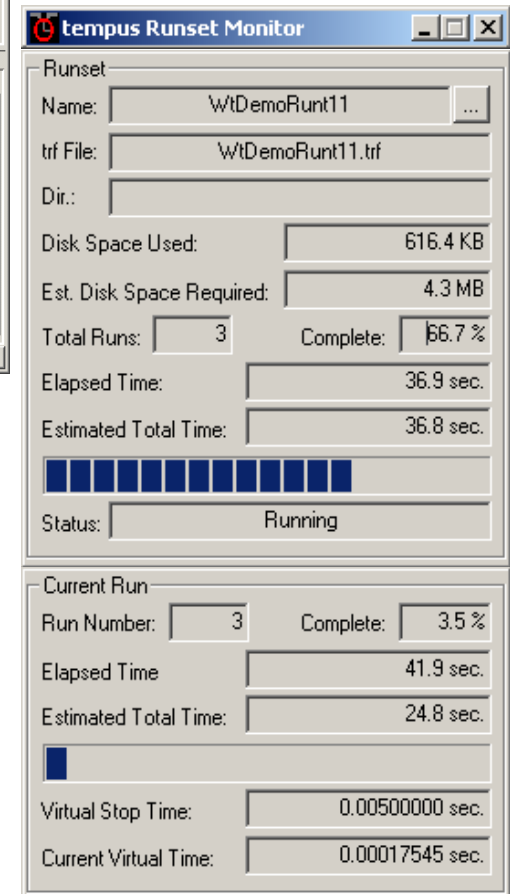
Create a "runset" which specifies the nature of the study you are to perform.

Running the simulation...

- Click on **Build->Execute**. This will automatically save the Runset Information to disk, generate the C++ main program, compile it, link it, and execute it.
- Shortly after execution begins, a “tempus Runset Monitor” will appear. This provides information such as elapsed time, disk space used, etc. When execution is complete, it will appear as shown.



- You could use the toolbar button to run instead.

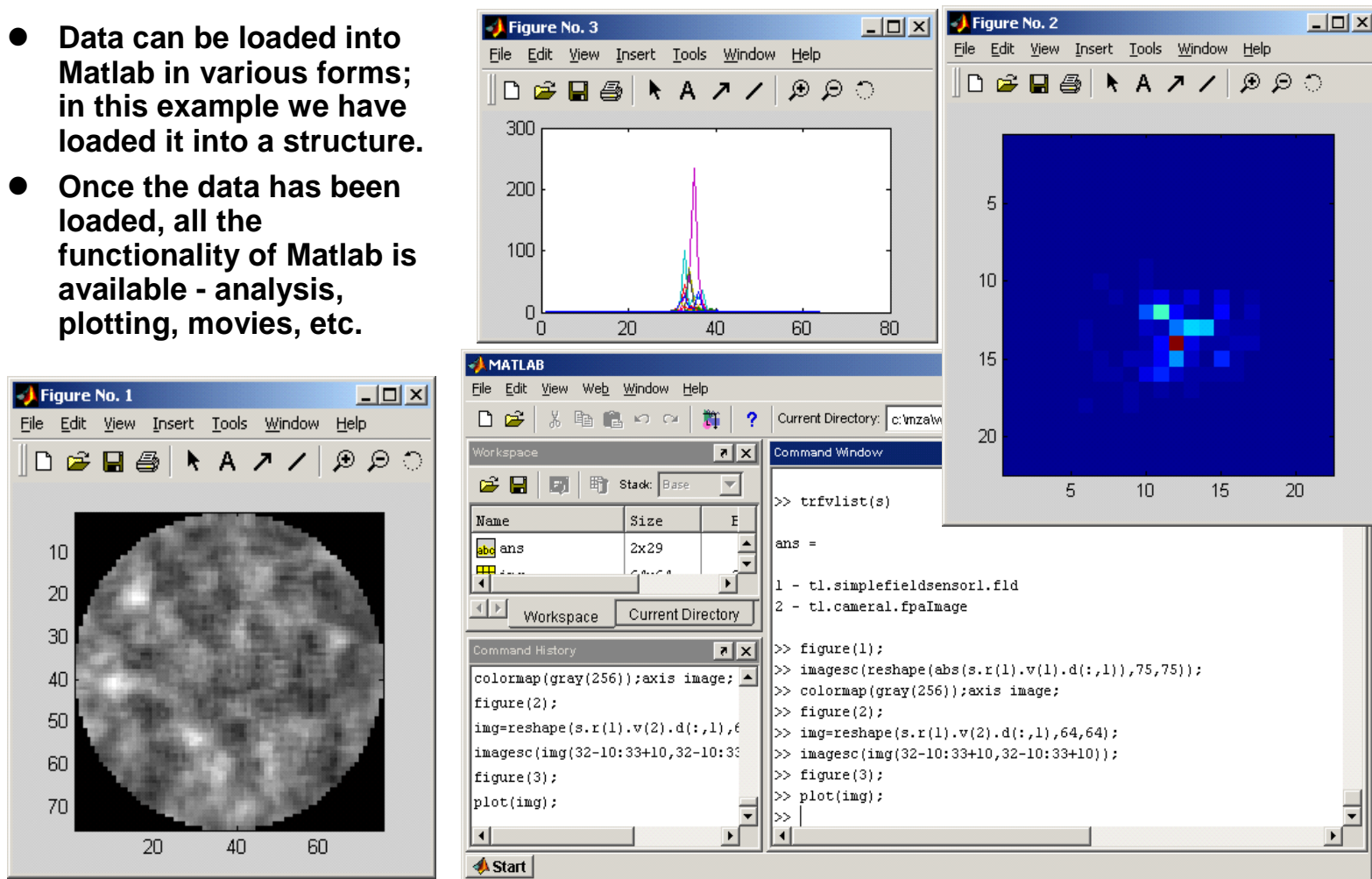


Run the simulation...

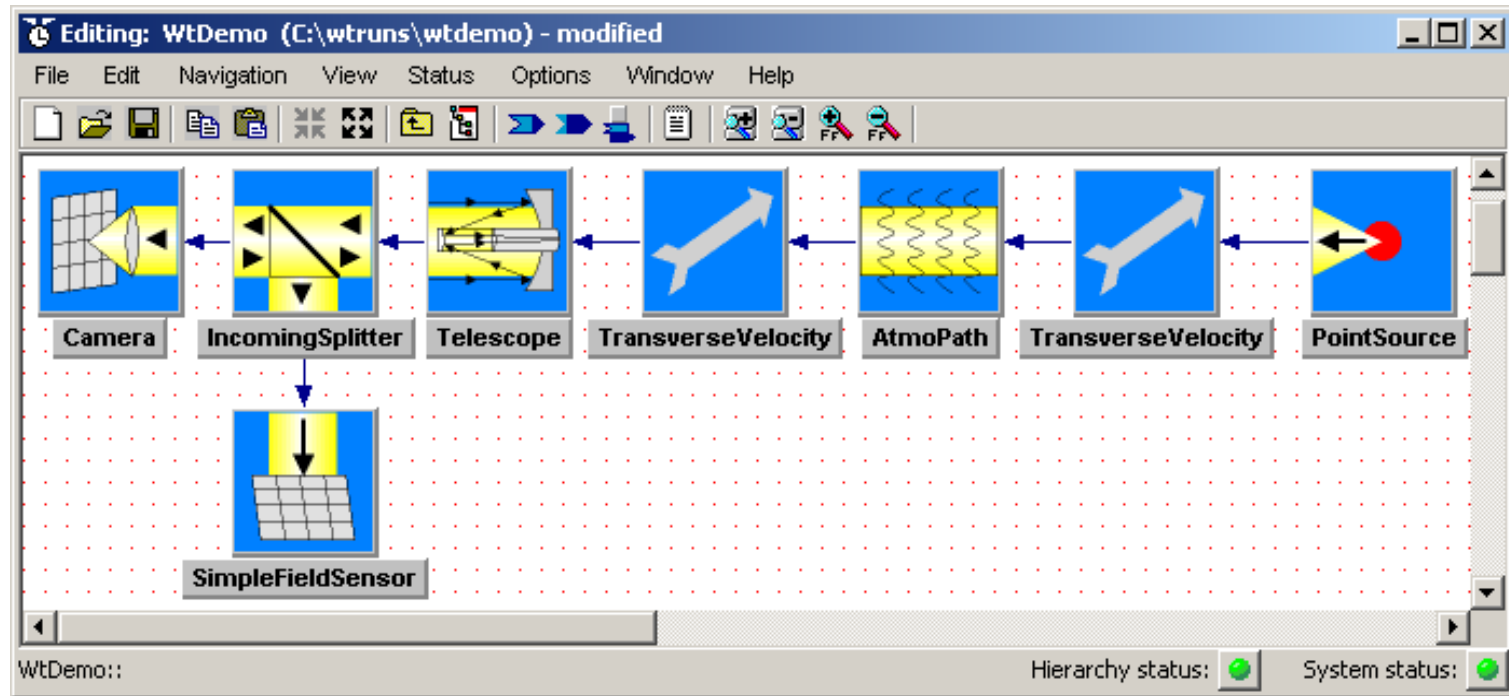
The time required to run a simulation can vary greatly. Some studies can be run in minutes. Others take CPU-years.

Analyzing the results in Matlab...

- Data can be loaded into Matlab in various forms; in this example we have loaded it into a structure.
- Once the data has been loaded, all the functionality of Matlab is available - analysis, plotting, movies, etc.

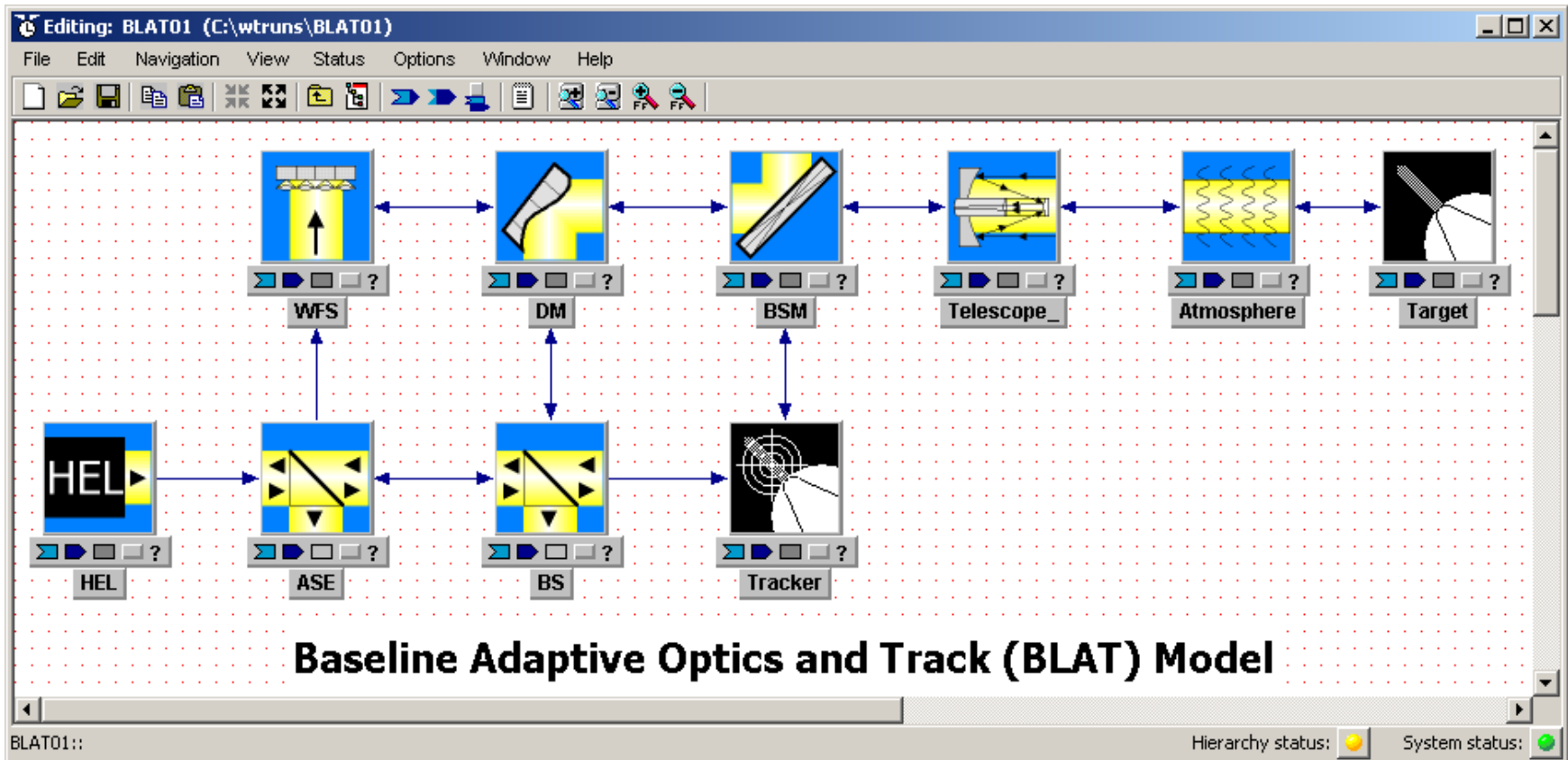


Finally, you can load the results into Matlab to visualize them.



- This is a model of a telescope system imaging a point source through turbulence.
- Model features:
 - Records amplitude and phase at the pupil plane, and intensity at the focal plane.
 - Models platform motion, source motion, and/or wind.
 - Uses standard turbulence models, e.g. Clear 1 or Hufnagel-Valley, and/or user-defined models.
 - All major system variables are parameterized, so they can be changed without changing the model itself.

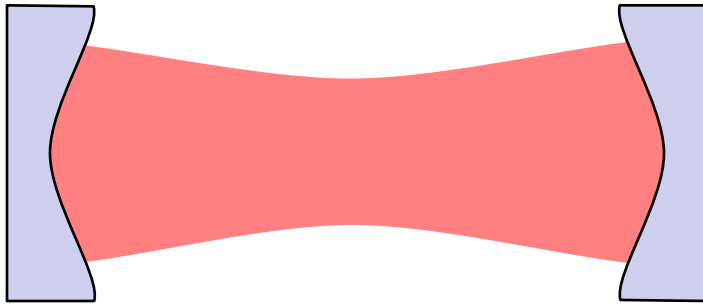
Baseline Adaptive Optics and Track (BLAT) Model



A closed-loop AO and track system using a standard tip-tilt centroid tracker and a tilt-removed least-squares reconstructor on a Shack-Hartmann wavefront sensor.

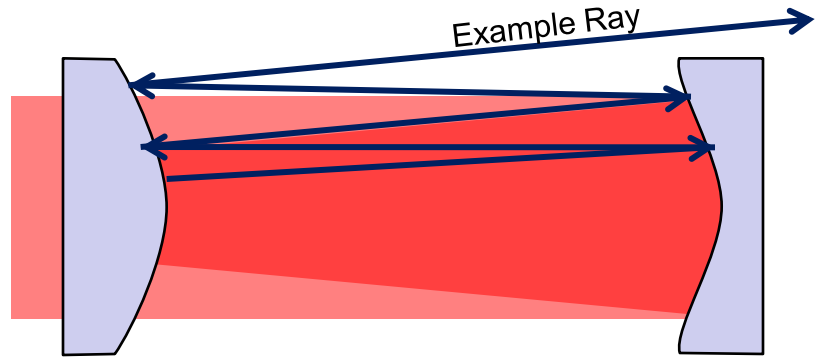
Laser Resonator Architectures: Stable vs. Unstable

Stable



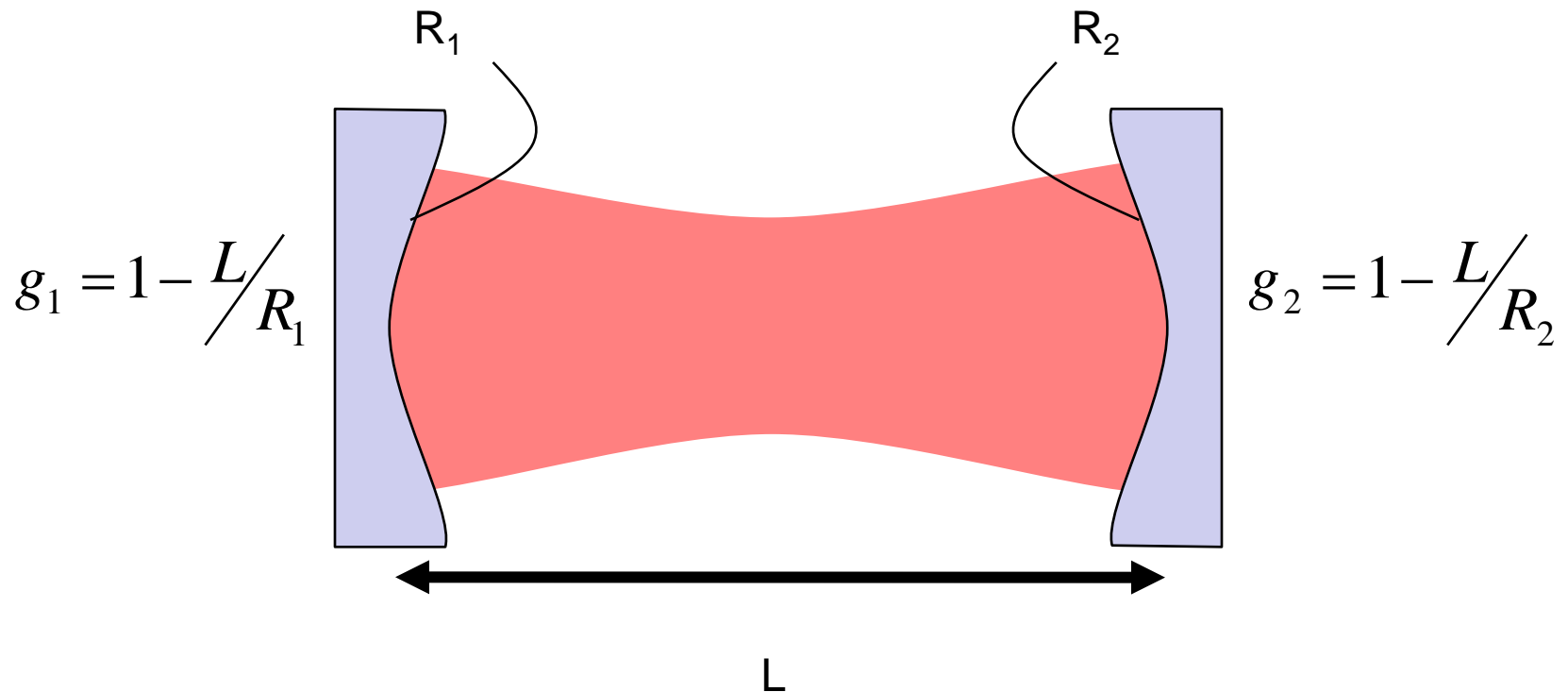
Rays captured by a stable resonator will never escape geometrically.

Unstable



All rays launched in an unstable resonator (except the on-axis ray) will eventually escape from the resonator.

Determining Resonator Stability



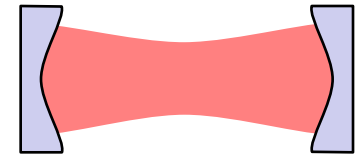
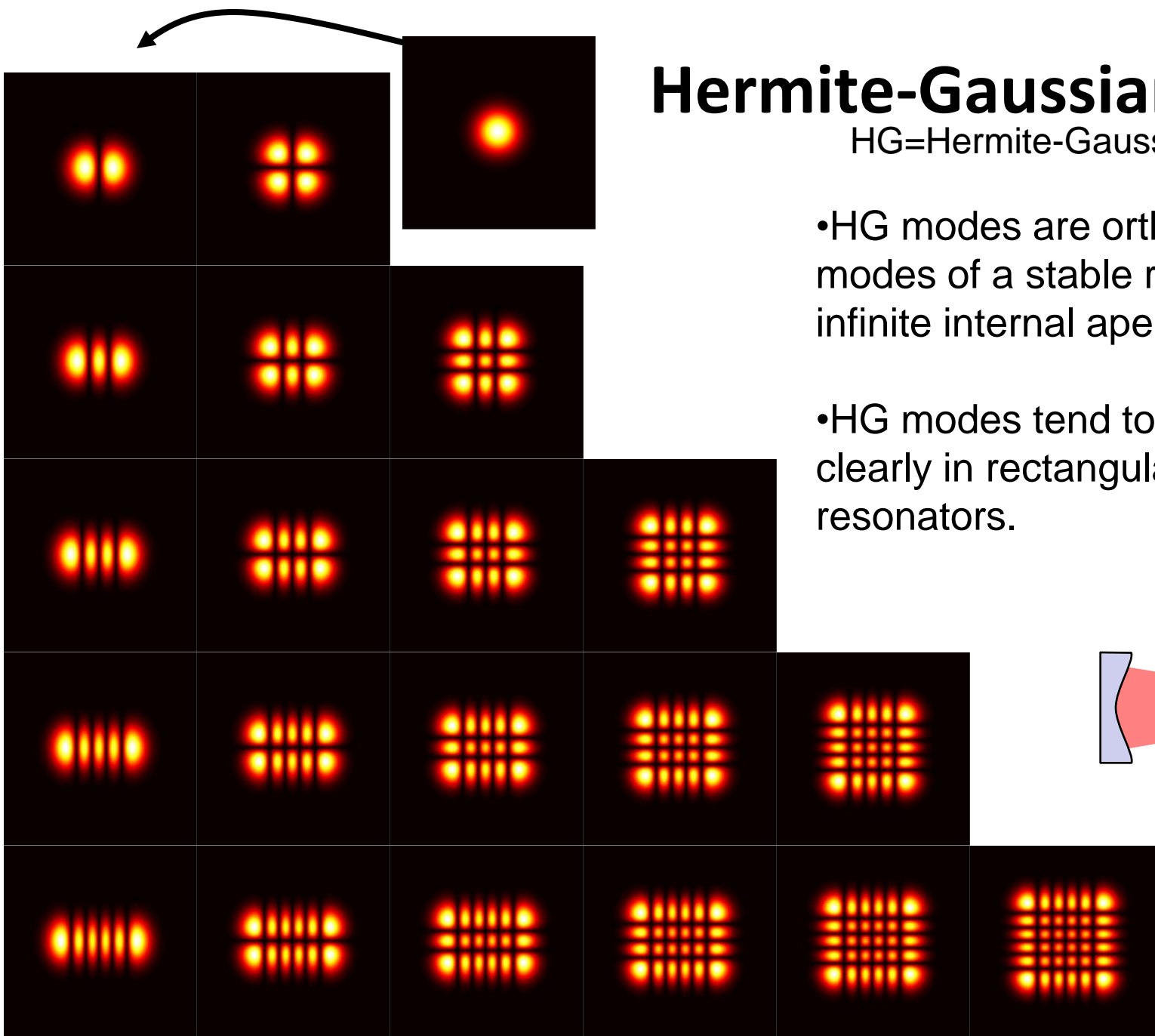
Stability Criteria

$$0 \leq g_1 g_2 \leq 1$$

Hermite-Gaussian Modes

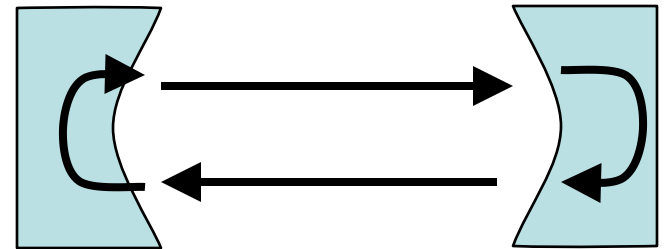
HG=Hermite-Gaussian

- HG modes are orthogonal modes of a stable resonator with infinite internal apertures.
- HG modes tend to appear clearly in rectangular-aperture resonators.



The Iterative Fourier Transform (aka Fox & Li) Technique

- A field is propagated through repeated round-trips until the field has converged to a stable field distribution.
- This is a commonly used technique for simplifying the 3D solution of Maxwell's Equations into a 2D problem (i.e. Gerchberg-Saxon technique)



A. G. Fox and T. Li. "Resonant modes in a maser interferometer", *Bell Sys. Tech. J.* 40, 453-58 (March 1961).

A. G. Fox and T. Li, "Computation of optical resonator modes by the method of resonance excitation", *IEEE J. Quantum Electronics.* QE-4, 460-65 (July 1968).

Comments on Fox & Li Solutions

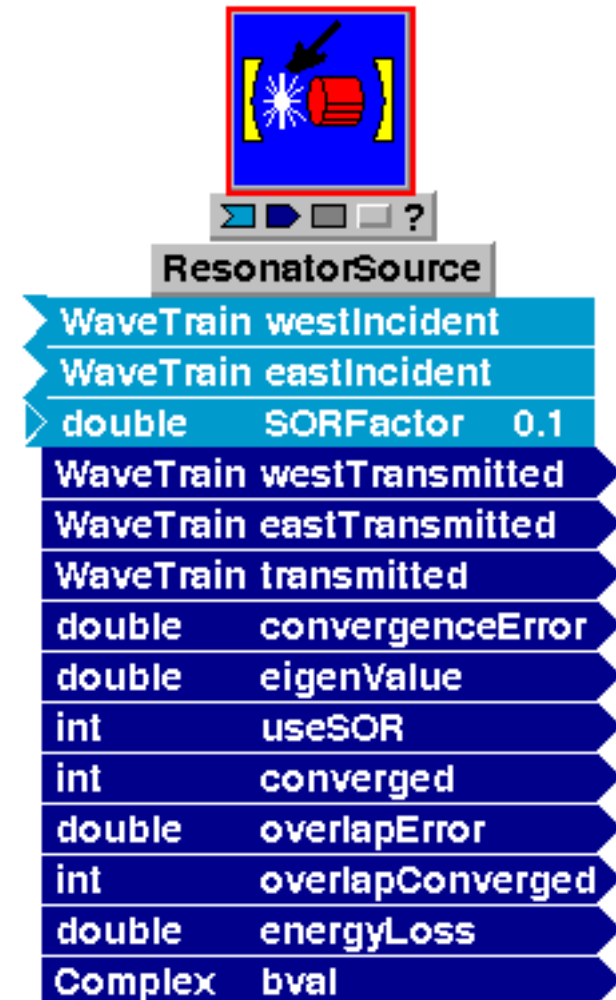
- Solution is for an instantaneous state, which is typically the steady-state of the laser.
- Stable resonators are much more computationally intensive to model than unstable resonators.
 - We attribute this to the geometric output coupling of an unstable resonator.
 - Larger eigenvalue difference between fundamental mode and the next higher-order mode.
- Not generally appropriate for pulsed or time-varying solutions unless the time-varying nature is much slower than a resonator round-trip time.
 - This is analogous to a split-time modeling techniques.

WaveTrain Components for Laser Resonators

- ResonatorSource
 - Core of all resonator modeling
- SimpleSaturableGain
 - Implementation of the approximate gain equation derived from the rate equations

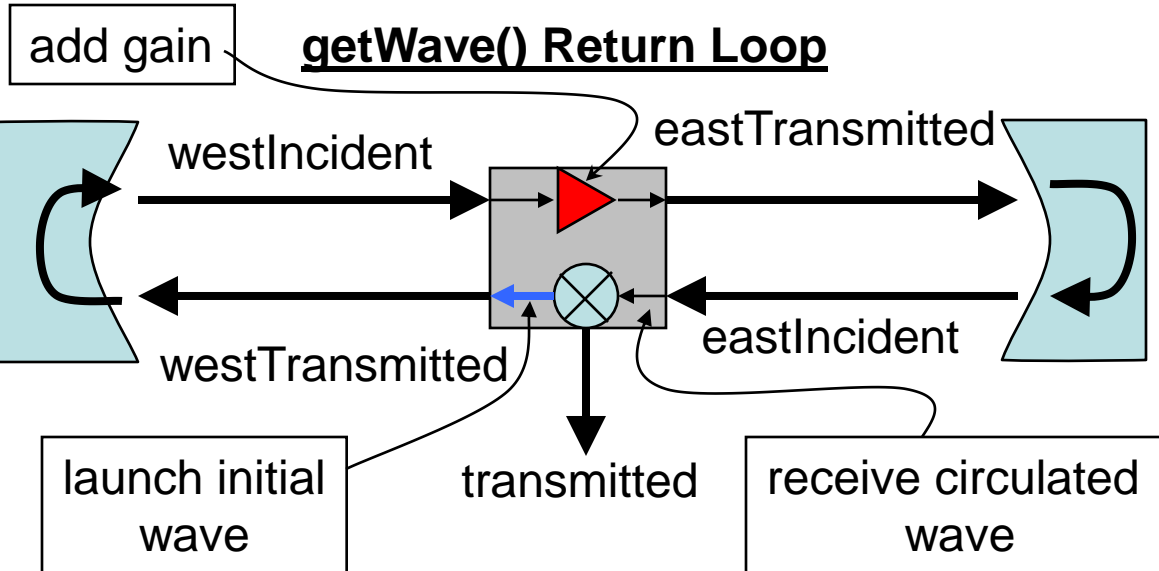
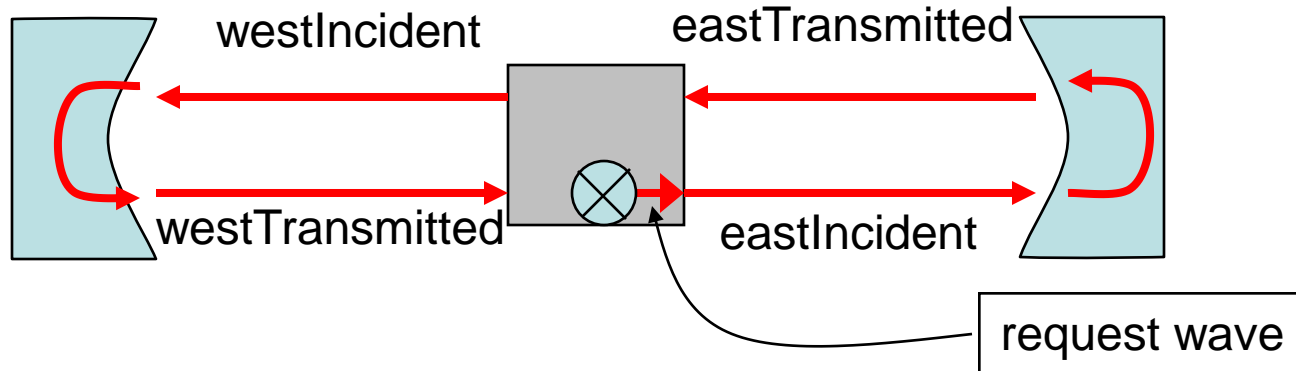
Introduction to the ResonatorSource in WaveTrain

- In WaveTrain, light is requested by a sensor and that query travels back through the path (or multiple paths) to the sources.
- ResonatorSource acts as both a sensor and a source because it both requests light and receives it.
- There is an output of the resonator source for evaluating the laser output during the Fox & Li iterations.



General RS Functionality

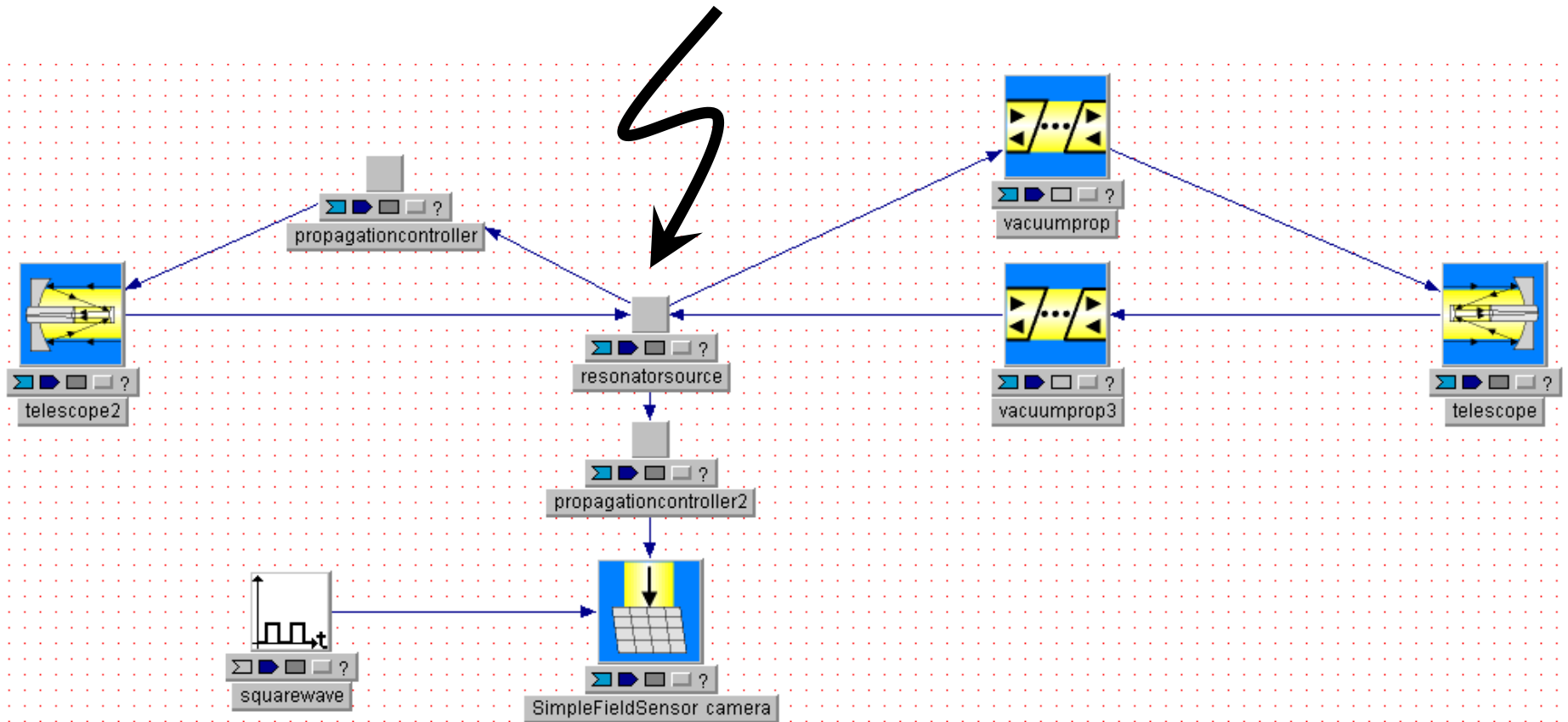
getWave() Query Loop



General ResonatorSource Functionality

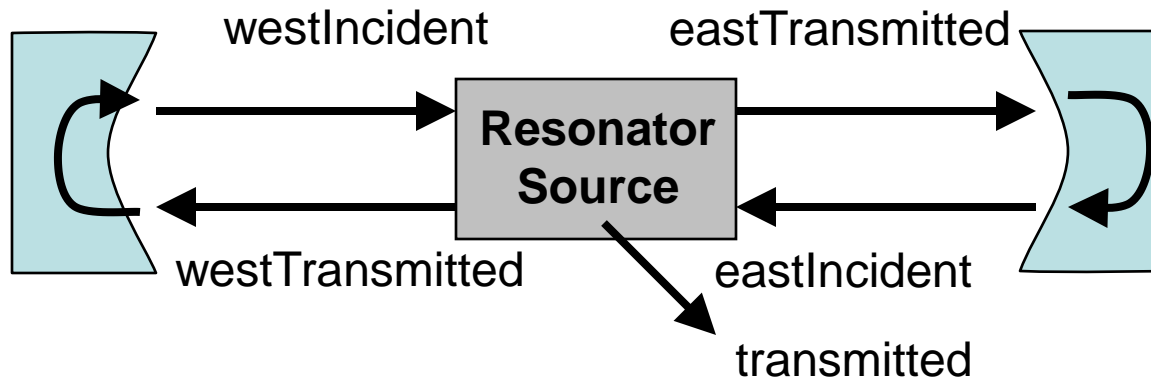
- Generally, the Resonator Source (RS):
 - passes waves going from west to east and adds gain to them,
 - returns the result of the last iteration for waves going east to west,
 - calculates the convergence error and eigenvalue, and
 - responds to outside requests for a wave by returning a wave from the wave buffer.

Development of a WaveTrain Resonator Source for Fox & Li



The WaveTrain Resonator Source

- Inputs
 - WaveTrains: westIncident, eastIncident
- Outputs
 - WaveTrains: westTransmitted, eastTransmitted, transmitted
 - Doubles: convergenceError & eigenValue



The WaveTrain™ Resonator I/O

- Inputs
 - westIncident - wave from the west
 - eastIncident - wave from the east
- Outputs
 - westTransmitted - wave out to the west
 - eastTransmitted - wave out to the east
 - transmitted - wave out of the resonator
 - convergenceError - error associated with the iterative convergence (rms difference between the field amplitudes)
 - eigenValue - ratio of two consecutive fields

Resonator Source Key Parameters

- Parameters
 - wavelength, initial field
 - roundTripLength - total propagation distance for one round-trip through the resonator
 - storageGrid - geometry of the buffer storage
 - gain - resonator gain factor
 - startTime - time to start the first light from the source
 - storageInterval - time interval upon which to sample the field
 - storageDuration- maximum storage look-back time duration

Gain Models

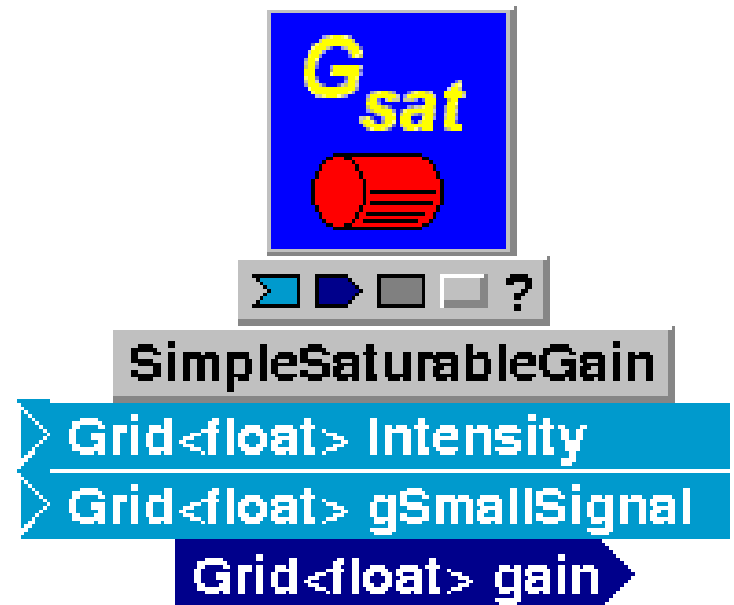
- WaveTrain currently has interfaces to several different gain models (some of which are proprietary to our commercial customers), but the most commonly used is SimpleSaturableGain.
- ComplexSaturableGain allows the user to specify a 2D gain and saturation intensity field.
- More complex effects like ASE have been successfully added to the saturable gain models as an additional factor.
- Interfaces to high fidelity gain models have also been demonstrated for COIL modeling (GASP interface and OCELOT interface)

SimpleSaturableGain

- Gain in laser medium is represented by the WaveTrain component SimpleSaturableGain
- This component adds gain to the incoming beam according to the equation:

$$G = \exp\left(0.5 \cdot \alpha \cdot L \cdot \left(\frac{1}{1 + I/I_{sat}}\right)\right)$$

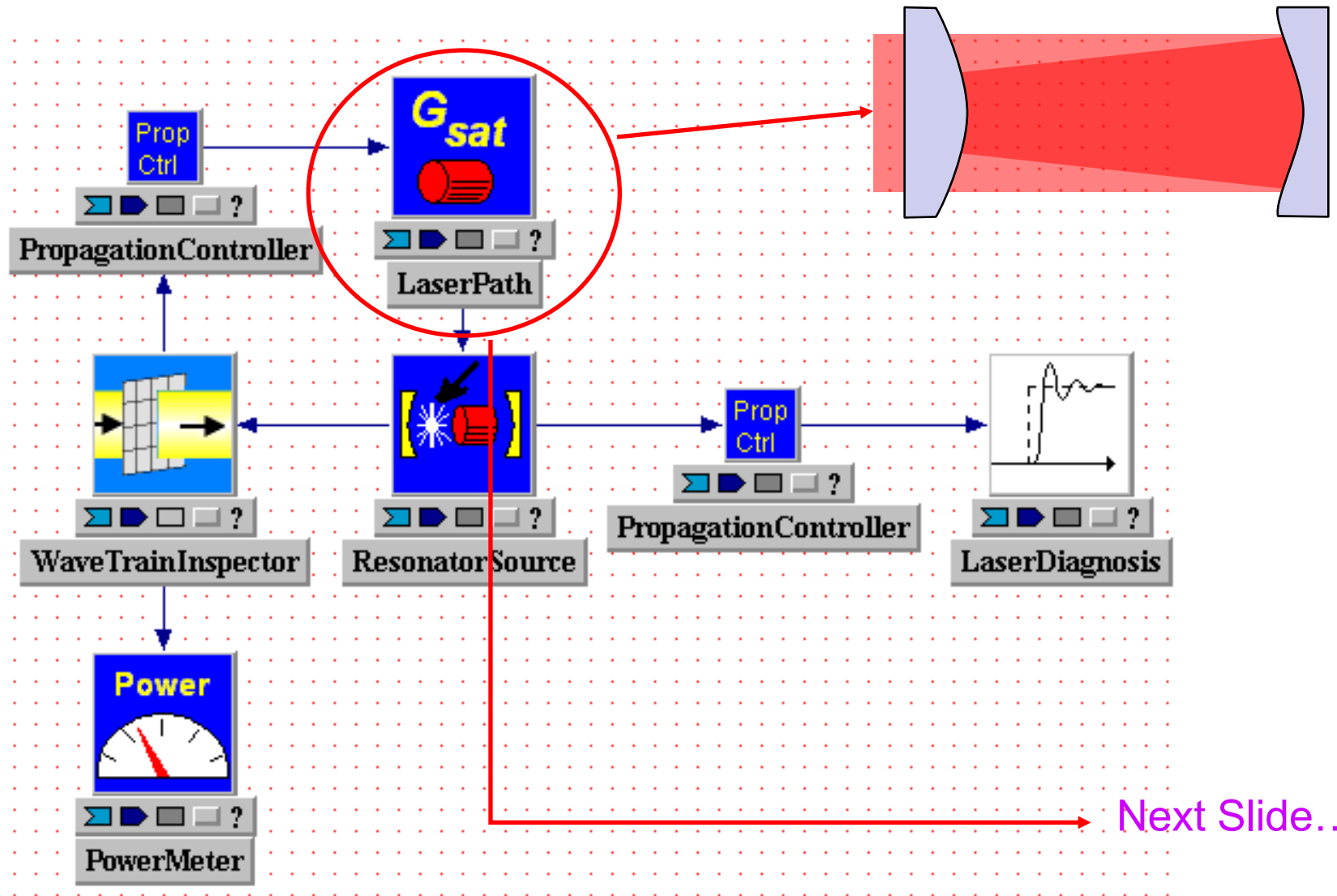
where α is gain per unit length,
L is cavity length, and
 I_{sat} is the saturation intensity



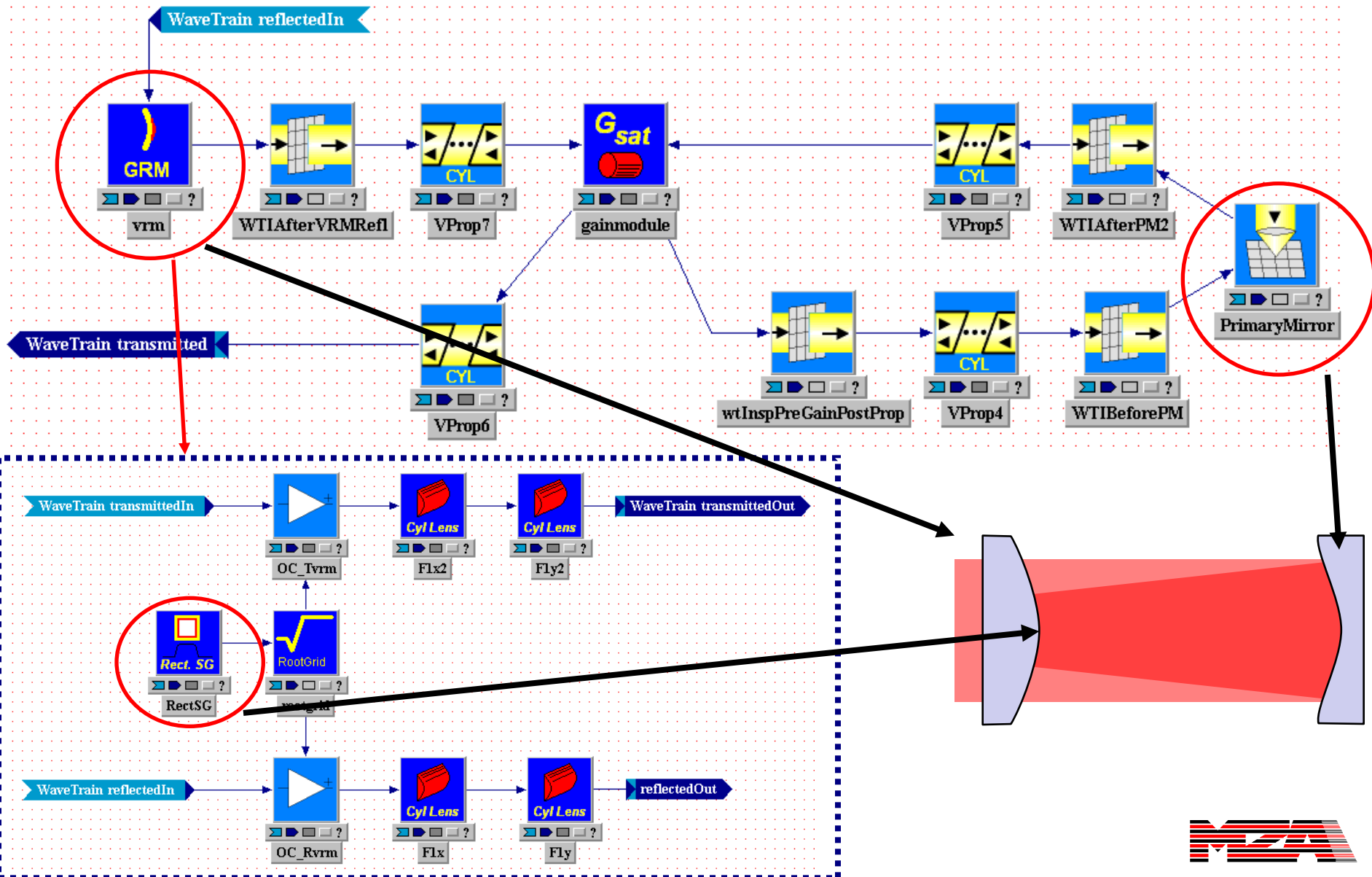
Unstable Laser Resonator

- Predictions from Theory
- WaveTrain Model Setup
- Example Parameters
- Results & Comparison with Theory
- Conclusions

WaveTrain Model



WT Model of Variable Reflectivity Mirror (VRM)

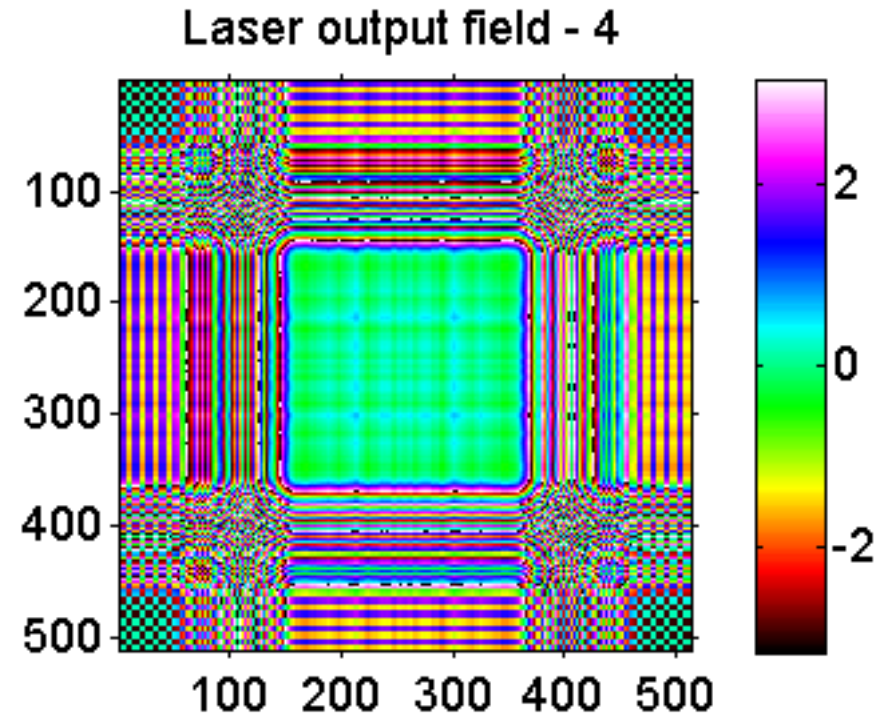
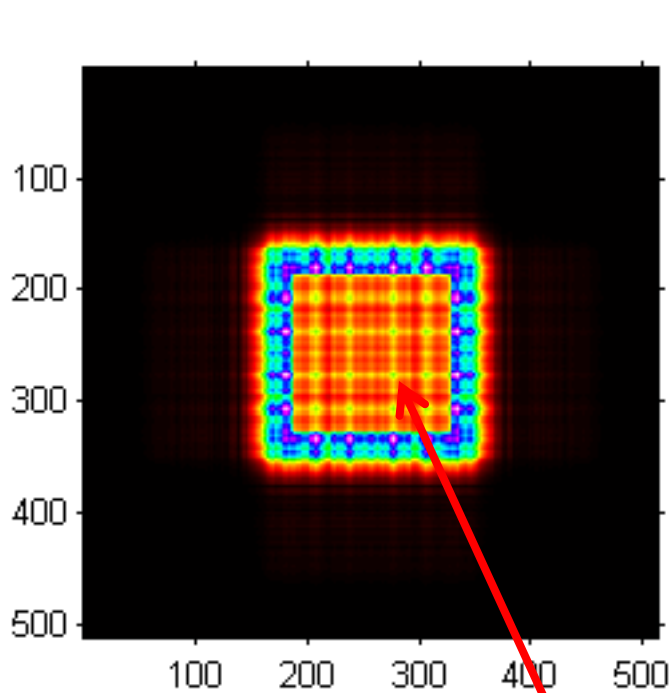


Parameters

- NumAvgs_vec = 1
- Reflectivity = 0.9
- Iterations = 4
- Rpm (Radius of curvature of primary mirror) = 7 m
- Rsm (Radius of curvature of secondary mirror) = -5 m
- cavityLength0 = 1.0 m
- Propagation Grid = 512 by 50e-6
- Ssgain = 1.0
- Amp0(Amplitude of initial field) = 15000
- Radius of initial field = 3.0e-2 m
- Wavelength = 1e-6
- Saturation intensity = 1e7 W/m²
- Normalization = 0
- convergenceThreshold = 1e-9
- GainLength = 1.0
- Aperture Width (AW) = 1cm
- Magnification (M) = 1.4(Rpm/Rsm)
- Rectangular gaussian waist = AW / (2*M)



Output Field After 4 Iterations with a 200th Order Super-Gaussian

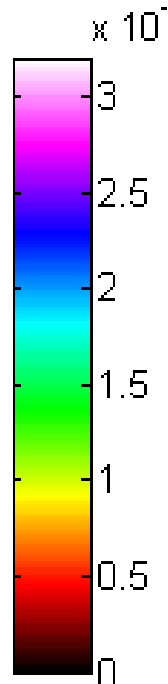
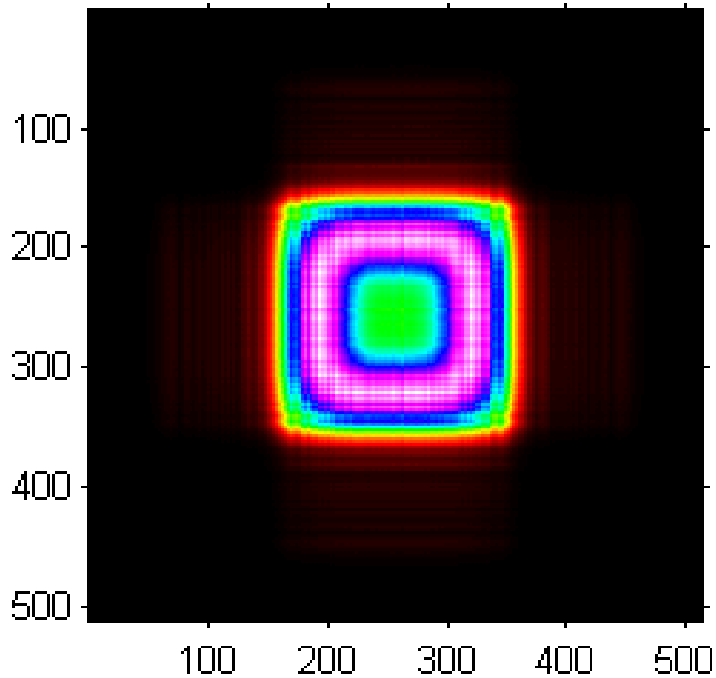


Significant structure
from Fresnel ringing

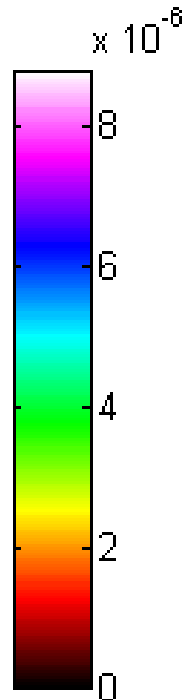
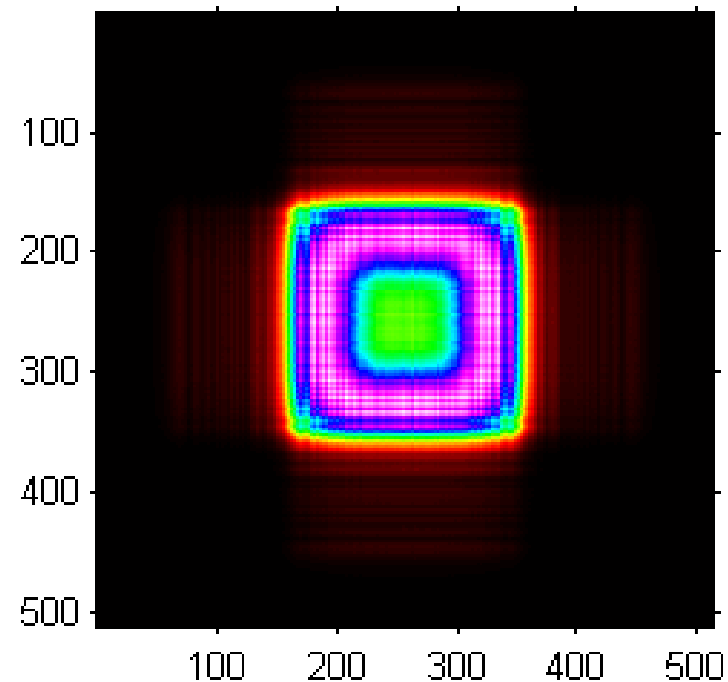
The Unstable Resonator Mode is Established Very Early.

4th Order Super-Gaussian

After Four Iterations



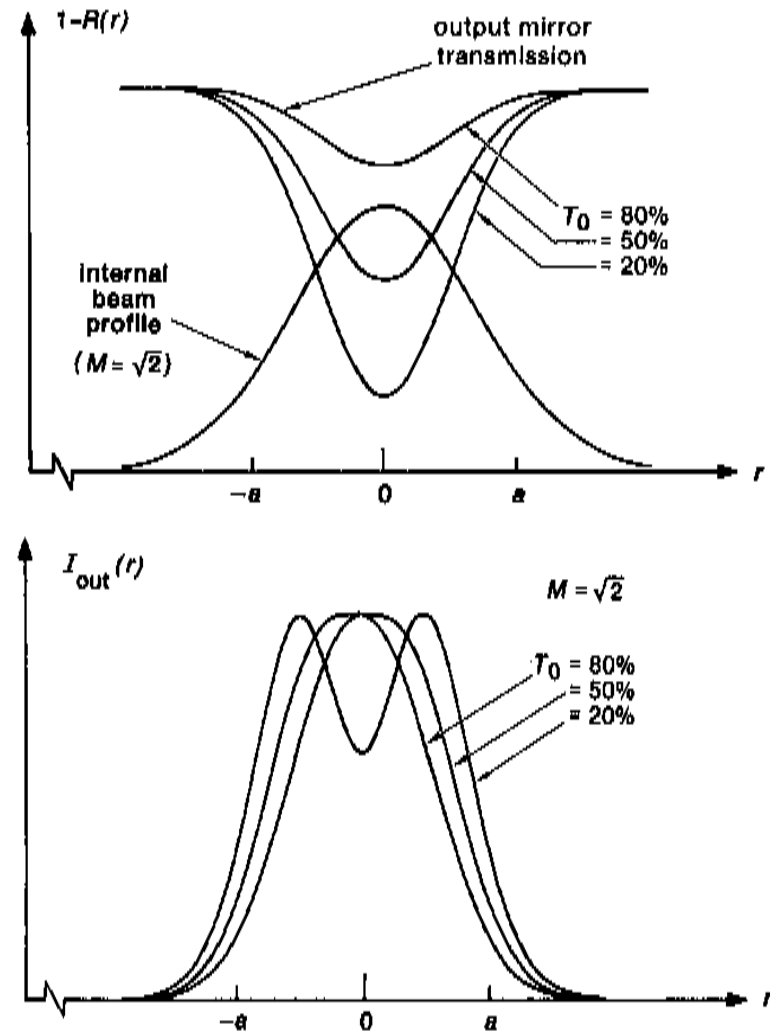
After 1000 Iterations



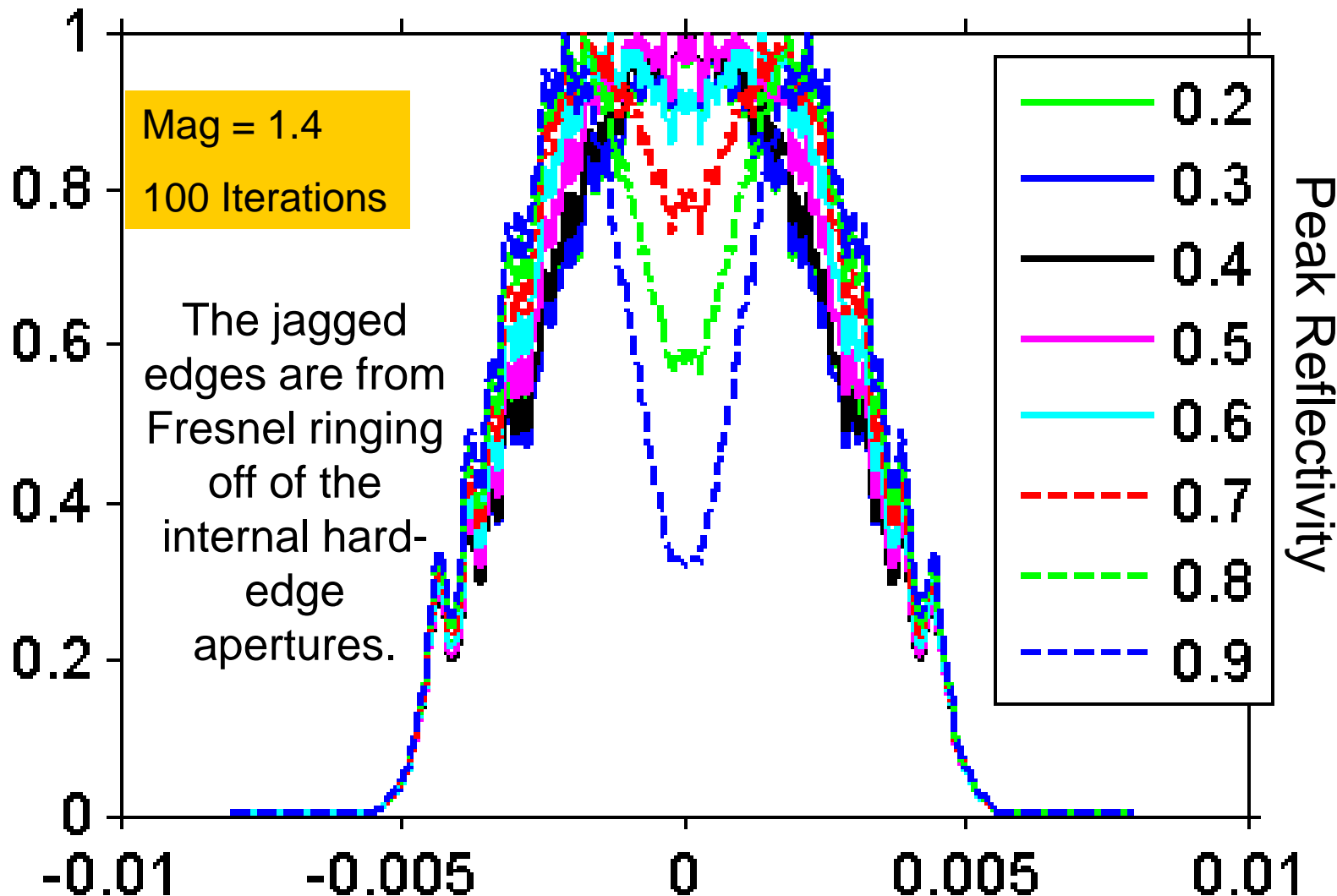
Fresnel ringing still present from the internal aperture.

GRM Unstable Resonator Theory

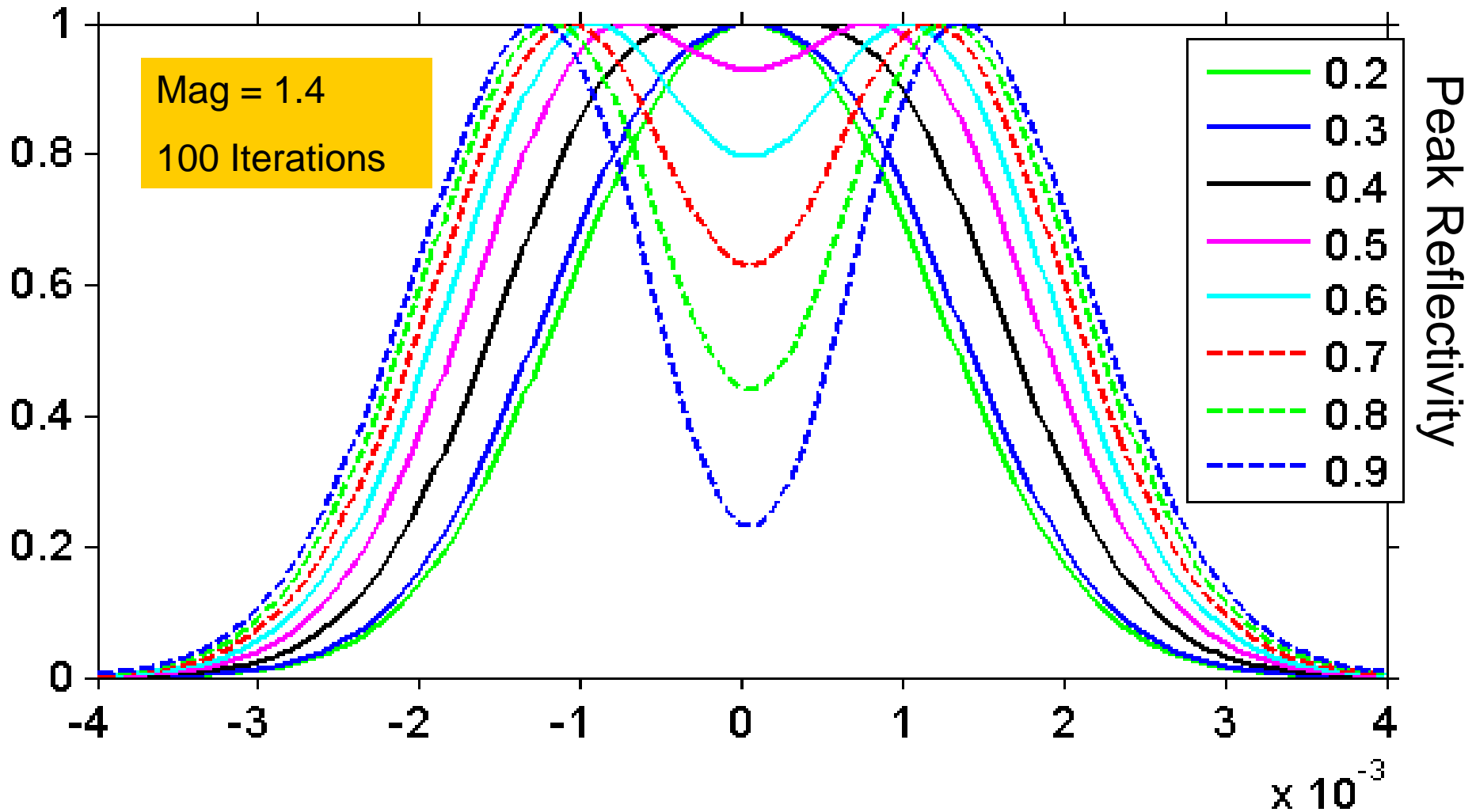
- To avoid Fresnel ringing at the edges of the beam, give the laser designer more control over the output beam profile, and reduce the effect of the spot of Arago, many laser designers use variable or graded reflectivity mirrors (VRMs or GRMs) in their resonators.
- Siegman presents some of the theory behind a gaussian GRM in Lasers.
- In the next few slides, we use WT to duplicate the results described by Siegman for a gaussian GRM.



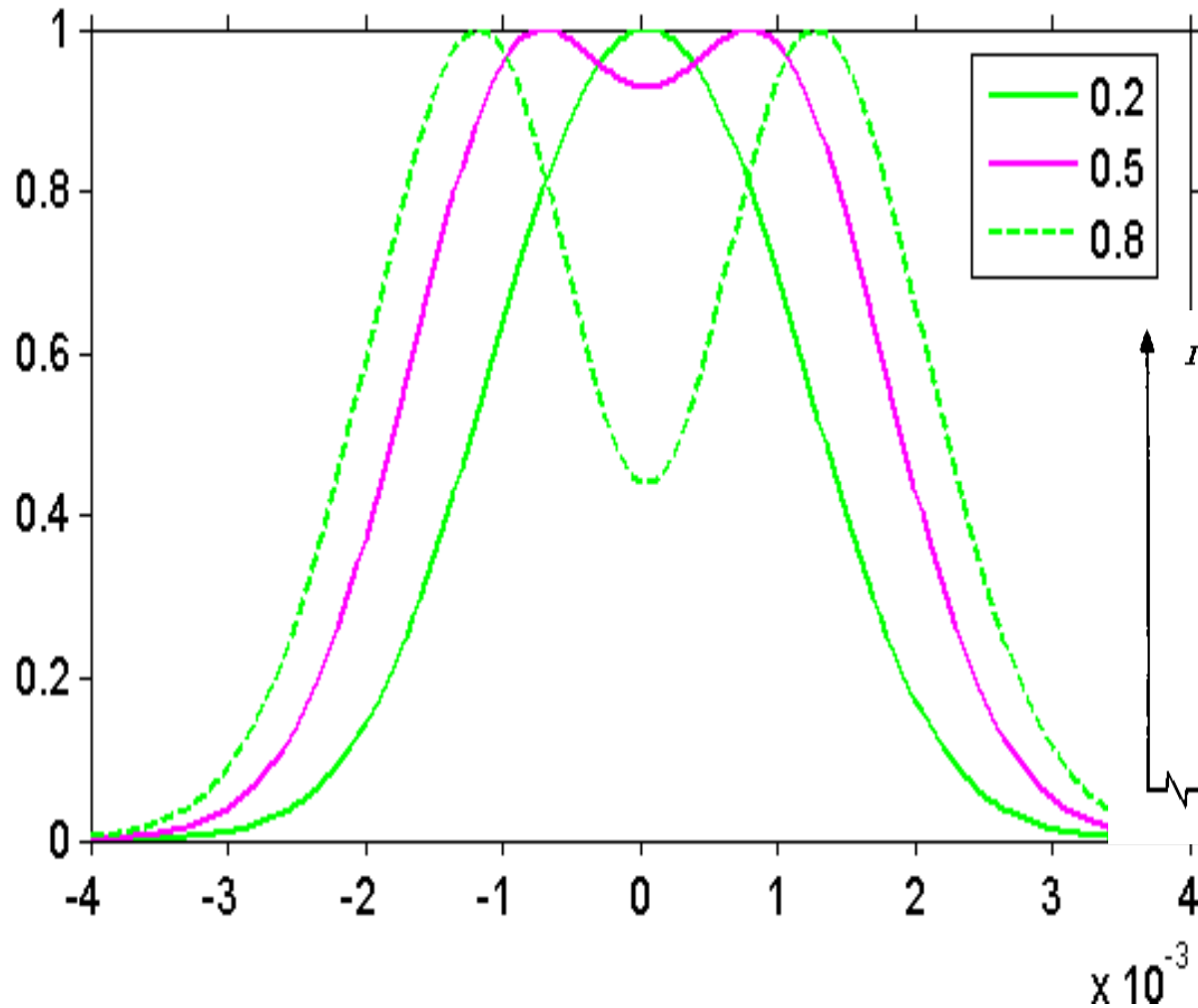
Gaussian GRM Intensity Profiles



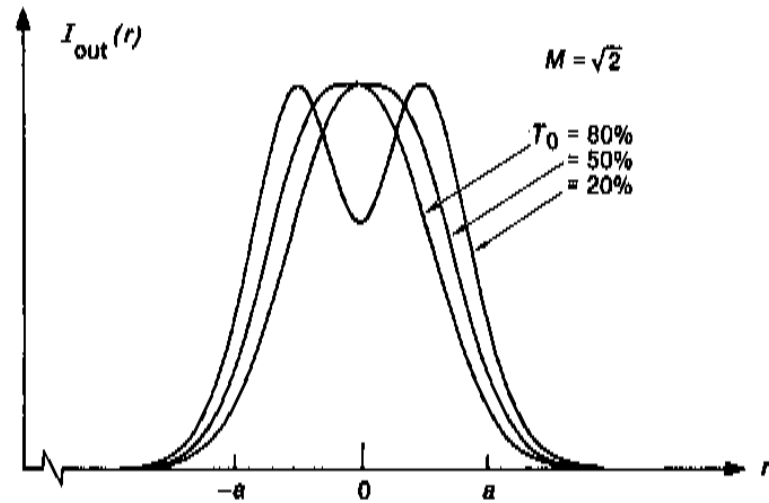
Gaussian GRM with Larger Apertures



Comparison to Siegman's Results



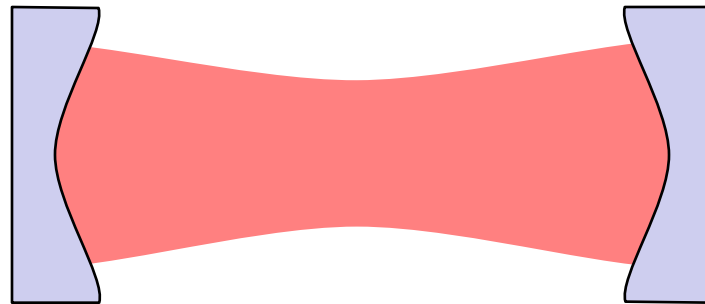
We see here a slight discrepancy, but the shapes are quite similar.



Conclusions

- We have presented how we have adapted WaveTrain to model laser resonators.
- We presented examples of modeling results from stable resonators with and without gain and unstable laser resonators with gain.
- We also presented a new modeling technique for increasing the speed and stability of models of multi-mode stable laser resonators.

Stable Resonator Without Gain

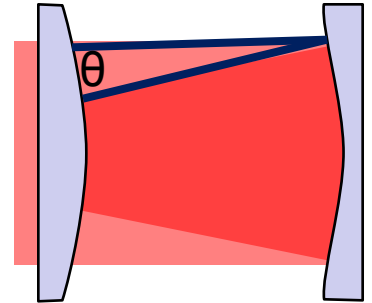


Stable Resonator without Gain

- Predictions from Theory
- WaveTrain Model Setup
- Example Parameters
- Results & Comparison with Theory
- Conclusions

Mesh Parameters for Laser Modeling

- Most Rigorously Correct Method:
 - Determine the mesh required for a round-trip and use that mesh.
 - For systems of simple optics, use the technique outlined by [Mansell, Praus, and Coy](#)
- Simple Approximation: Determine the mesh required for the propagation between the two end-optics using the simple [Coy and Mansell](#) formulas embodied in the [MZA worksheet](#).
- Unstable Resonator Approximation: Determine the maximum ray angle needed to map the scraper hole or GRM edge to the edge of the primary/collimating mirror.
- Stable Resonator Corollary: Reduce the required mesh angle by the number of round-trips for ray-reproduction/imaging (more discussion on how to calculate this factor later).



$$\theta \approx \frac{\left(D_{\max} - \frac{D_{\max}}{M} \right)}{L}$$

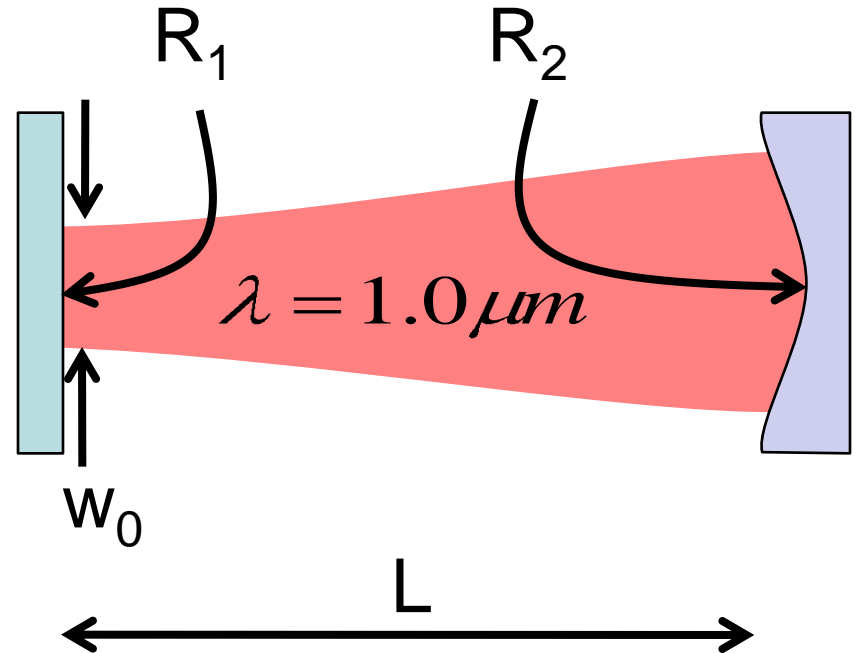
$$= \frac{D_{\max}}{L} \left(1 - \frac{1}{M} \right)$$

$$\theta \leq \frac{\lambda}{2\delta} \Rightarrow \delta \leq \frac{\lambda}{2\theta}$$

$$N \geq \frac{D_{\max} + \theta \cdot L}{\delta}$$

Plano-Concave Resonator Lowest-Order Mode

$$w_0^2 = \left(\frac{\lambda}{\pi} \right) \left[R_2 - L \right]$$



Example: $\lambda = 1\mu\text{m}$, $L = 0.8\text{ m}$, $R_2 = 10\text{ m} \rightarrow w_0 = 0.93\text{ mm}$

Notes on Lowest Order Mode Theory

- Derivation:
 - The lowest order mode (Gaussian) size is can be derived for any resonator using Gaussian beam propagation equations.
 - Example: For the plano-concave resonator, when is the wavefront curvature equal the end mirror radius of curvature or $R(z=L) = \text{ROC}_{\text{primary mirror}}$.
- This theory assumes no internal apertures or gain media.

$$w(z) = w_0 \left(1 + \left(\frac{z}{z_R} \right)^2 \right)^{1/2}$$

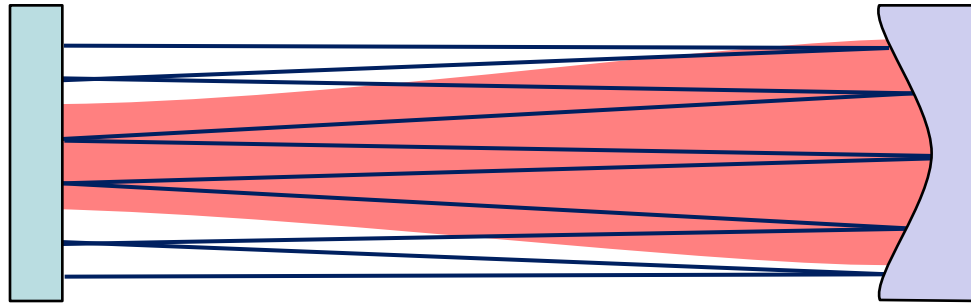
$$R(z) = z + \frac{z_R^2}{z}$$

$$z_R = \frac{\pi \cdot w_0^2}{\lambda}$$

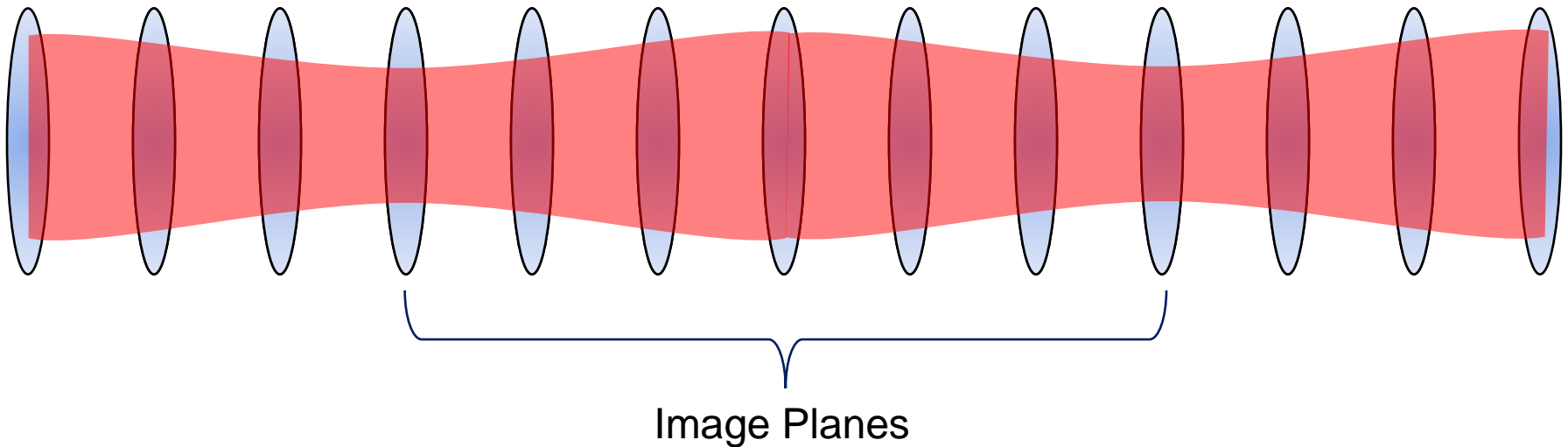


Number of Round-Trips to Image/Repeat

Plano-Concave Stable Resonator



Linearized Plano-Concave Stable Resonator



Number of Round-Trips to Image/Repeat

This problem can be addressed using ray matrices. Consider a resonator with a round-trip ray-matrix given by M . In N round-trips, the ray-matrix will be given by M^N . To reproduce any input ray, we need to determine the number of round trips to make the identity matrix, or $M^N=I$.

$$\begin{bmatrix} A & B \\ C & D \end{bmatrix}^N = M^N = I = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

This can be determined numerically, but can also be addressed using eigenvalue analysis. The approach on the right derives an equation for N assuming a plano-concave resonator with length L and the end mirror radius of curvature equal to $2f$.

$$M^N v_i = \lambda^N v_i$$

$$M^N = \lambda^N$$

$$M = \begin{bmatrix} 1 & L \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 \\ -1/f & 1 \end{bmatrix} \begin{bmatrix} 1 & L \\ 0 & 1 \end{bmatrix}$$

$$M = \begin{bmatrix} 1-L/f & 2L-L^2/f \\ -1/f & 1-L/f \end{bmatrix}$$

$$X = 1 - L/f$$

$$\lambda = X \pm \sqrt{1 - X^2} j$$

$$\lambda = e^{j\phi}$$

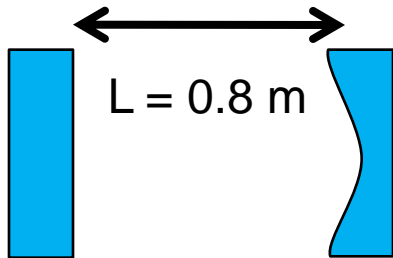
$$\phi = \tan^{-1} \left(\frac{\sqrt{1 - X^2}}{X} \right)$$

$$\lambda^N = e^{jN\phi}$$

$$N = \frac{2k\pi}{\phi} = \frac{2k\pi}{\tan^{-1} \left(\frac{\sqrt{1 - X^2}}{X} \right)}$$

Example Plano-Concave Resonator

Resonator Setup



$$R = 10 \text{ m}$$

$$f_{\text{eff}} = 5 \text{ m}$$

$$M = \begin{bmatrix} 1 - L/f & 2L - L^2/f \\ -1/f & 1 - L/f \end{bmatrix} = \begin{bmatrix} 0.84 & 1.472 \\ -0.2 & 0.84 \end{bmatrix}$$

$$X = 1 - L/f = 0.84$$

$$\phi = \tan^{-1}\left(\frac{0.5426}{0.84}\right) = 0.5735$$

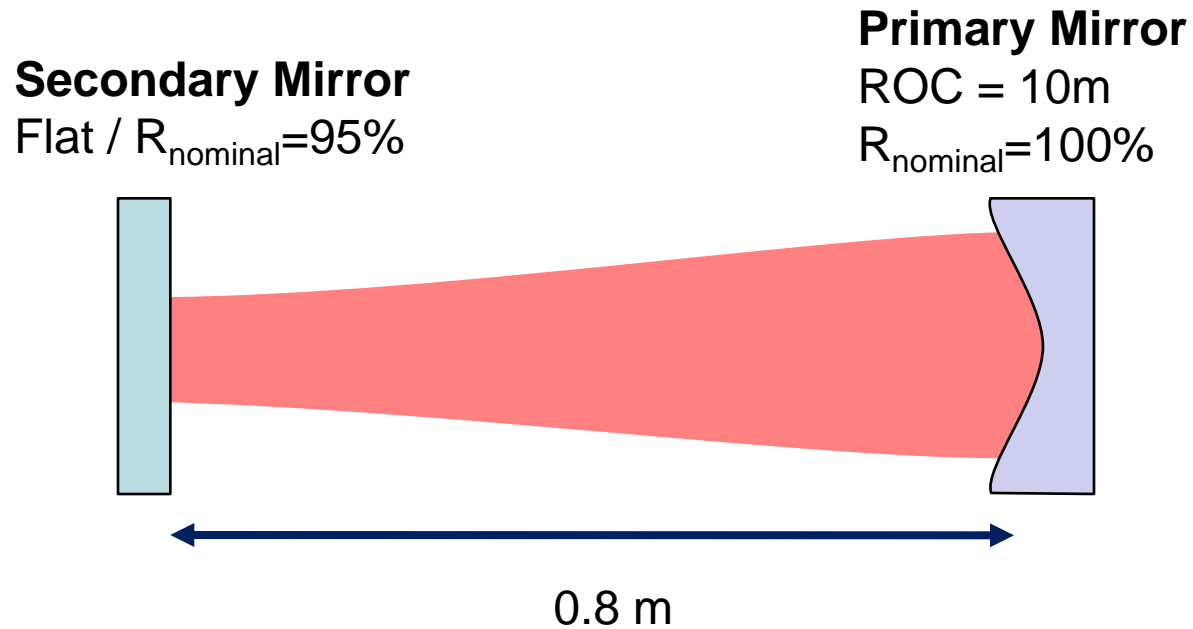
$$N = \frac{2\pi}{\phi} = \frac{2\pi}{.5735} \approx 11$$

$$M^{11} \approx \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} = I$$

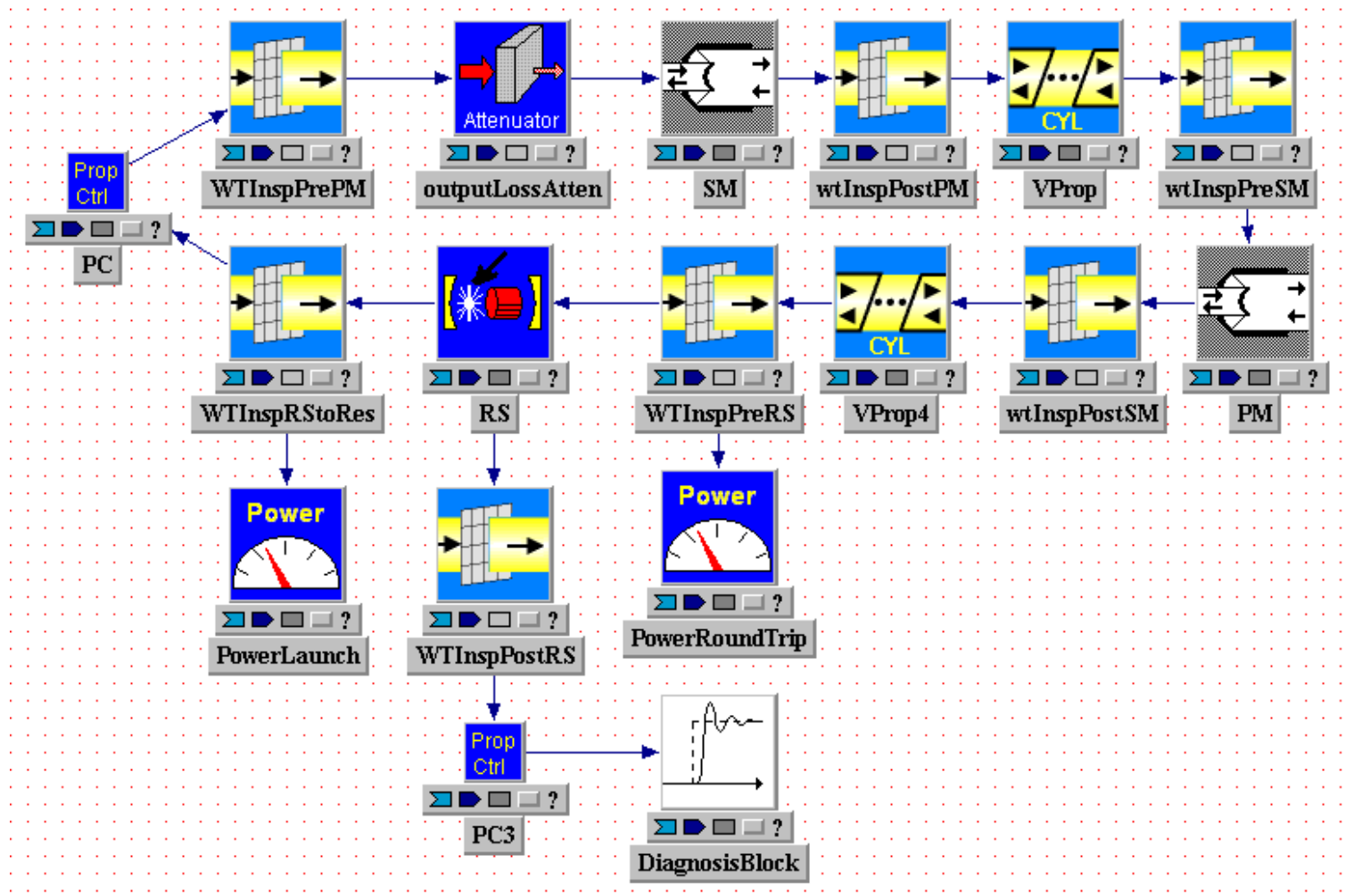
Impact of the Number of Round-Trips to Image

- This number is approximately the reduction factor of the required angular bandwidth predicted by the Coy/Praus/Mansell theory referenced earlier.
- This number is also the number of intensity profiles that need to be averaged to achieve a stable intensity for saturable gain calculations in a stable resonator (more on this later).

Example Laser Resonator Setup



Wave Train Model

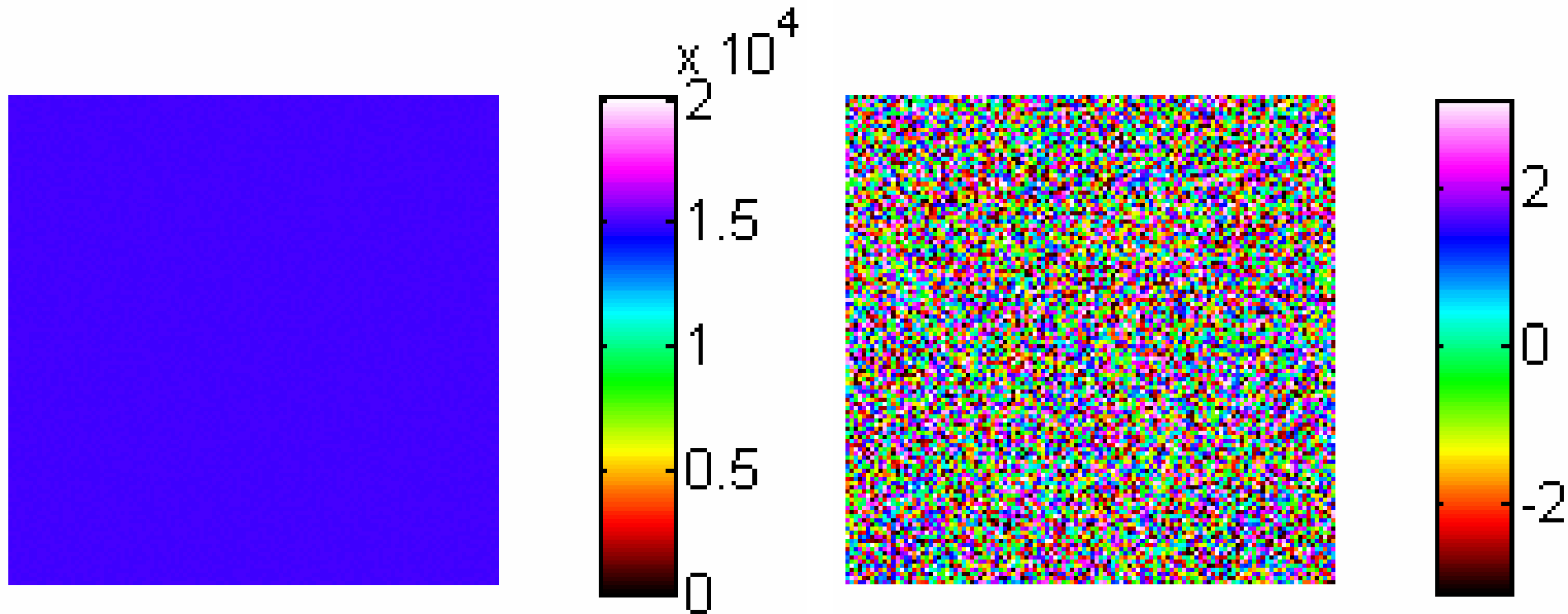


Parameters

- R_c (Radius of curvature of secondary mirror) = 10 m
- Cavity Length = 0.8 m
- Propagation grid = 256 by 56 μm (earlier 128 by 75 μm)
- Wavelength = 1 μm
- Reflectivity of output mirror = 95 %
- Initial Field = BwomikTopHat field of 6 cm initial Radius and 15000 amplitude
- Normalization = 1
- Iterations = 10000
- Varying Aperture diameter



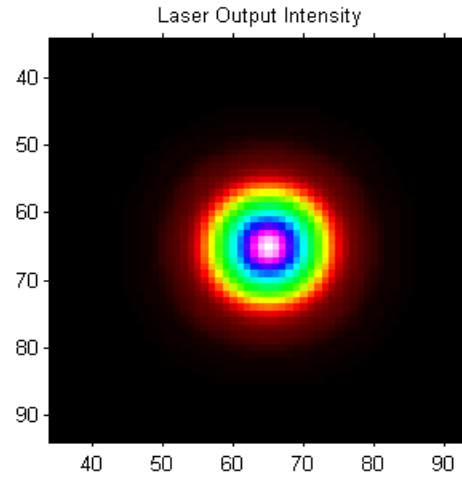
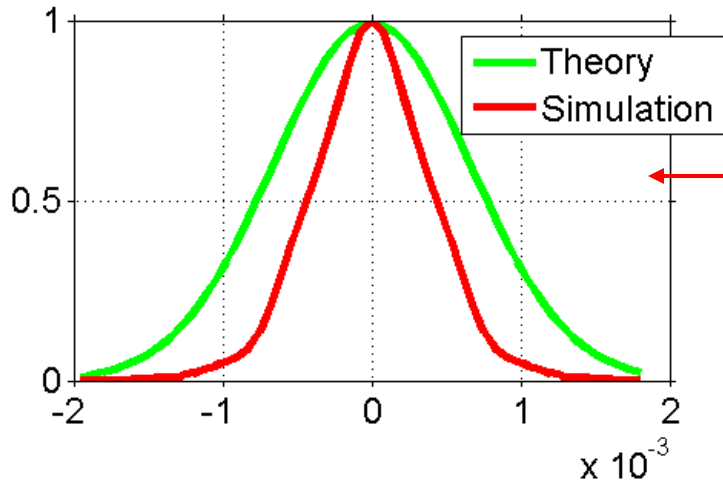
Seed all laser modes with a Bwomik field.



Bwomik Field is a plane wave with random phase that tends to seed all the modes of a resonator. This is implemented in “LaserGridInitializers.h”.

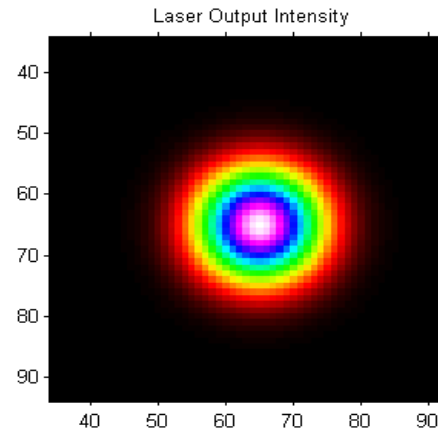
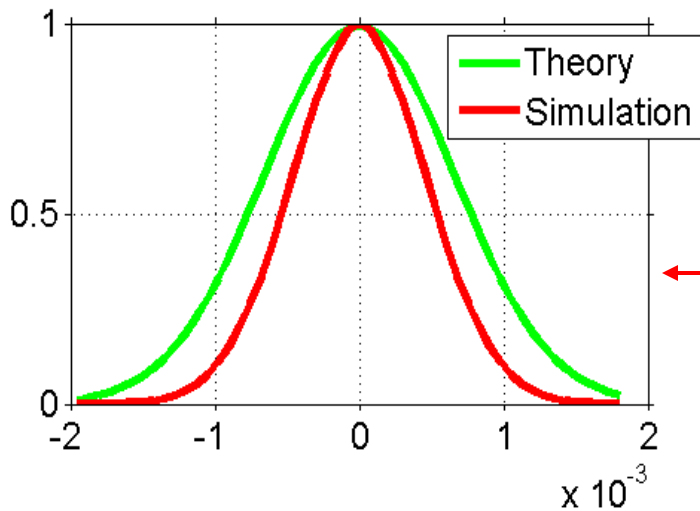
Converged Resonator Field Dependence on Internal Aperture Diameter

Larger aperture results approximate the theory more accurately.



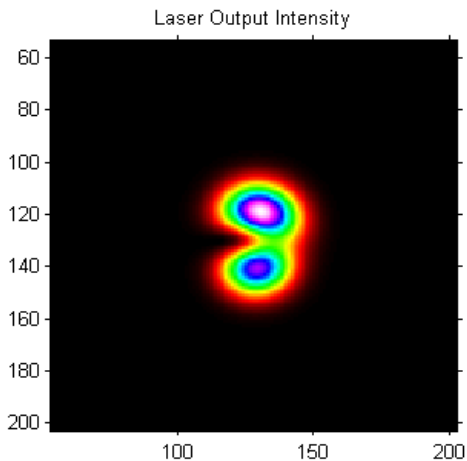
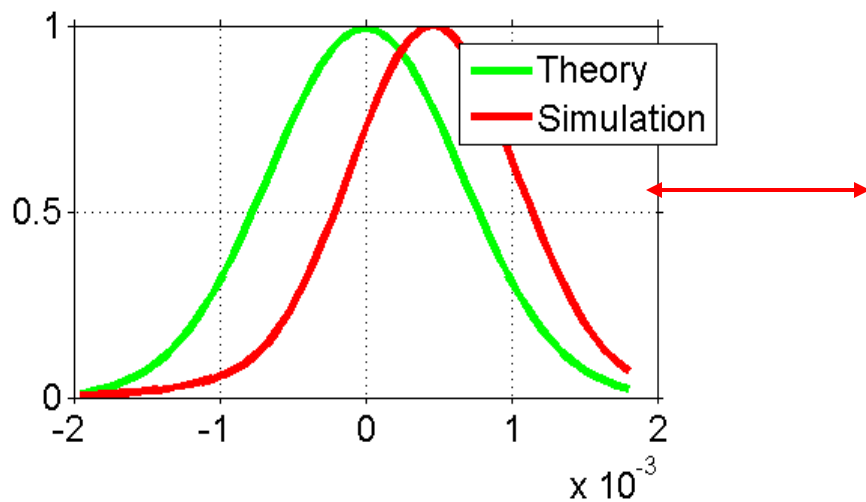
Iterations = 10000

Aperture diameter = 2.0 mm



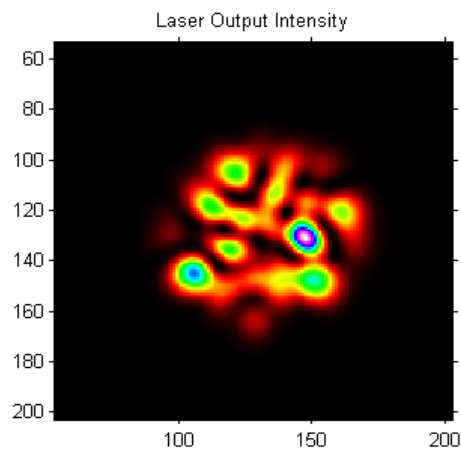
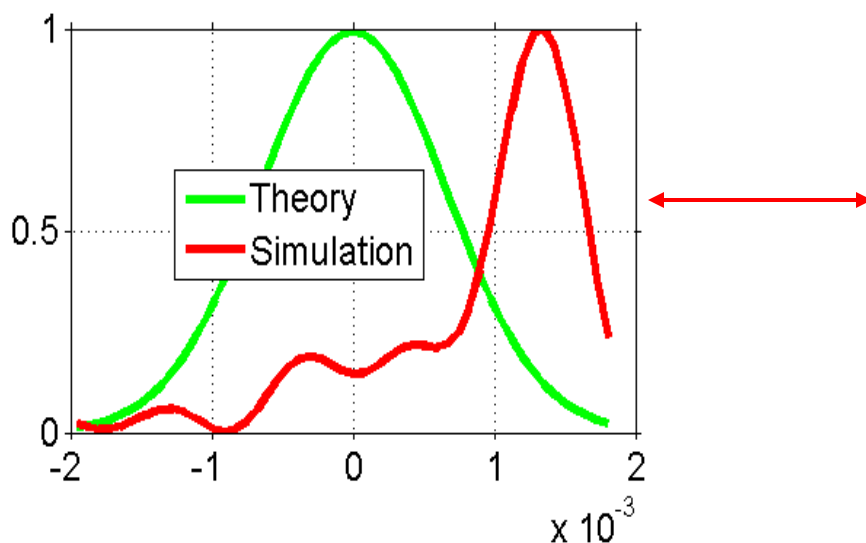
Aperture diameter = 4.0 mm

Bigger apertures require more iterations to converge.



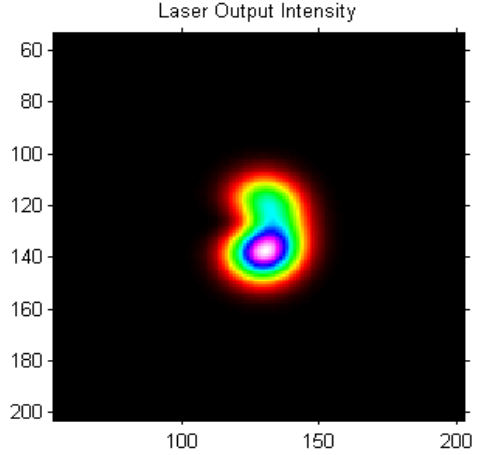
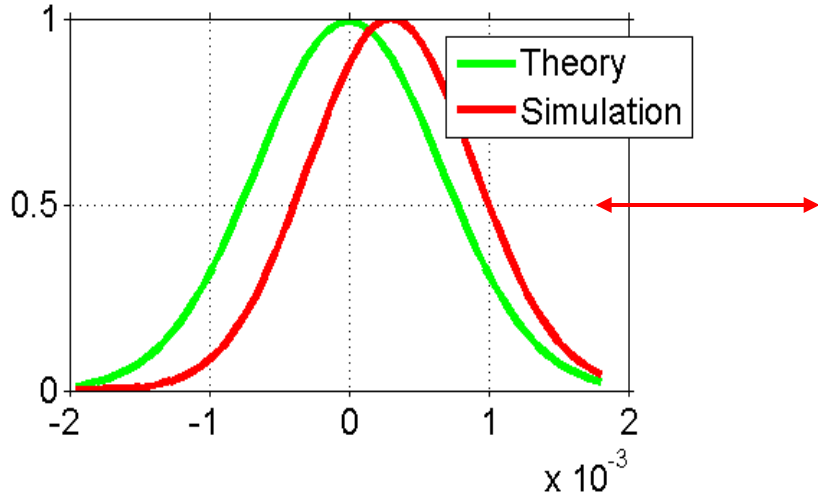
Iterations = 10000

Aperture diameter = 5.0 mm



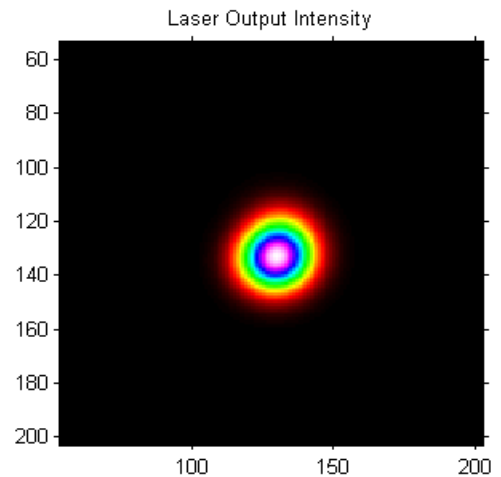
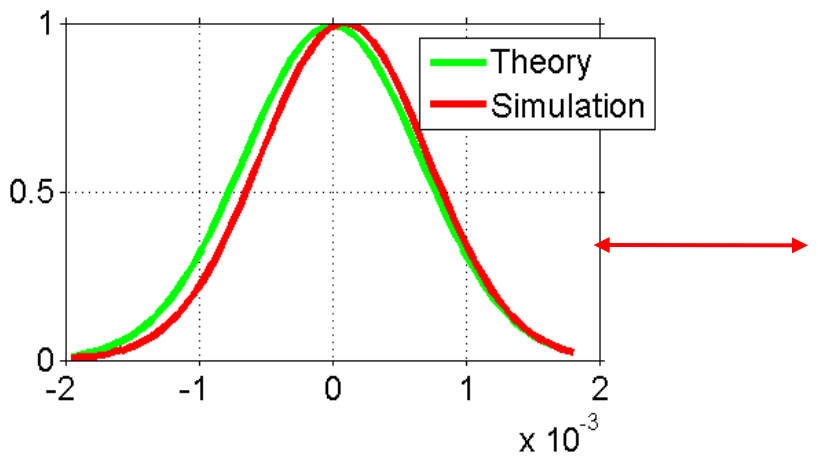
Aperture diameter = 7.0 mm

The 5-mm case begins to approach convergence after 50,000 iterations.



Iterations = 25000

Aperture diameter = 5.0 mm

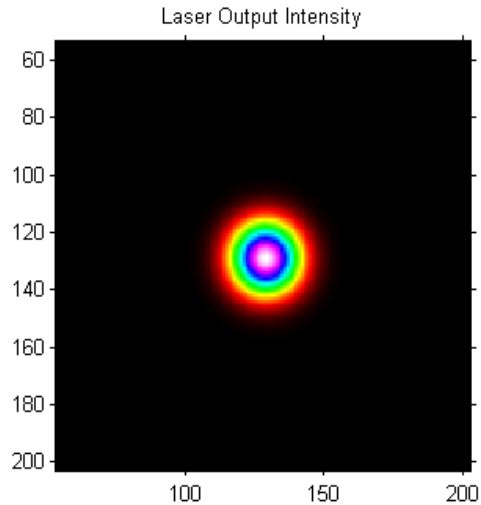
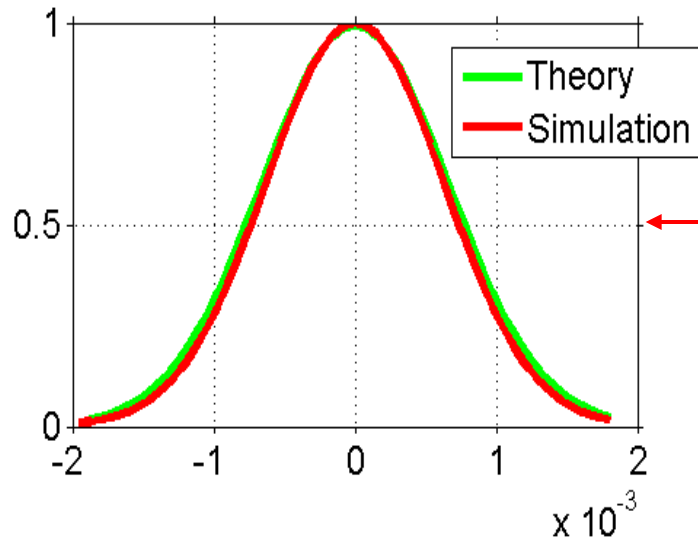


Iterations = 50000

Aperture diameter = 5.0 mm



The 5mm diameter aperture was reasonably well converged after 75,000 iterations.

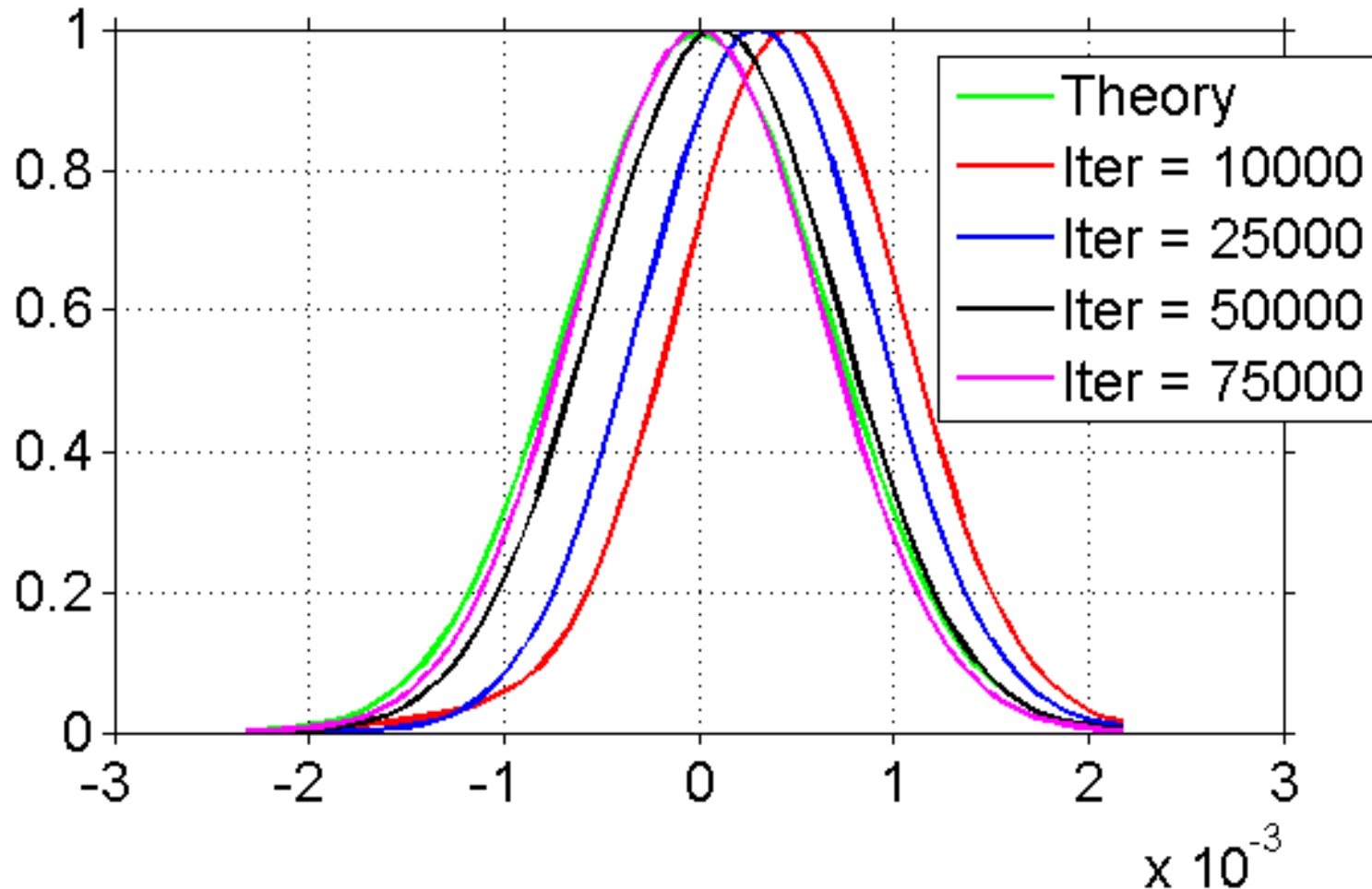


Iterations = 75000

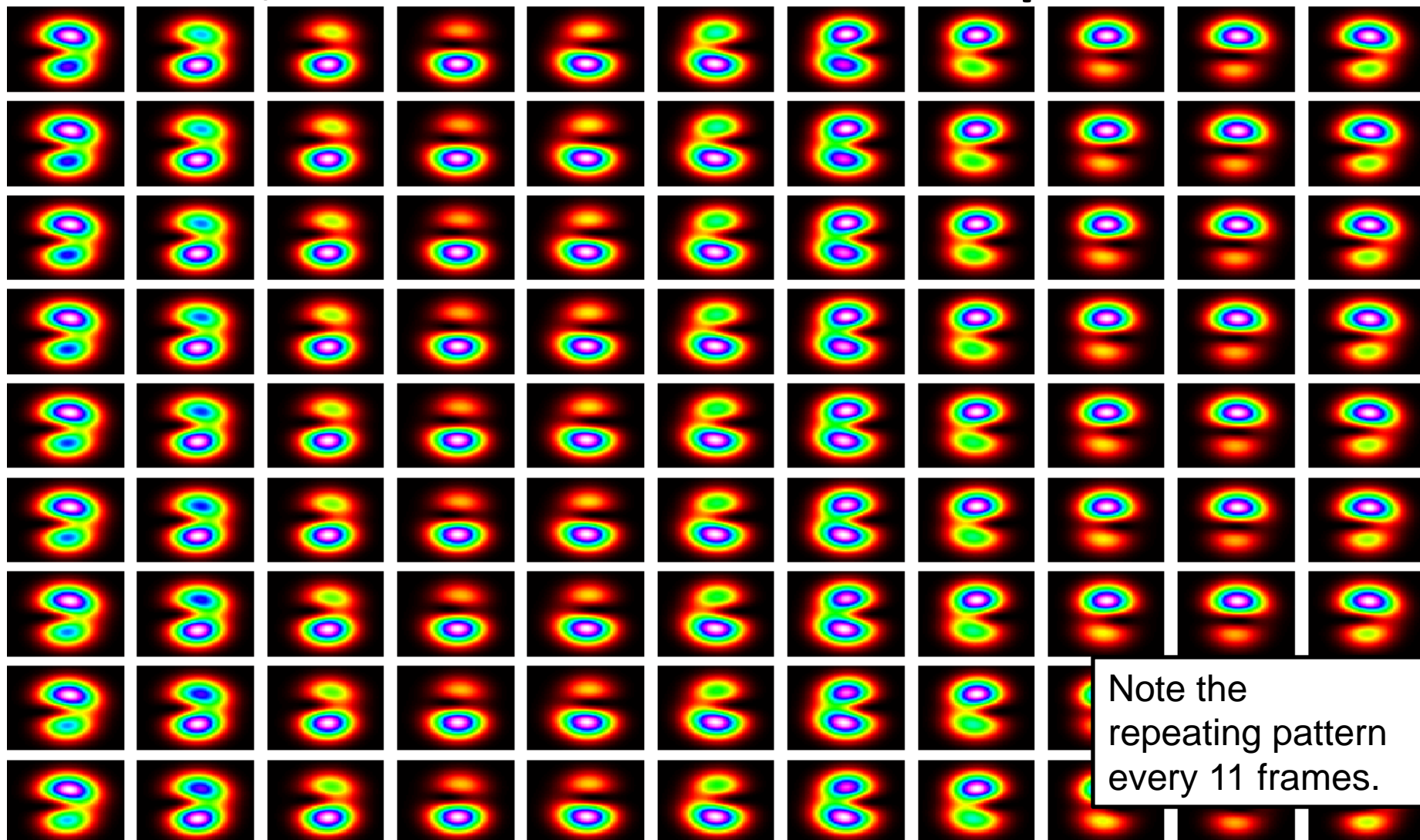
Aperture diameter = 5.0 mm



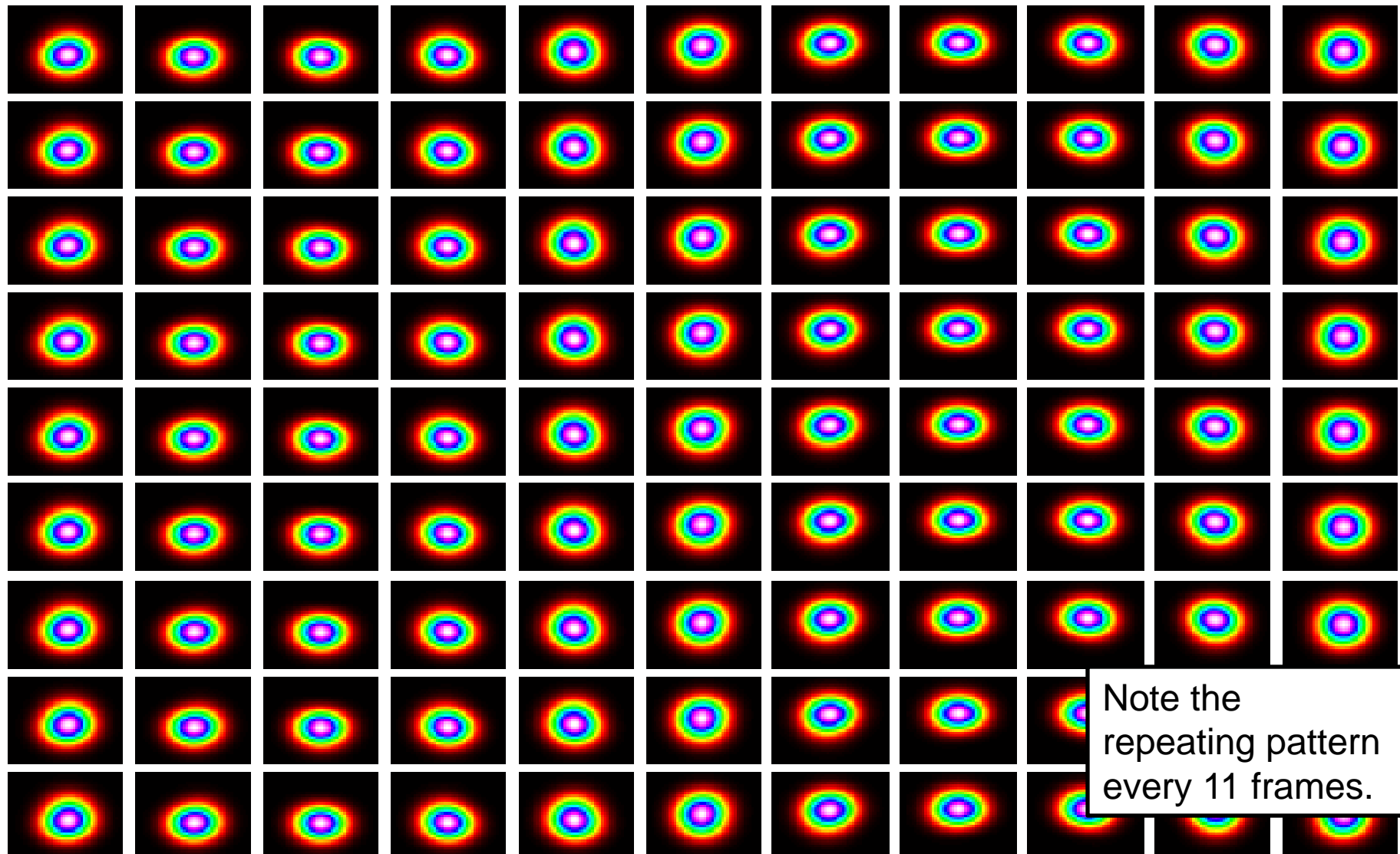
Intensity Cross-Section Comparison for 5-mm Aperture Cases with Different Iteration Numbers



Variation of Output Intensity with Last 99 Frames of 10,000 with 5-mm Diameter Aperture



Variation of Output Intensity with Last 99 Frames of 50,000 with 5-mm Diameter Aperture



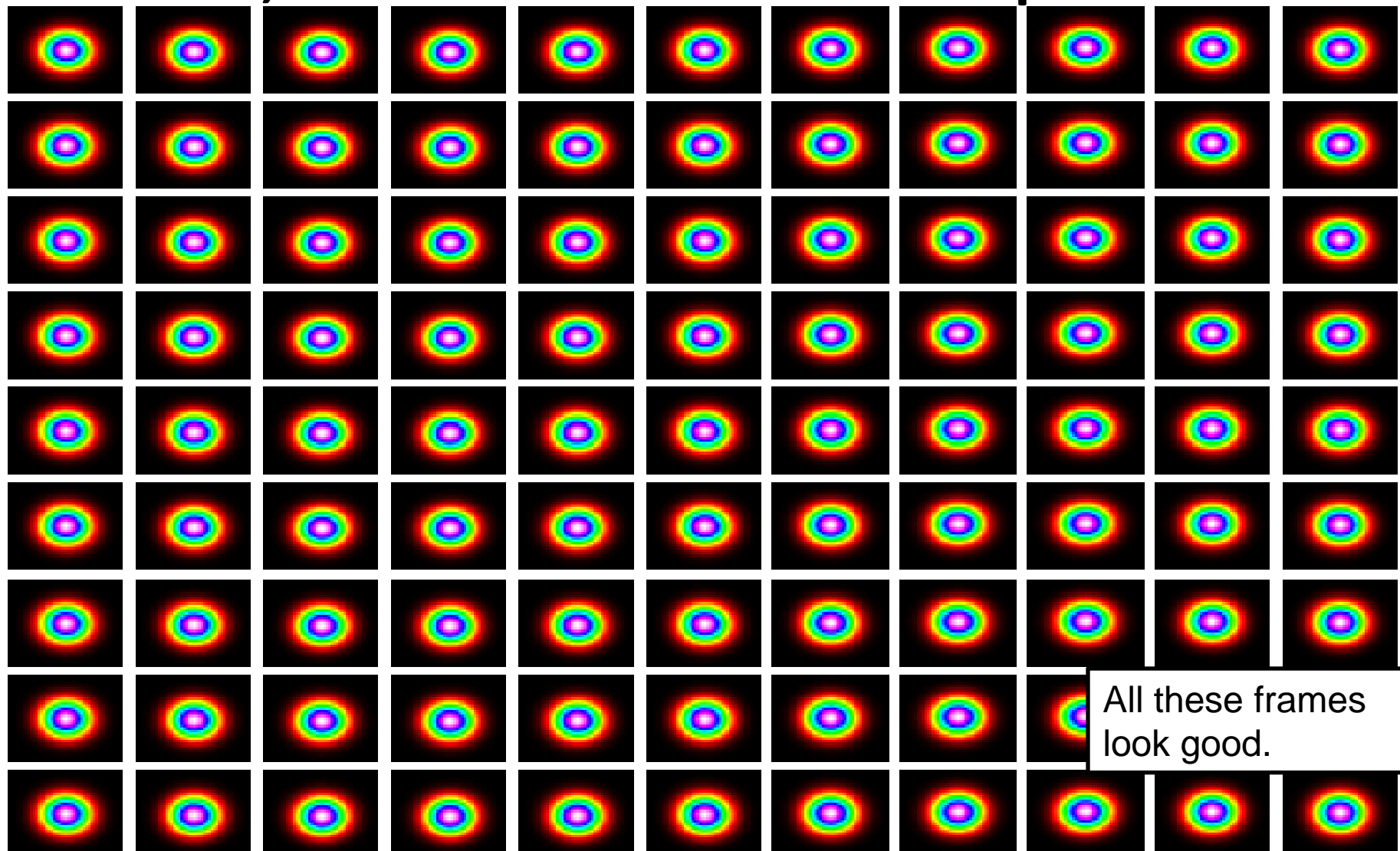
Note the repeating pattern every 11 frames.

62

62



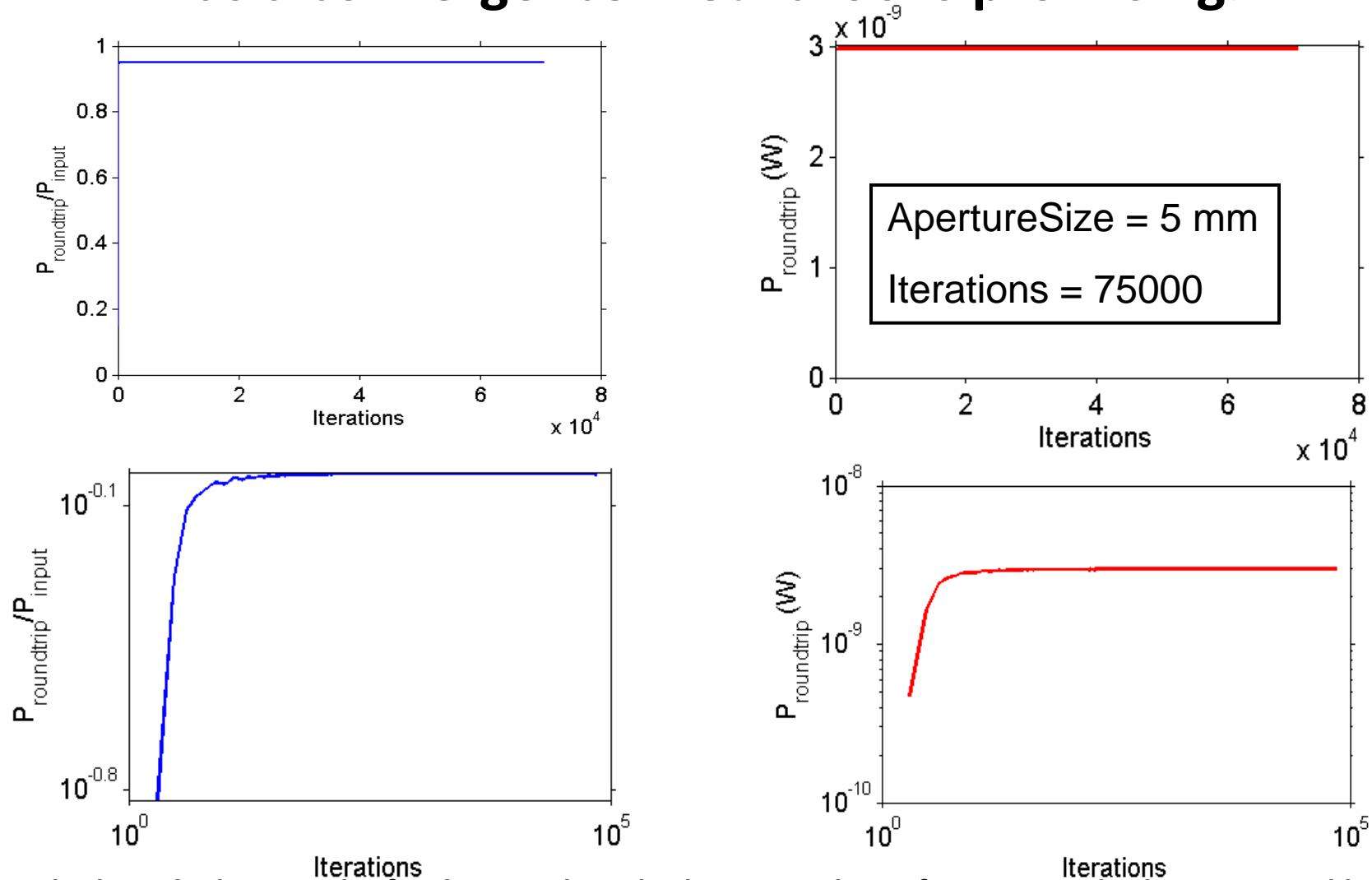
Variation of Output Intensity with Last 99 Frames of 75,000 with 5-mm Diameter Aperture



All these frames look good.



Evaluation of power stability or power reproducibility as a convergence metric looks promising.

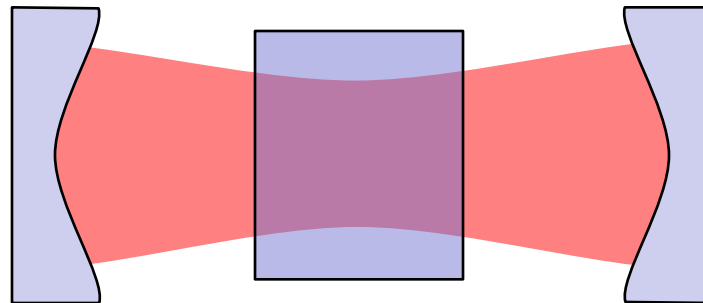


When the laser locks in to the fundamental mode there is no loss of power inside the cavity and hence the ratio of Laser output power to input power slowly increases with time and approaches 1

Stable Resonator Model Conclusions

- The WaveTrain stable resonator model showed that the models with larger aperture (~ 5 times w_0) converged very close to the theoretical shape in many (75,000) iterations.
- Even fairly early in the iterations, the beam intensity shape repeats itself every 11 iterations, as is predicted by theory.
- Power convergence appears to be a promising metric for the WT model convergence.

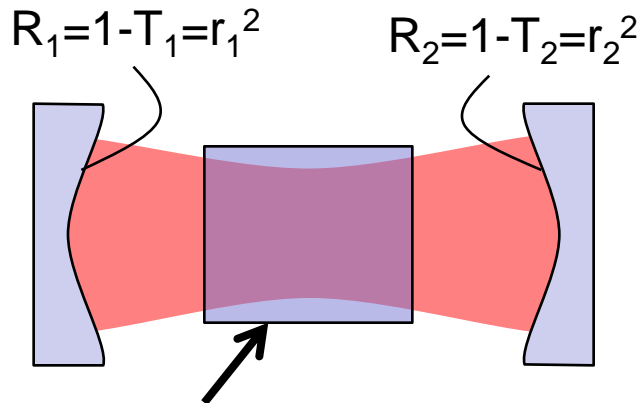
Stable Resonator With Gain



Stable Resonator with Gain

- Predictions from Theory
- WaveTrain Model Setup
- New Technique & Component
- Example Parameters
- Results & Comparison with Theory
- Conclusions

Rigrod Theory



$$G_0 = \exp(\alpha_{m0} L)$$

α_{m0} = small signal gain per length

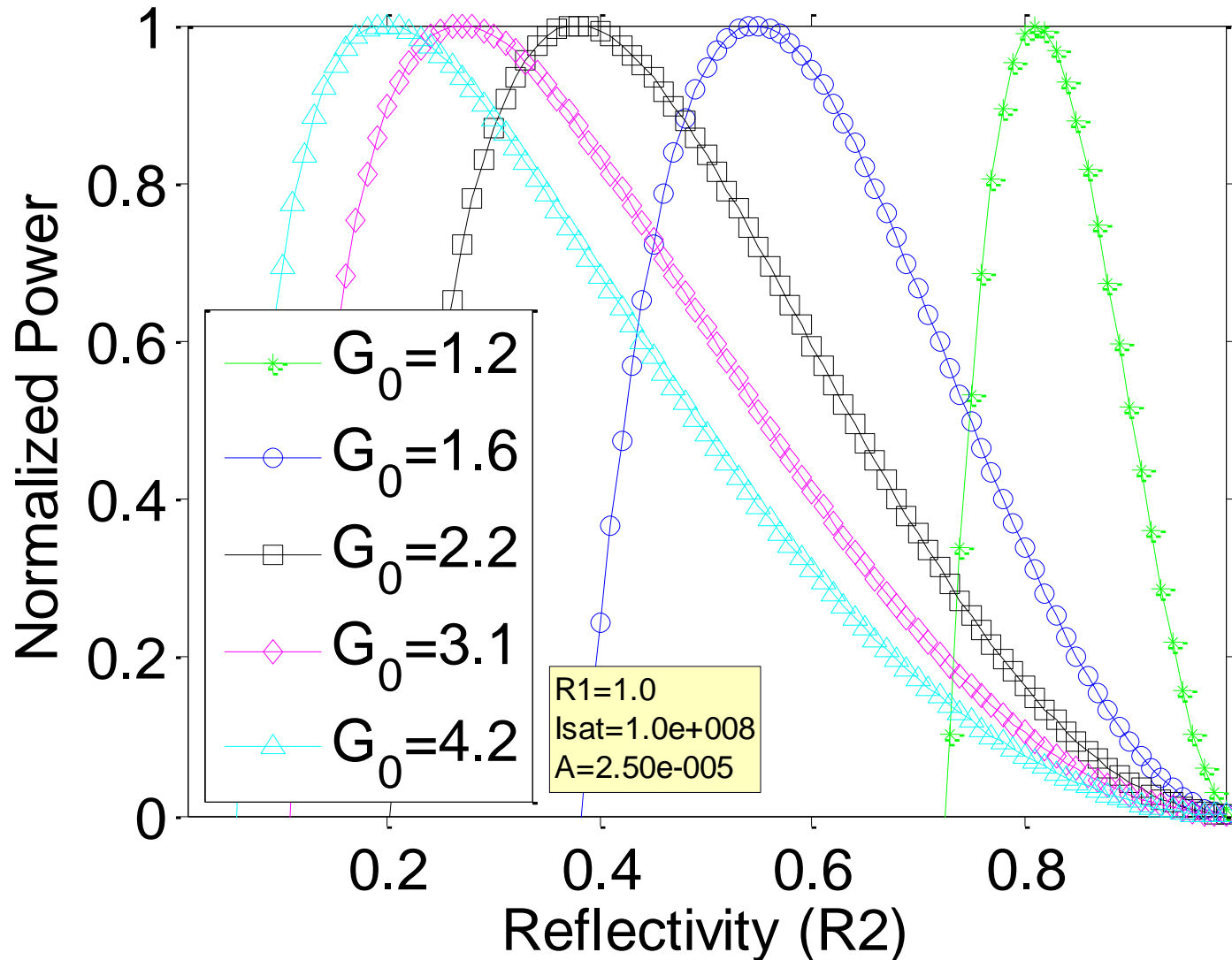
$$I_{out} = T_2 I_2 = \frac{T_2 I_{sat}}{\left[\left(+ r_2 / r_1 \right) \left(- r_1 r_2 \right) \right]} \left[\ln G_0 \right] \ln \left(\frac{1}{r_1 r_2} \right)$$

$$I_{available} = \ln G_0 I_{sat}$$

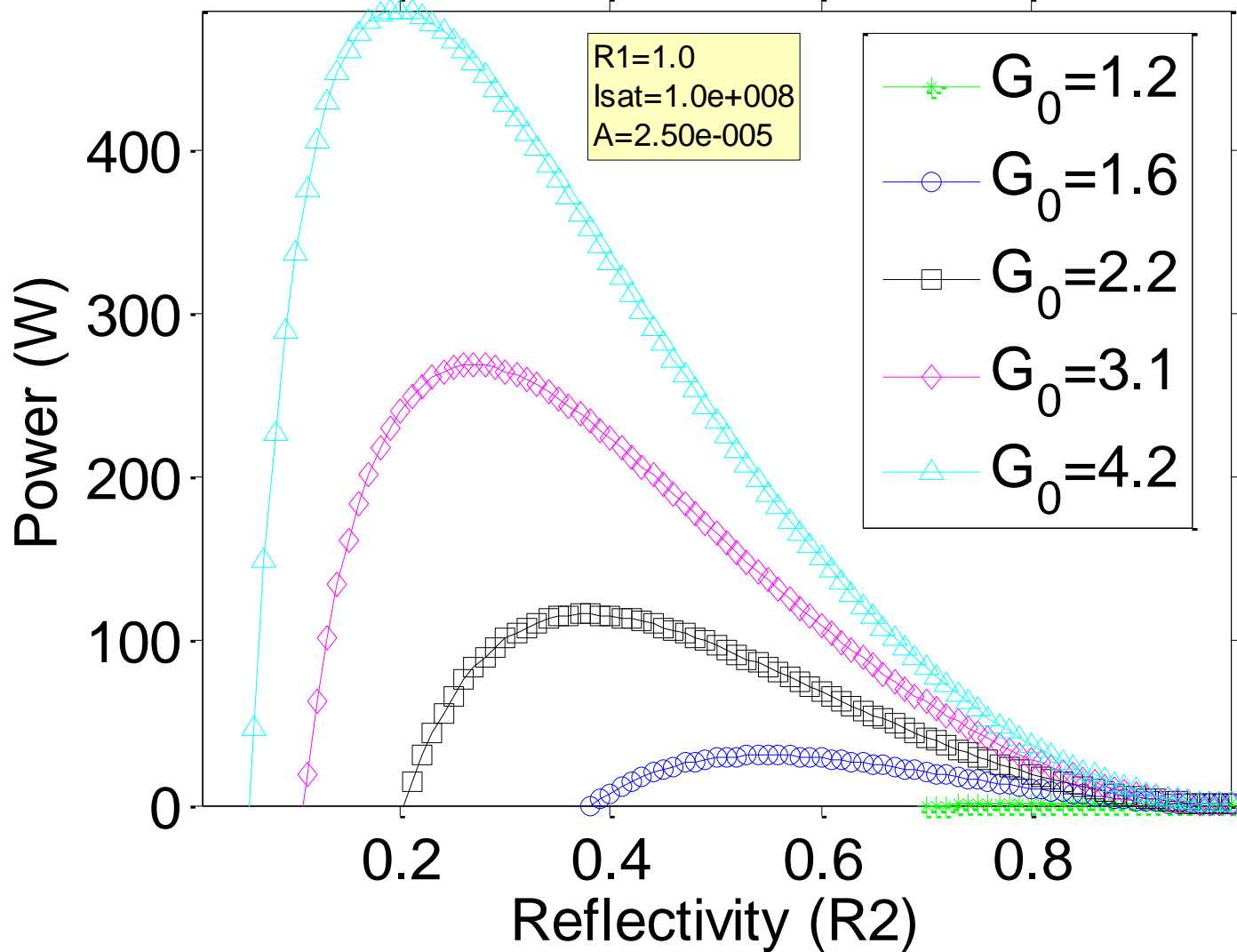
$$\eta \equiv \frac{I_{out}}{I_{available}} = \frac{T_2}{\left[\left(+ r_2 / r_1 \right) \left(- r_1 r_2 \right) \right]} \left[1 + \frac{\ln r_2}{\ln G_0} \right]$$

R is power reflectivity, r is field reflectivity

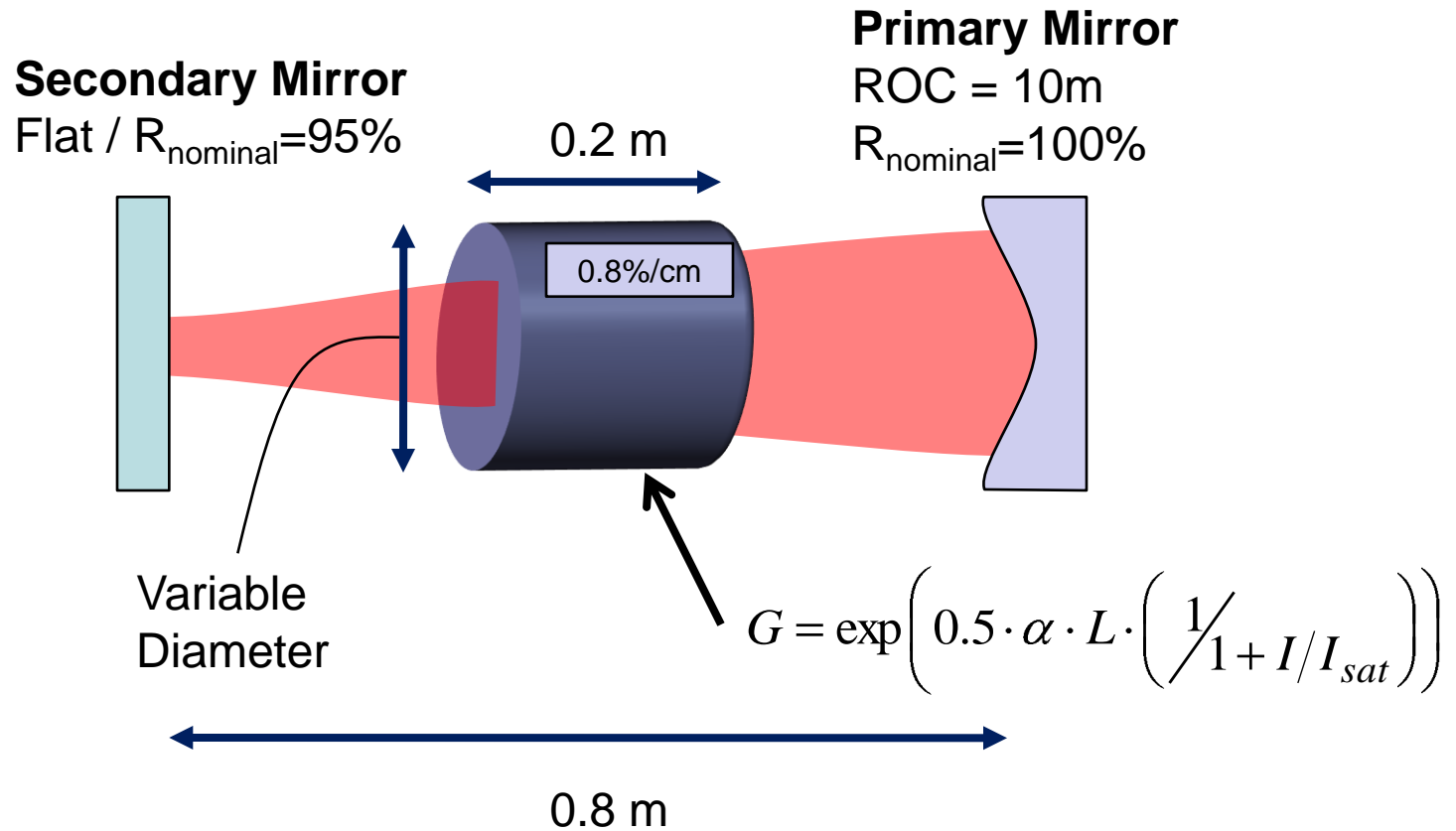
Typical Rigrod Results



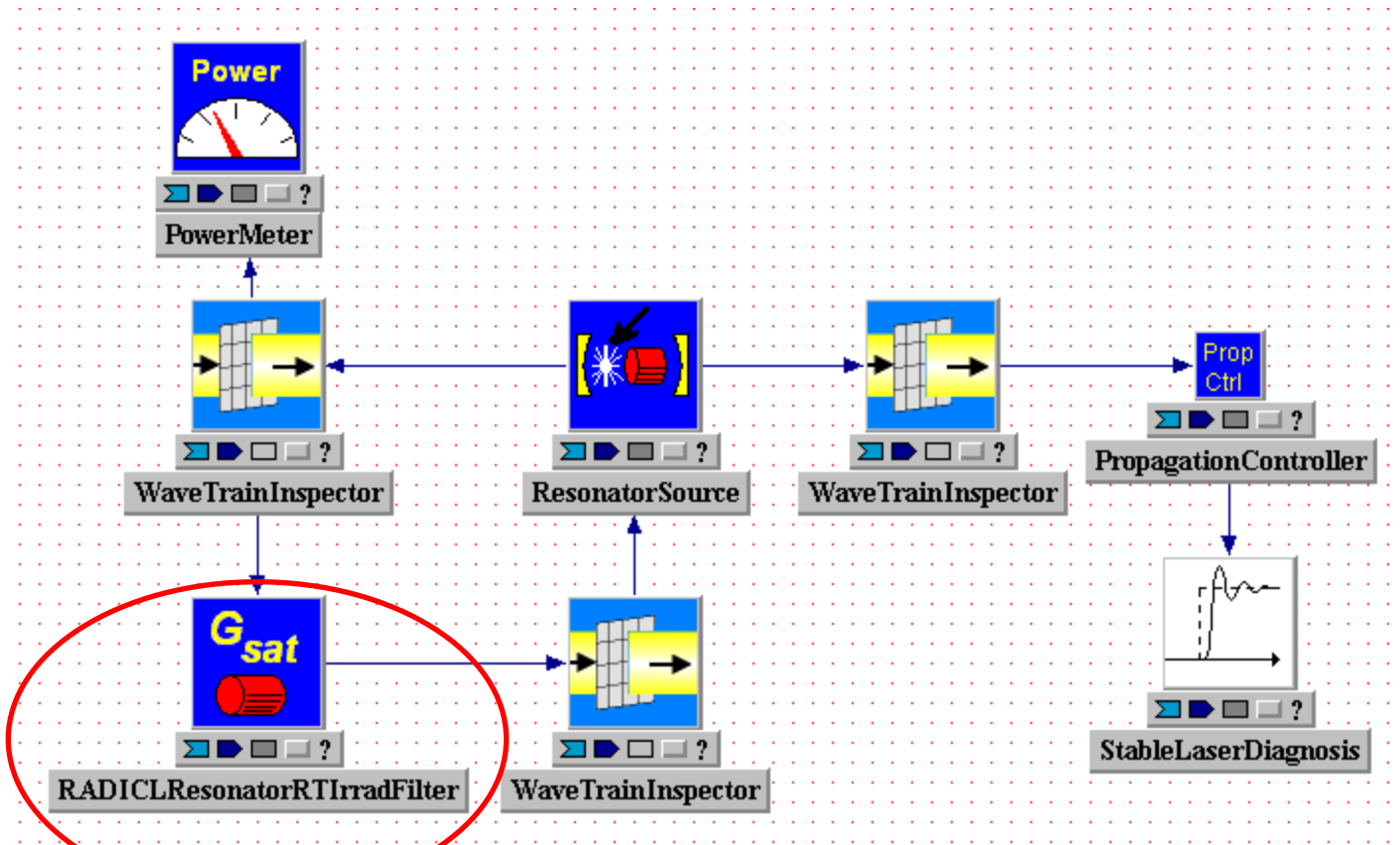
Typical Rigrod Results



Example Laser Resonator Setup

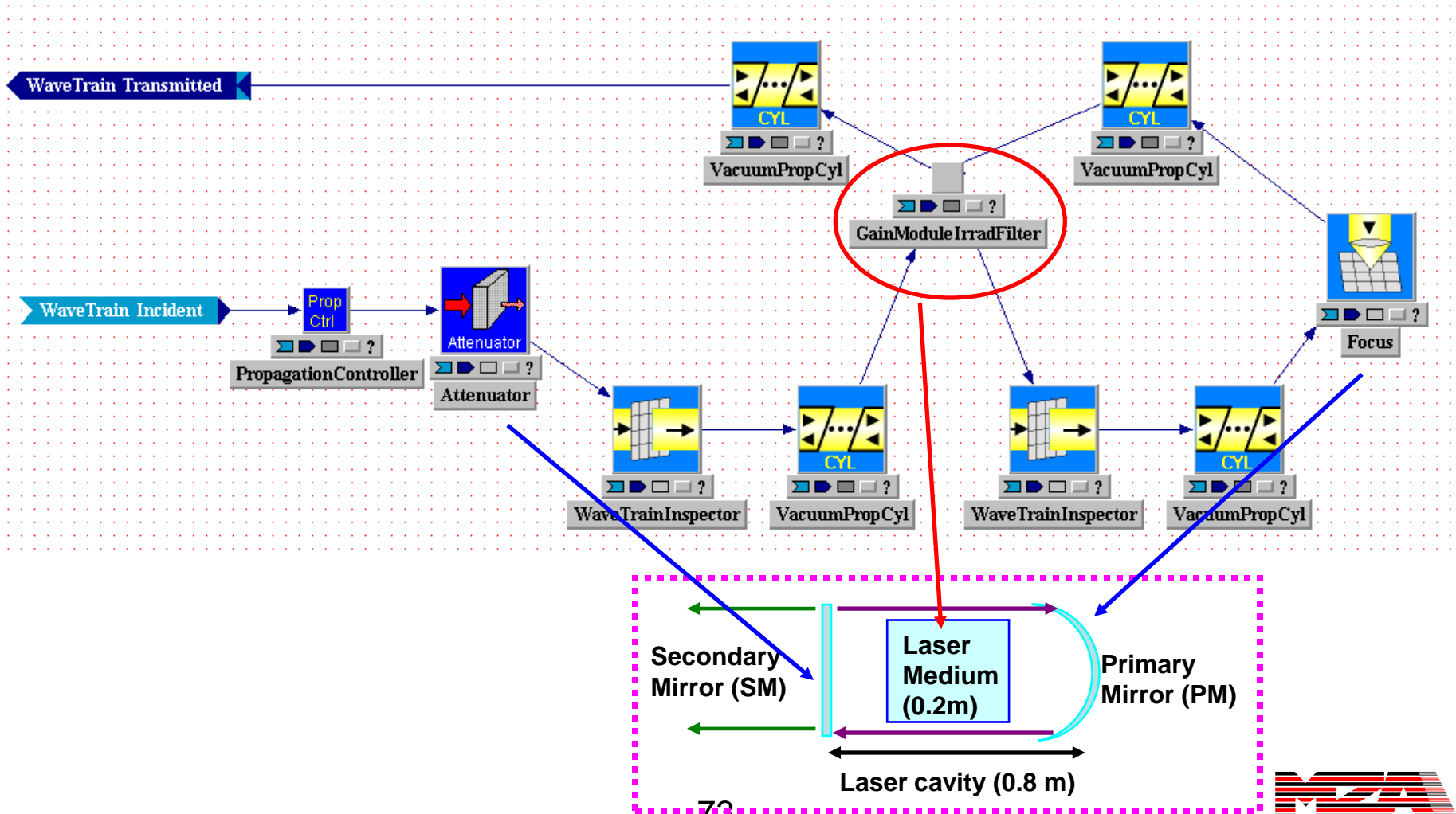


Wave Train Model

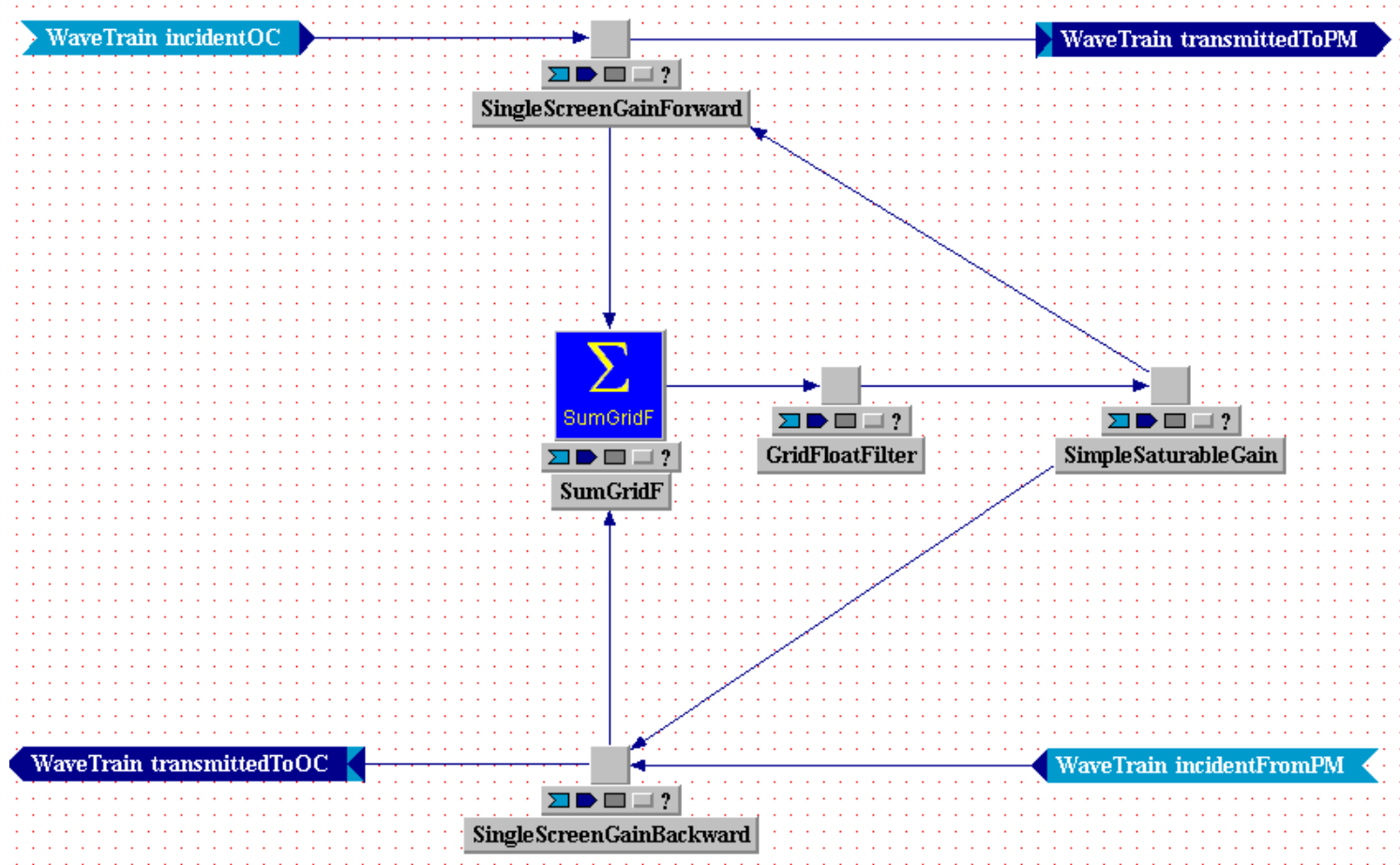


Next Slide...

Wave Train Model Of Laser Cavity



WT Model of Gain Medium



Description of the GridFloatFilter

- We developed the GridFloatFilter to average a user-specified number of intensity frames together to get a more stable intensity profile.
- We found that the best results are achieved when the number of iterations over which to average is equal to the number of round-trips to image (see earlier derivation).
 - The original logic here was that the Fox & Li technique is modeling a single slice of a continuum of fields and by averaging we can take this into account.

Parameters

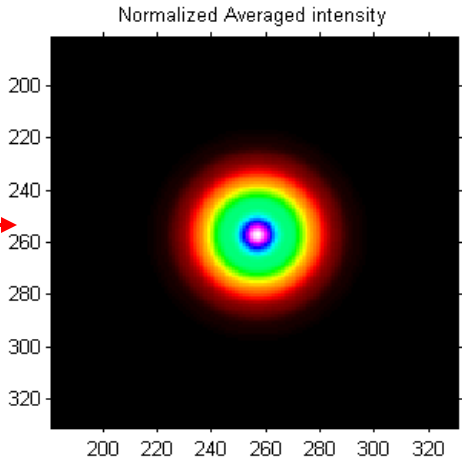
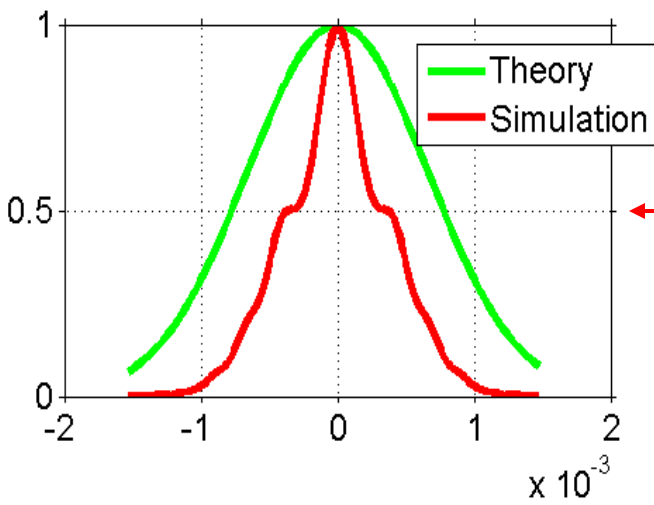
- NumAvgVec = 11
- Reflectivity = 0.7 – 0.9
- Iterations = 1000
- Rc (Radius of curvature of convex mirror) = 10 m
- cavityLength0 = 0.8 m
- Propagation Grid = 512 by 30e-6
- Ssgain = 0.8
- Amp0(Amplitude of initial field) = 15000
- Radius of initial field = 6.0e-2 m
- Seed = 12345
- Wavelength = 1e-6
- Saturation intensity = 1e7 W/m²
- Focus = Rc/2
- Normalization = 0
- convergenceThreshold = 1e-9
- GainLength = 0.2
- Aperture diameter = 3mm



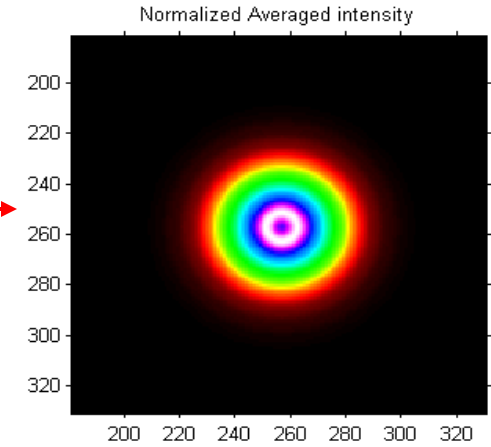
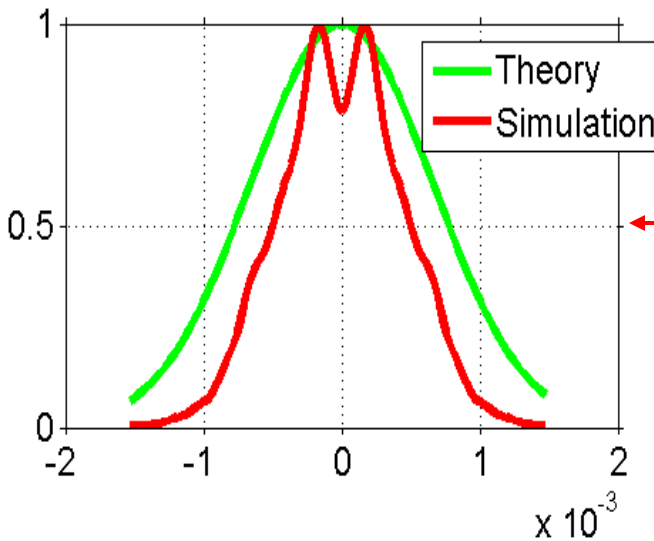
Model Results for No Intensity Averaging



Intensity patterns for last frame and intensity plot along the central axis of Averaged intensity show the evolution of various modes with increase of aperture diameter



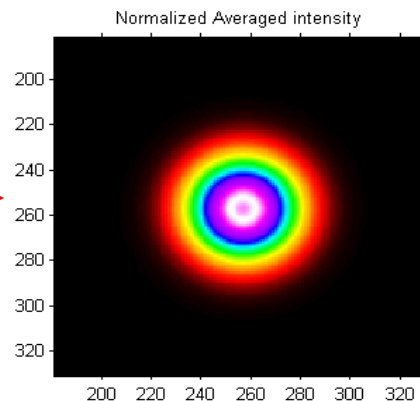
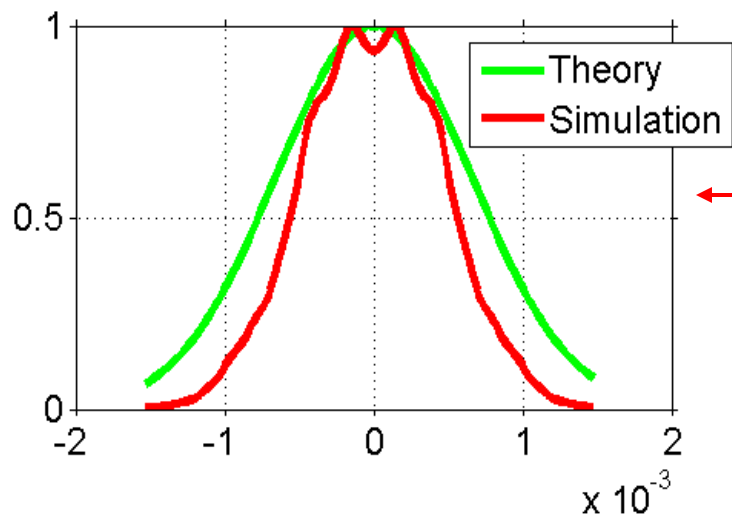
Aperture diameter = 2.0 mm



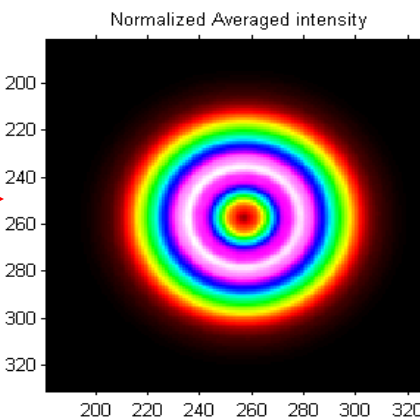
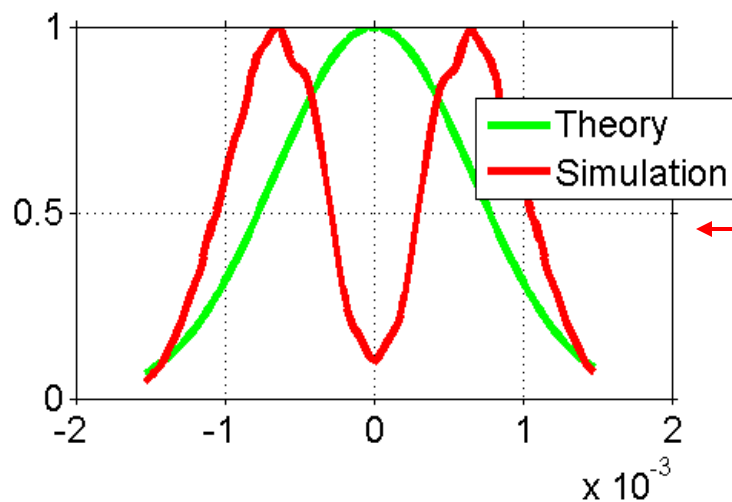
Aperture diameter = 2.5 mm



Intensity patterns for last frame and intensity plot along the central axis of Averaged intensity show the evolution of various modes with increase of aperture diameter

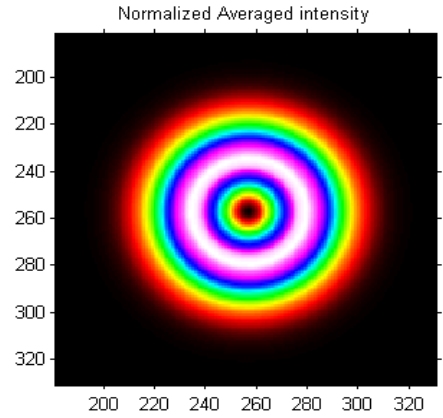
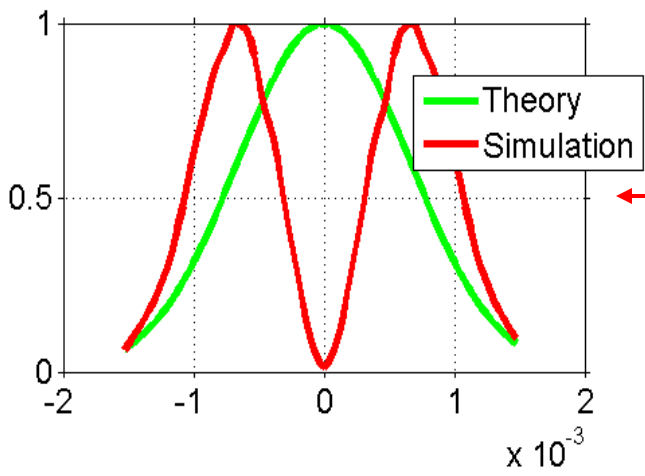


Aperture diameter =
3.0 mm

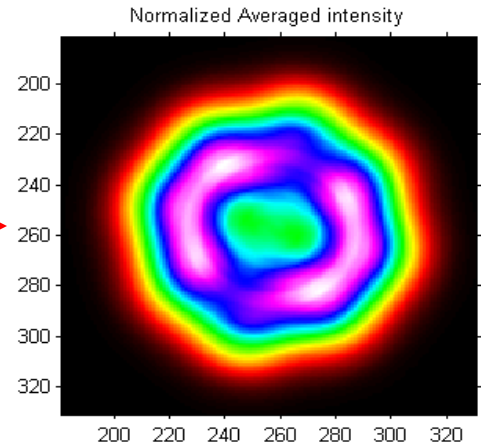
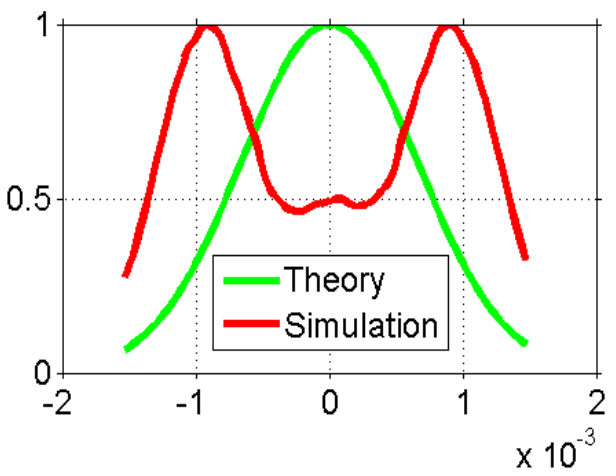


Aperture diameter =
3.5 mm

Intensity patterns for last frame and intensity plot along the central axis of Averaged intensity show the evolution of various modes with increase of aperture diameter



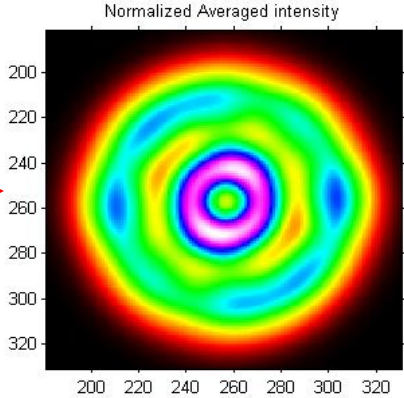
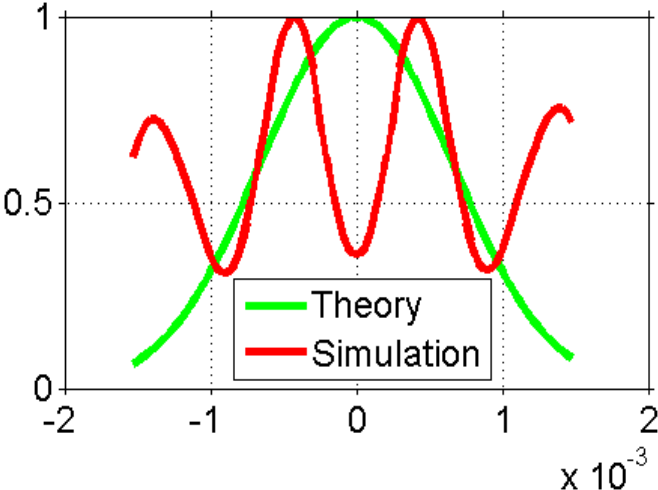
Aperture diameter = 4.0 mm



Aperture diameter = 4.5 mm



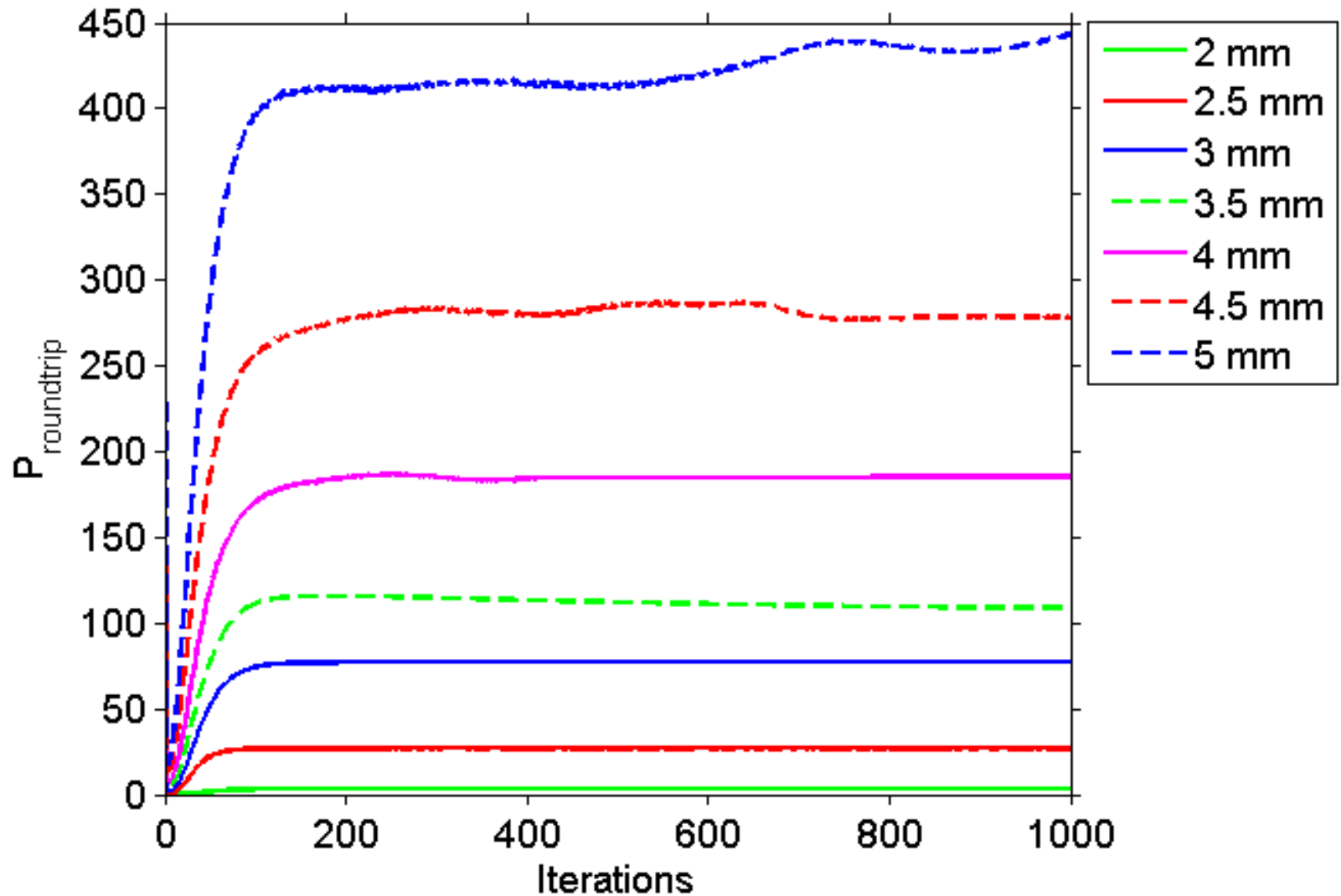
Intensity patterns for last frame and intensity plot along the central axis of Averaged intensity show the evolution of various modes with increase of aperture diameter



Aperture diameter = 5.0 mm



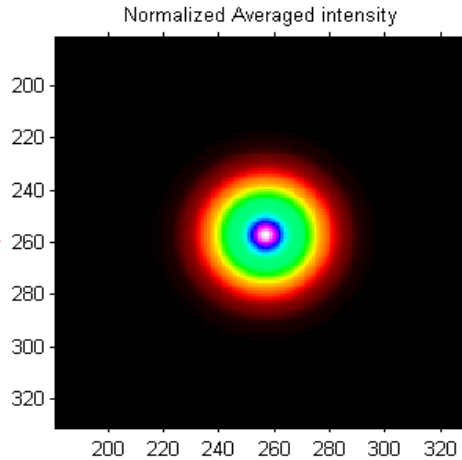
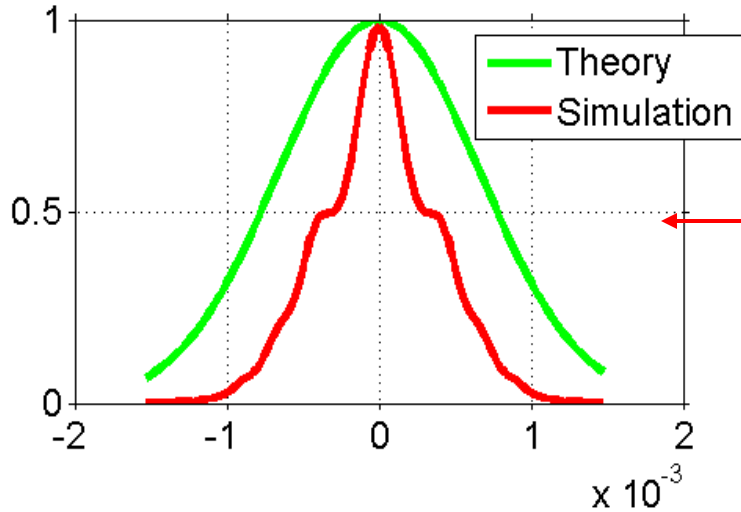
Output Power



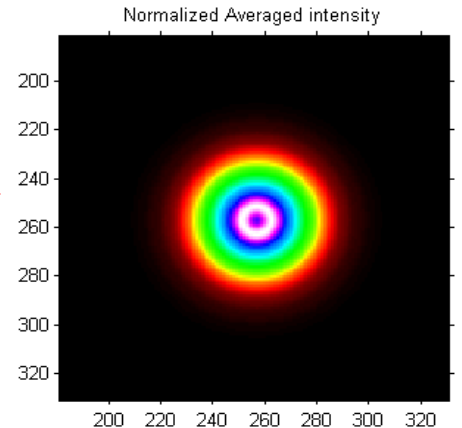
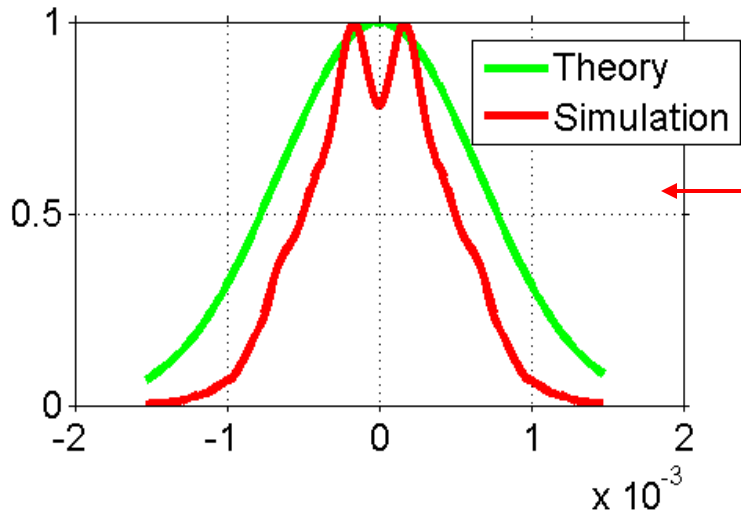
Model Results for 11-Frame Intensity Averaging

1000 Iterations

Small Aperture Results



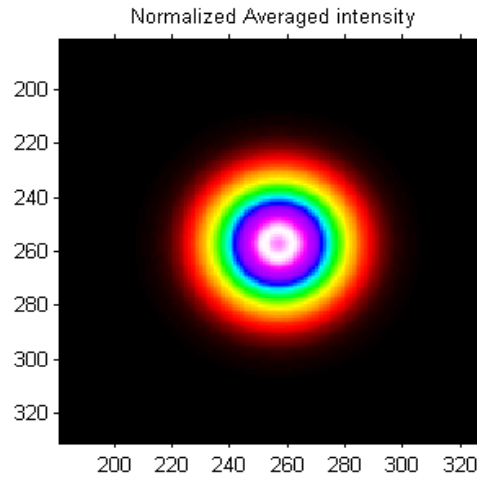
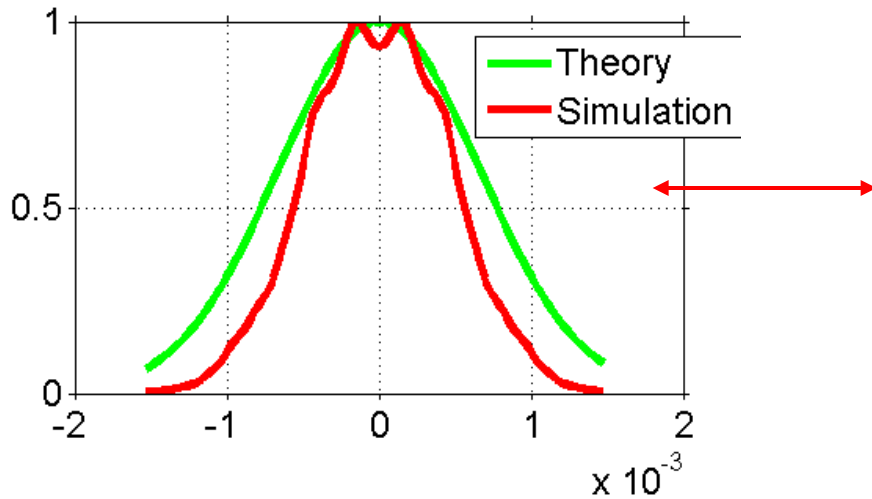
Aperture diameter = 2.0 mm



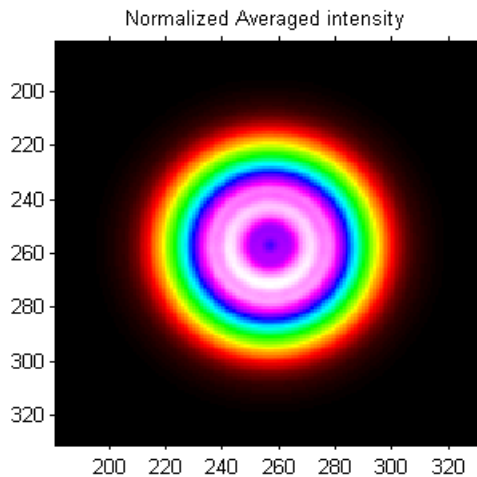
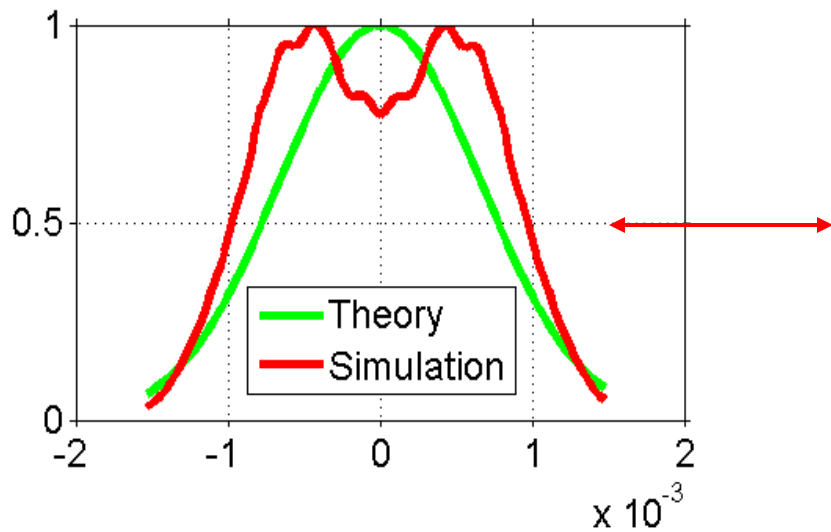
Aperture diameter = 2.5 mm



Medium Aperture Results

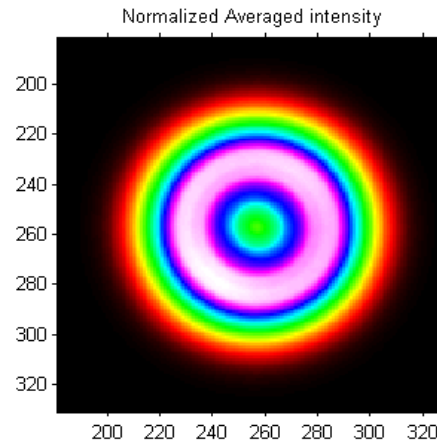
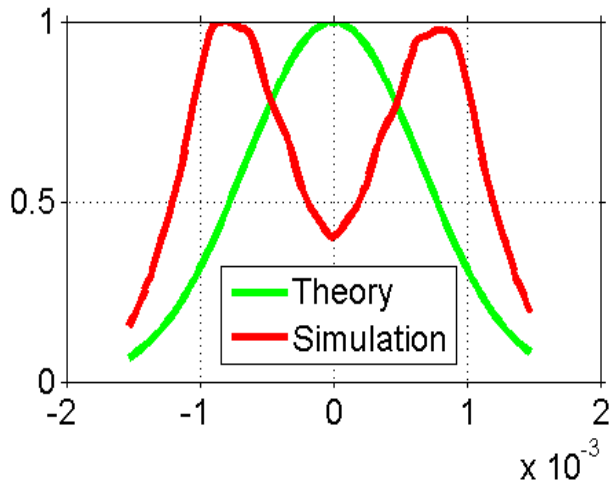


Aperture diameter =
3.0 mm

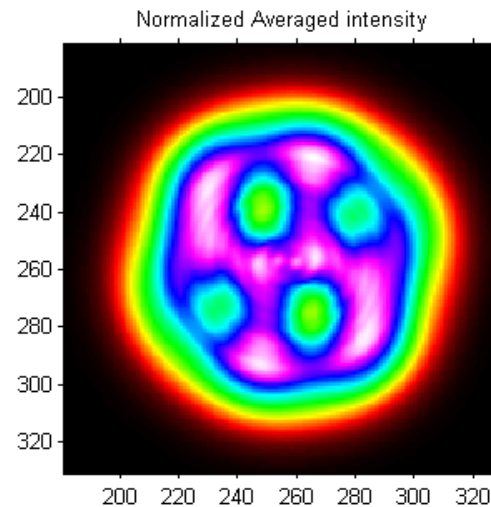
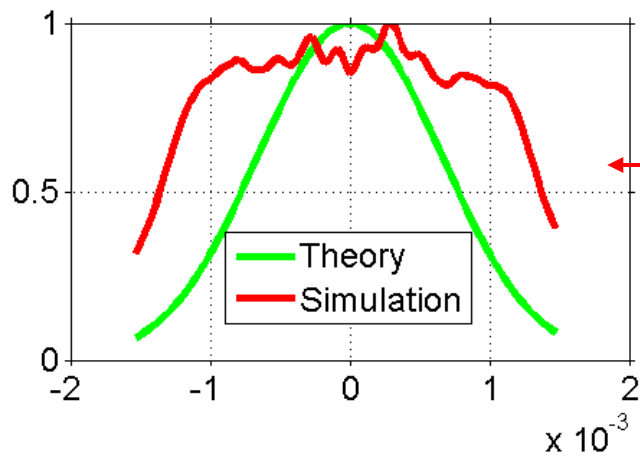


Aperture diameter =
3.5 mm

Larger Aperture Results

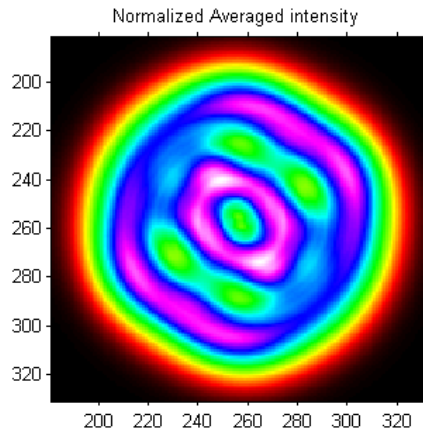
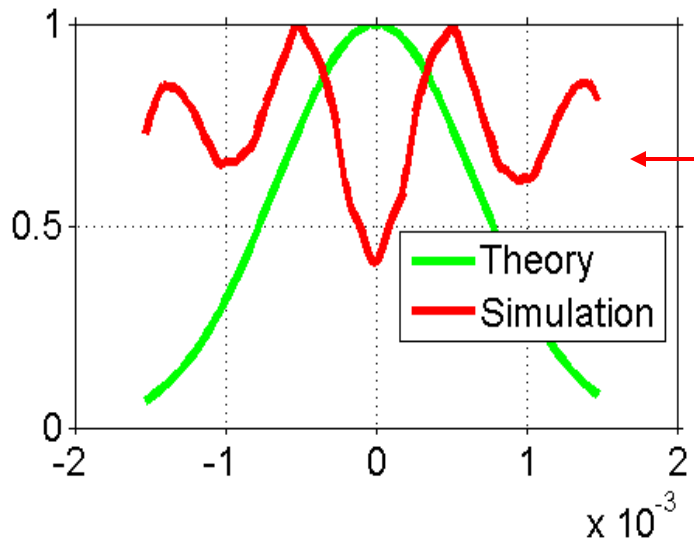


Aperture diameter =
4.0 mm



Aperture diameter =
4.5 mm

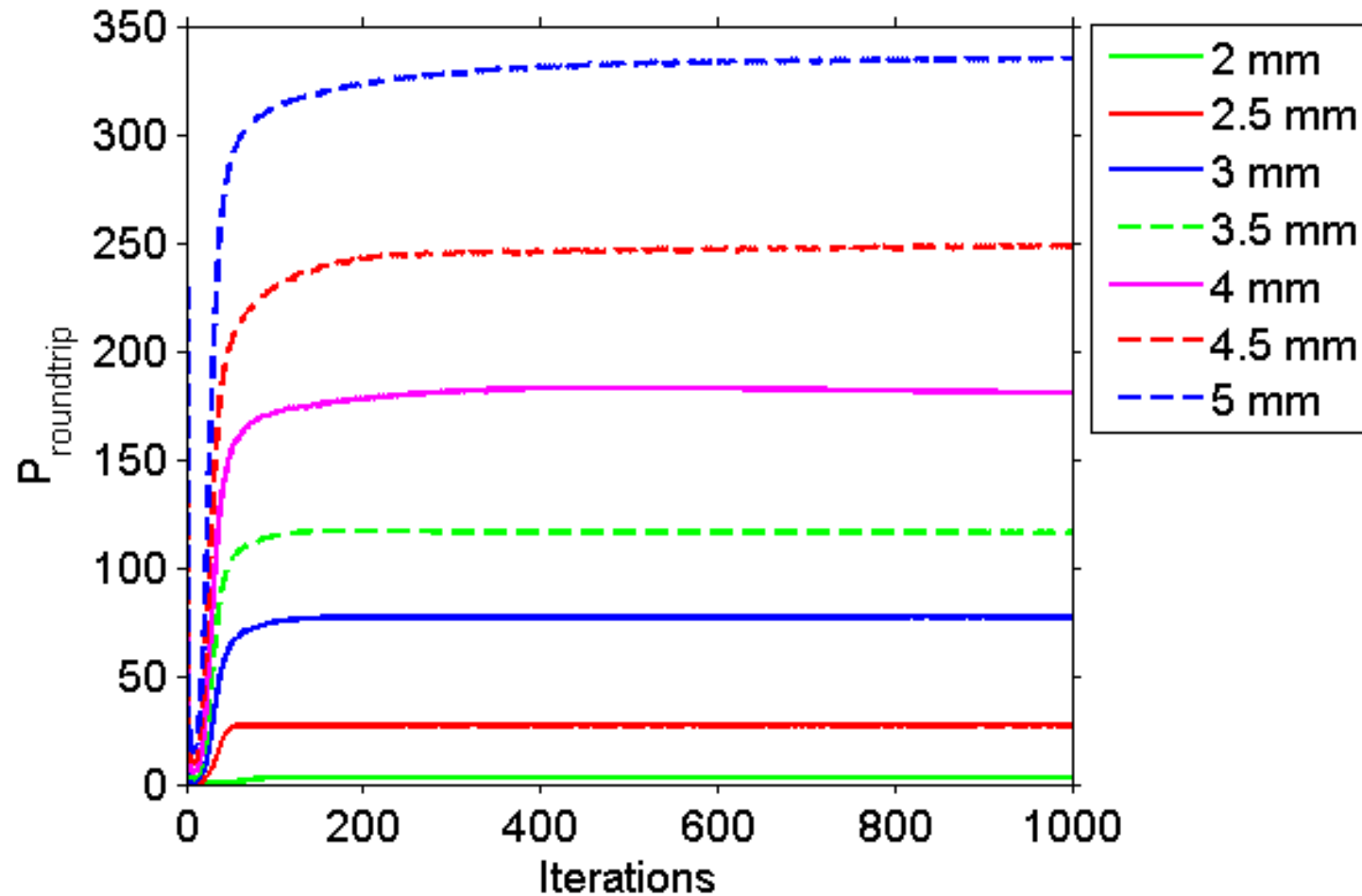
Largest Aperture Results



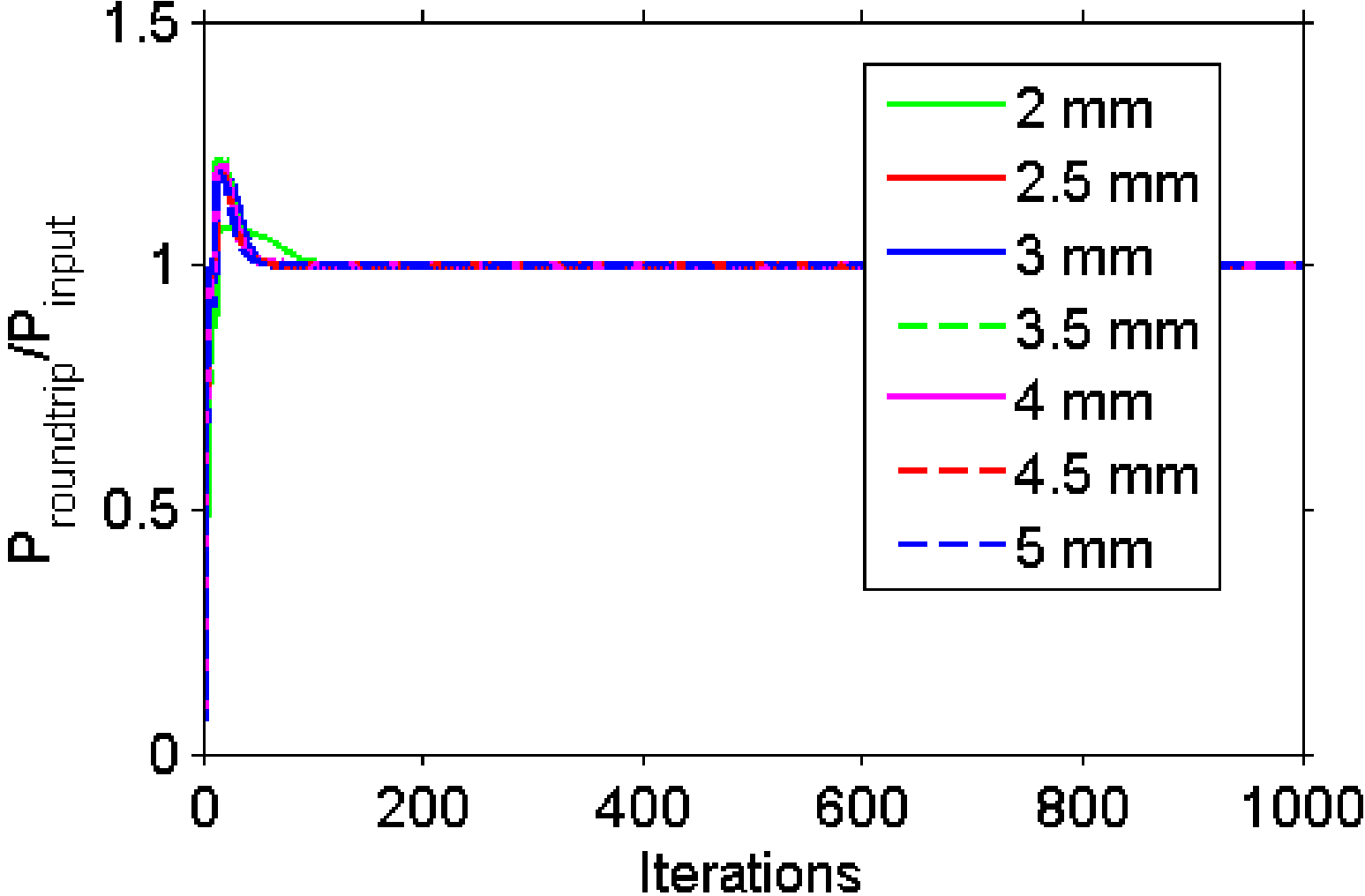
Aperture diameter =
5.0 mm



Output Power Analysis vs. Iteration



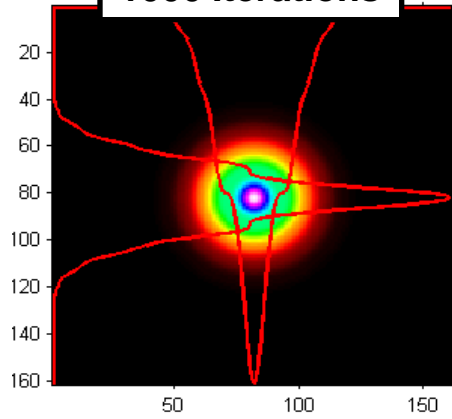
Output Power Ratio vs. Iteration



Comparison of Intensity Profiles

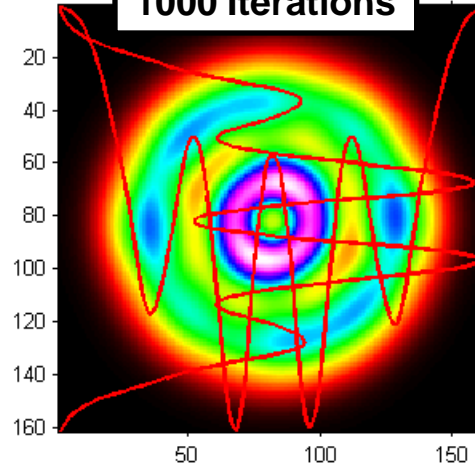
2-mm Aperture

1000 Iterations



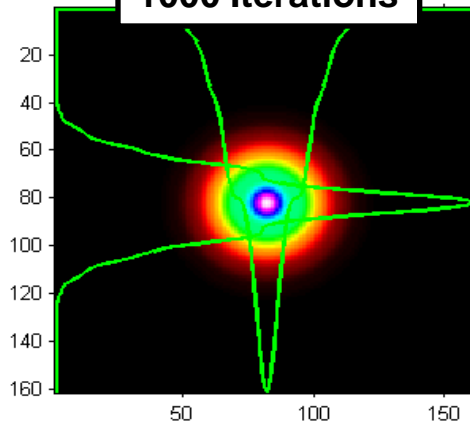
5-mm Aperture

1000 Iterations



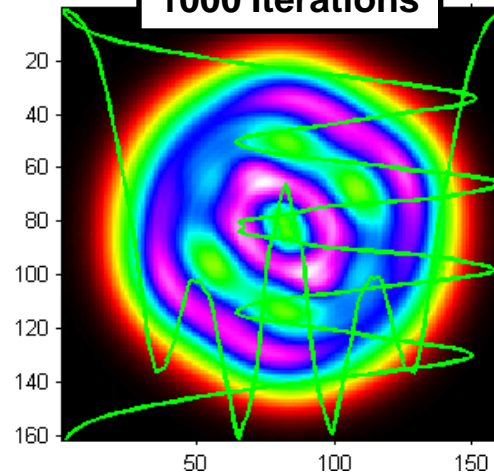
No Averaging

1000 Iterations

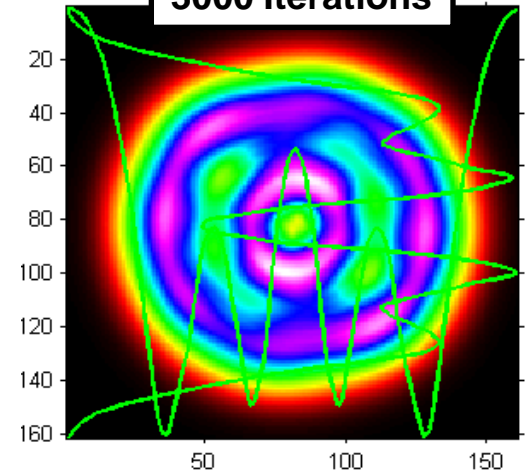


11-Frame Averaging

1000 Iterations

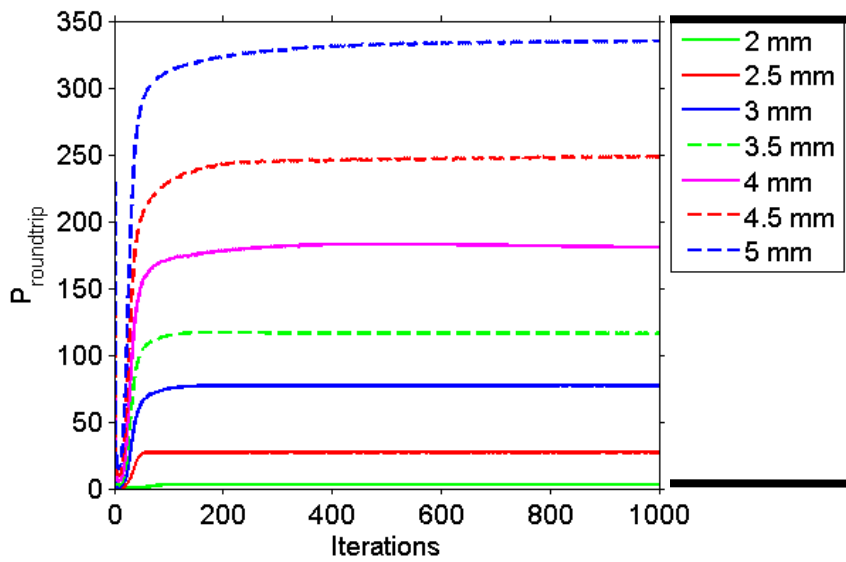


3000 Iterations

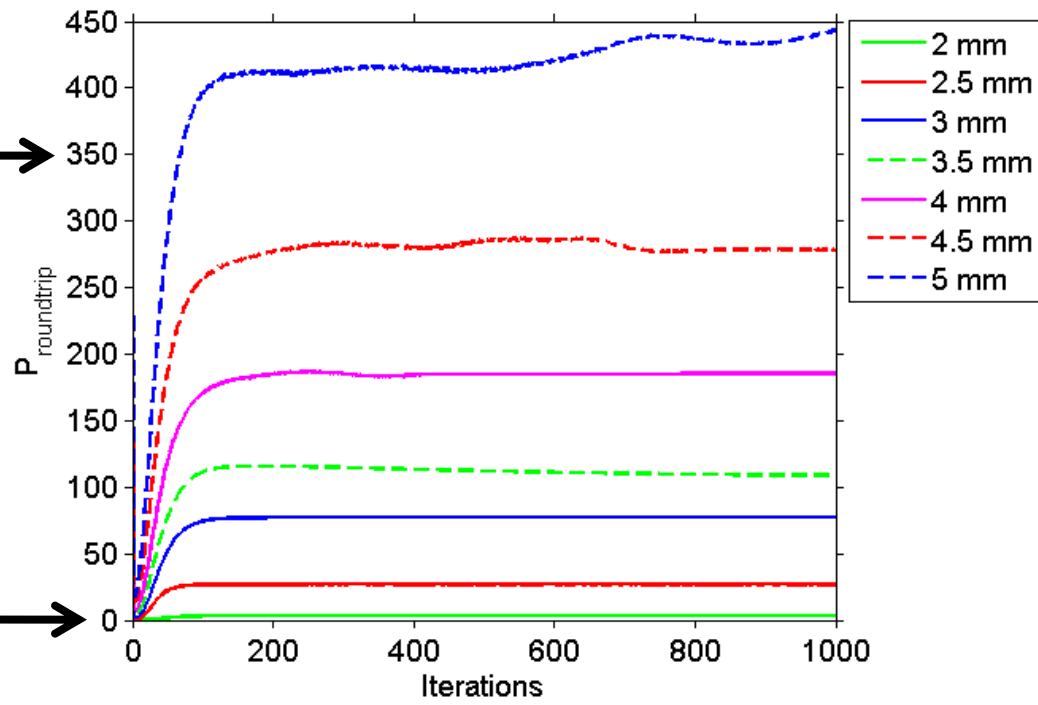


The averaging case converges more rapidly and to a steadier state in the presence of multiple transverse modes running.

11-Frame Averaging



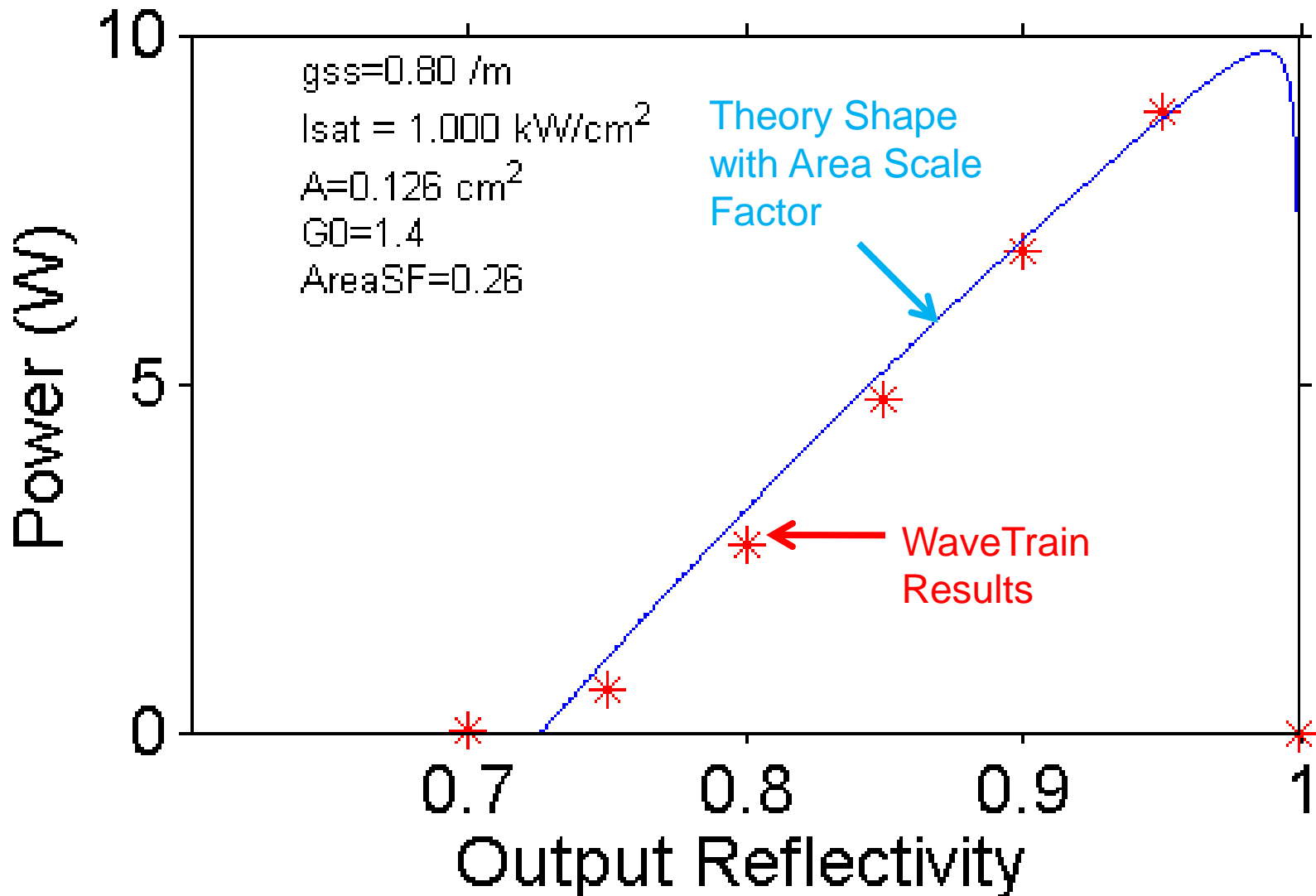
No Averaging



Shape and power Level is comparable for small apertures, but significantly different for larger apertures. We are now trying to anchor to Rigrod power predictions.



Preliminary Rigrod Comparison



Conclusions

- The model of the stable resonator with gain using the internal intensity averaging appears to converge much faster and operate much more stably than the model without the averaging.
- We need to perform more anchoring experiments to complete the verification of this new technique, but the results so far are promising.